

Comb photon and intriguing features
in
Comb laser-atom interaction

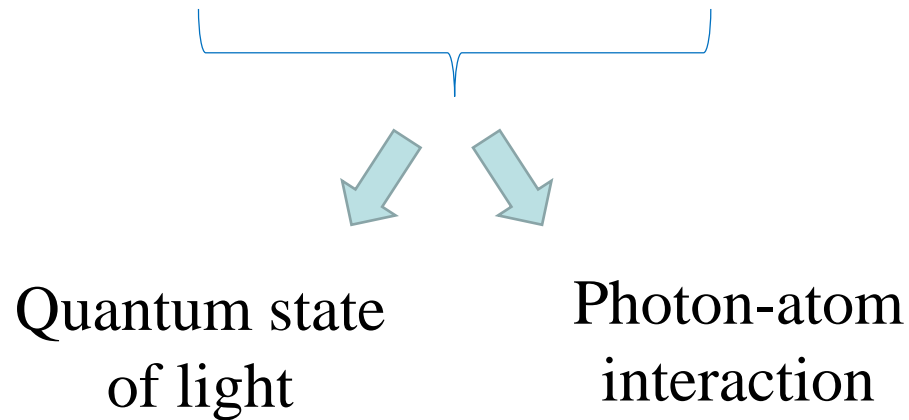
Wang-Yau Cheng (鄭王曜)

Department of Physics, National Central University, Taiwan

2021 workshop on quantum technology

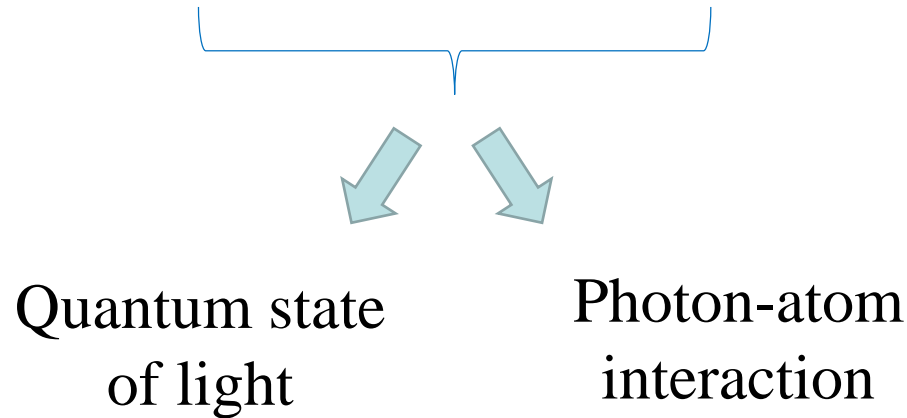
*I am a comb laser or “clock” expert, not
“quantum optics”*

However, it might be a good chance to sell
my unique comb laser to people in the field
of “quantum optics”



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Outline

1. What is comb laser?

→ From the perspective of spectroscopist

→ From the perspective of “quantum optics” people

2. 40-femtosecond pulse train simultaneously resolves Rb and Cs spectra with 3-kHz resolution

1. Spectral line narrowing
2. Multi-pathway AC stark shift
3. Quantum interfered spectra

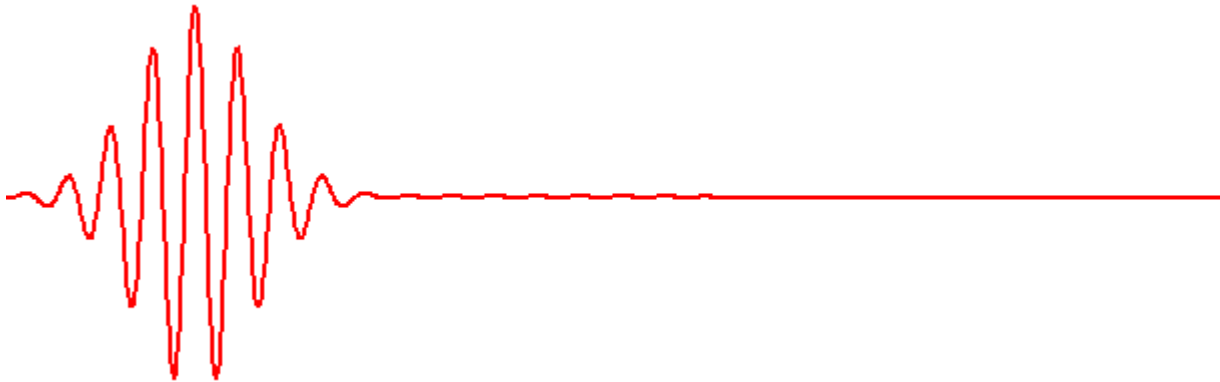
3. Application: a novel comb laser without need of expensive cesium clock

What is comb laser (I):

from the perspective of “laser spectroscopy”

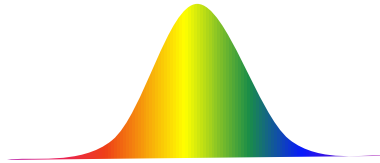
Viewpoint of time domain:

- High peak power (compared to CW laser)
 - Femtosecond time scale
- } Good for **controlling** extremely nonlinear optics
- Fixed carrier-envelope phase → Good for **selecting** atomic quantum states



Viewpoint of frequency domain:

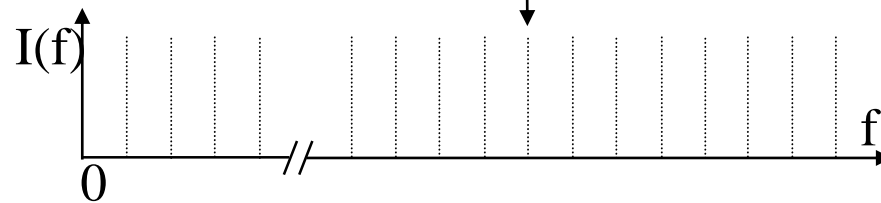
- Wide-band



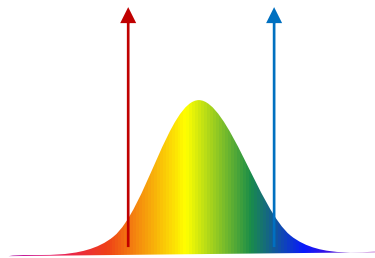
F_n fixed to < 1 kHz instability



- High-resolution



- High coherence



Coherent-state photons
with different colors

In this talk, we demonstrate:

“wide-band (40 nm) & high resolution (5 kHz) laser spectroscopy”

What is comb laser (II):

from the perspective of “quantum optics”

Coherent state is a superposition of Fock states photons

$$|\alpha\rangle_t = e^{-|\alpha|^2/2} \sum_{n=0}^{\infty} \frac{(\alpha e^{-i\omega t})^n}{\sqrt{n!}} e^{-i\omega t/2} |n\rangle$$

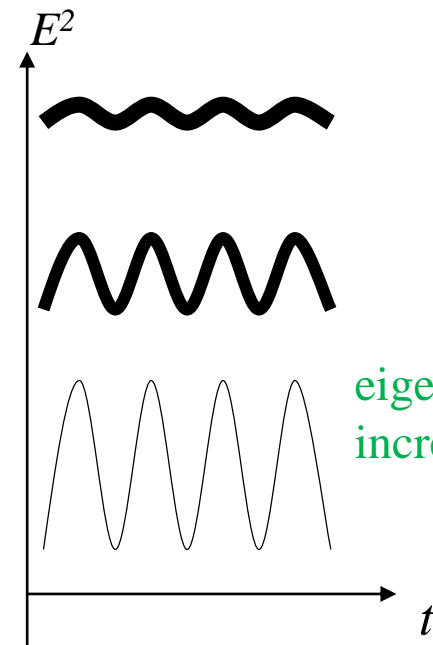
Photon number state

Coherent state photon reach the minimum criteria of uncertainty principle

$$\Delta q \times \Delta p = \frac{1}{2} \hbar$$

$$p \sim H \sim \frac{\partial E}{\partial t} \sim \text{phase of } E$$

$q \sim$ amplitude of E



eigenvalue α increased

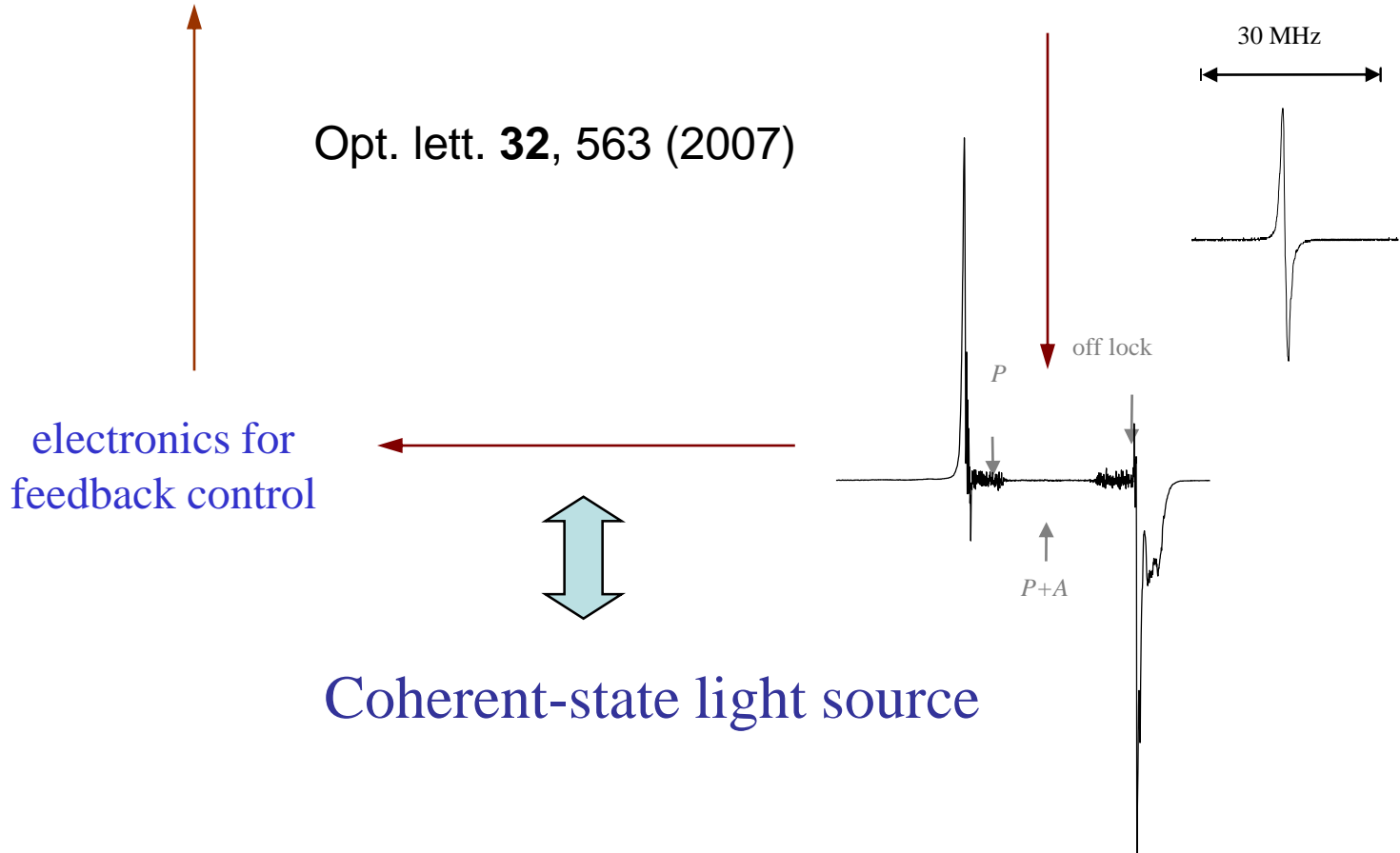
over-complete

$$g^{(2)}(\tau) = 1 \quad \langle \alpha | \alpha' \rangle \neq 0$$

Frequency-stabilized laser provide “Coherent state” photon

frequency instability 40 Hz
Over 3.2×10^{14} Hz duty cycle

cesium 6S-8S
dipole not-allowed transition



Comb laser is a superposition of N ($N=10^5-10^6$)
frequency-stabilized lasers

$$\begin{aligned}
 & |\alpha_{\omega_1}\rangle_t (= e^{-|\alpha|^2/2} \sum_{n=0}^{\infty} \frac{(\alpha e^{-i\omega_1 t})^n}{\sqrt{n!}} e^{-i\omega_1 t/2} |n\rangle) \\
 & + |\alpha_{\omega_2}\rangle_t (= e^{-|\alpha|^2/2} \sum_{n=0}^{\infty} \frac{(\alpha e^{-i\omega_2 t})^n}{\sqrt{n!}} e^{-i\omega_2 t/2} |n\rangle) \\
 & \quad \bullet \\
 & \quad \bullet \\
 & \quad \bullet \\
 & \quad \bullet \\
 & \quad \bullet \\
 & + |\alpha_{\omega_N}\rangle_t (= e^{-|\alpha|^2/2} \sum_{n=0}^{\infty} \frac{(\alpha e^{-i\omega_N t})^n}{\sqrt{n!}} e^{-i\omega_N t/2} |n\rangle)
 \end{aligned}$$

They all have the same phase (mode locked)

$$\Delta q \times \Delta p = \frac{1}{2} \hbar$$

$q \sim \text{amplitude of } E$

$p \sim H \sim \frac{\partial E}{\partial t} \sim \text{phase of } E$

Superposition of all coherence-state light with wide-band mode locked carrier frequencies (femtosecond pulse train)



Via Spontaneous down conversion



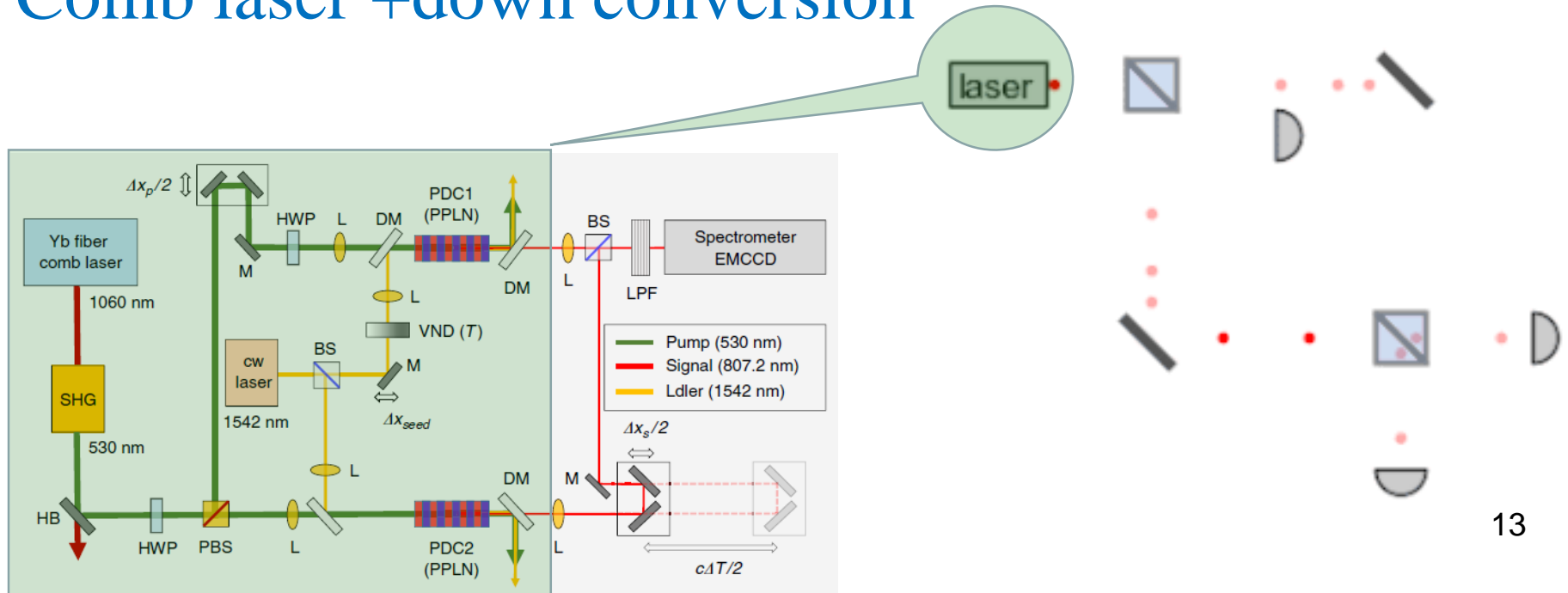
Still keep the anti-bunching property

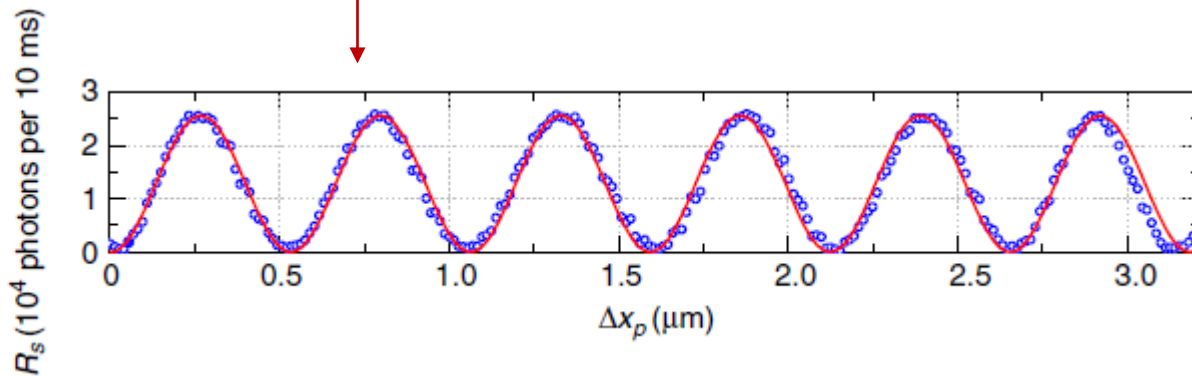
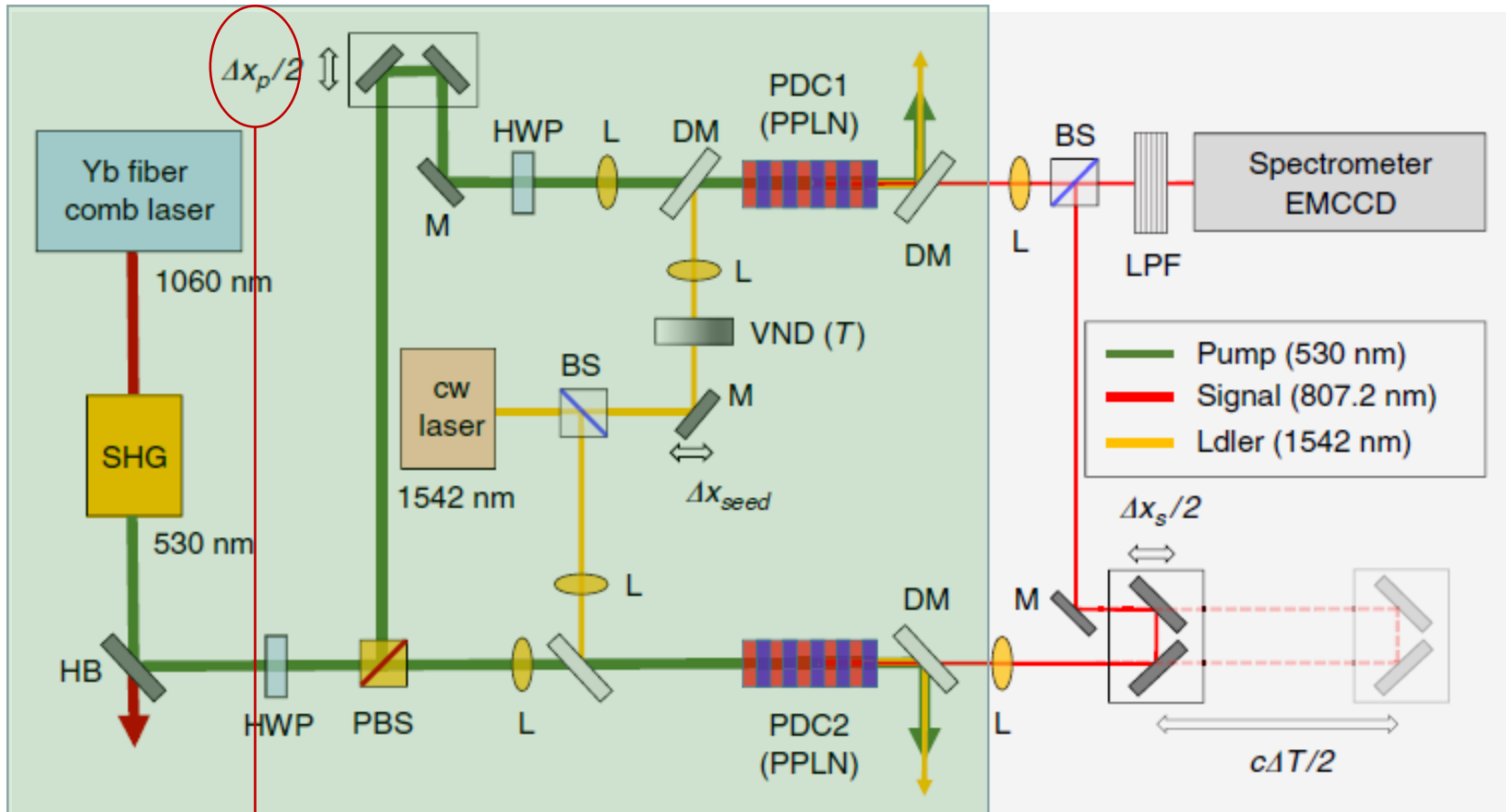
Frequency comb single-photon interferometry

Sun Kyung Lee¹, Noh Soo Han¹, Tai Hyun Yoon^{1,2} & Minhaeng Cho^{1,3}

Use comb laser as a light source for “which-way interferometer” experiment

Comb laser +down conversion





Application:
 Quantum metrology
 (Quantum tick-tack clock)

Their very recent report by using comb laser:

SCIENCE ADVANCES | RESEARCH ARTICLE

PHYSICS

Quantitative complementarity of wave-particle duality

Tai Hyun Yoon^{1,2*} and Minhaeng Cho^{1,3*}

Yoon and Cho, *Sci. Adv.* 2021; **7** : eabi9268

18 August 2021

Quantum interference in comb laser-atom interaction

Tz-Wei Liu

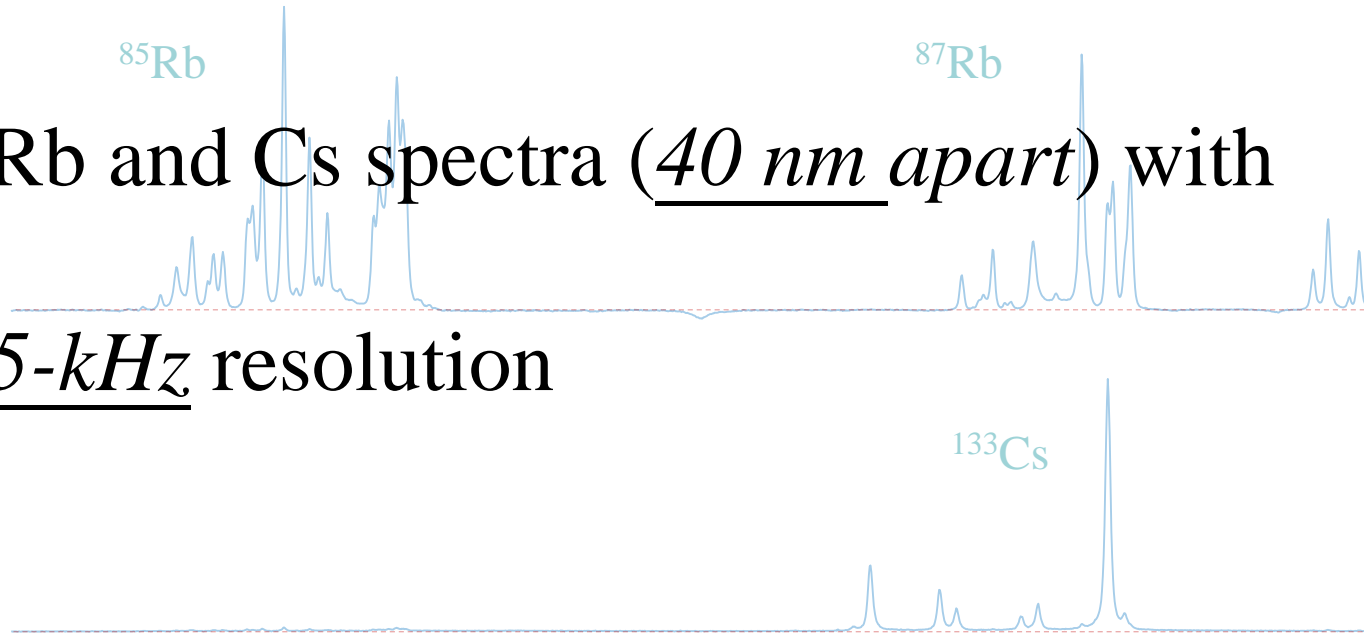


He is currently looking for a teaching job

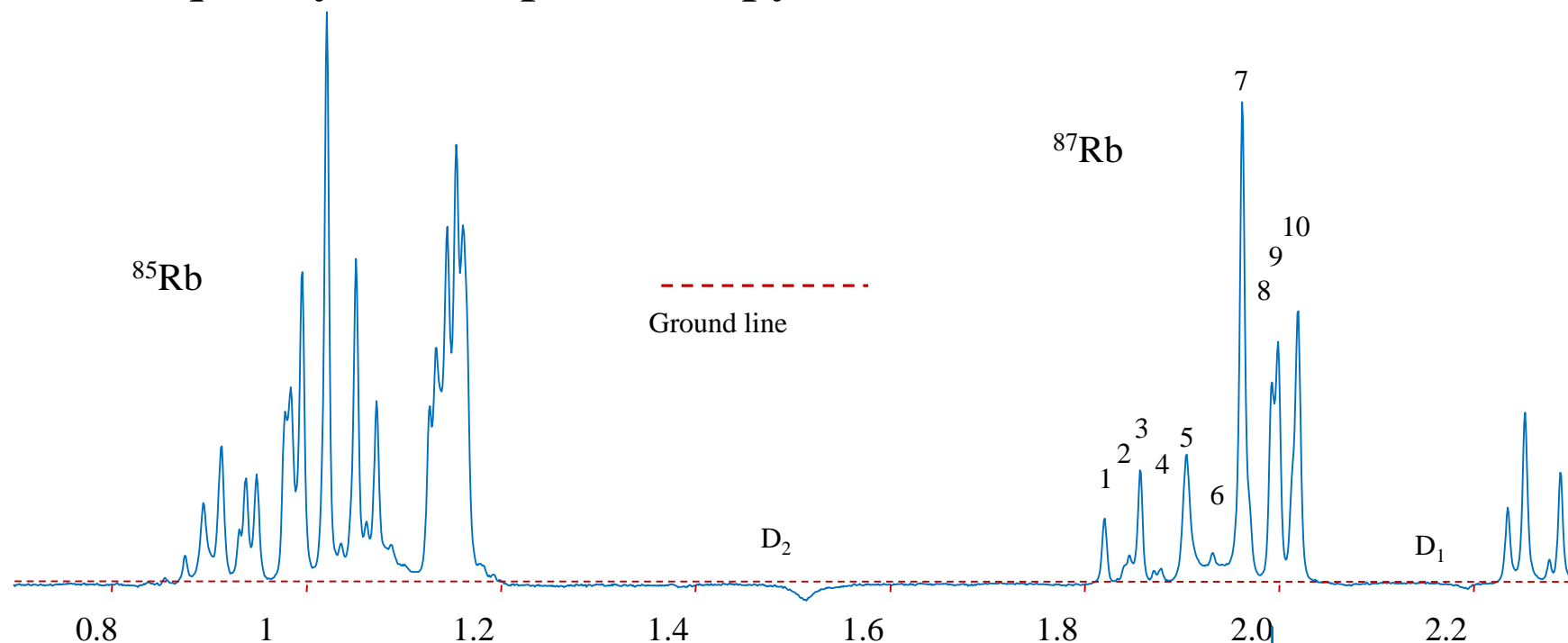
40×10^{-15} second pulse laser

Simultaneously resolves

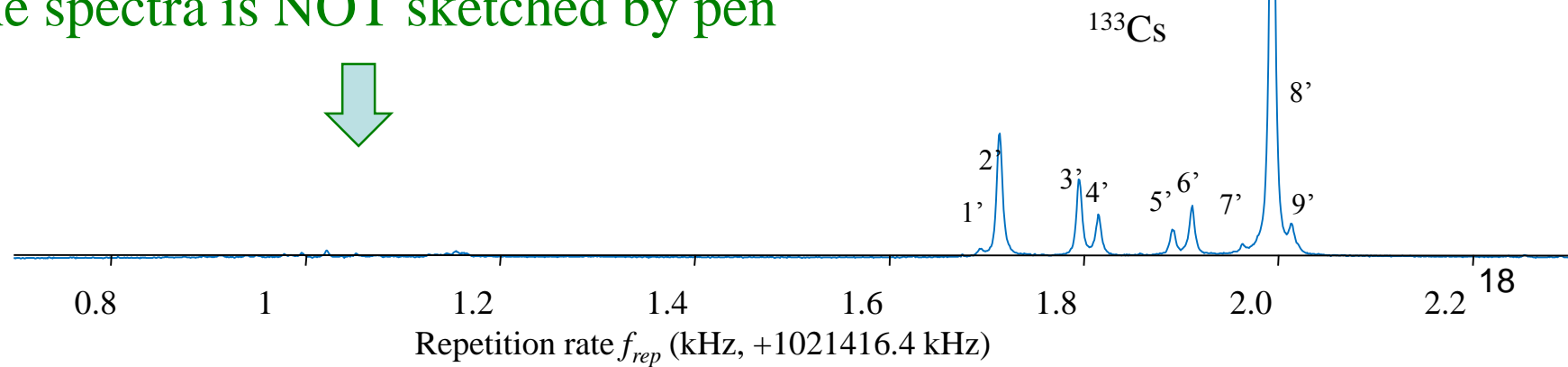
Rb and Cs spectra (40 nm apart) with
 5-kHz resolution



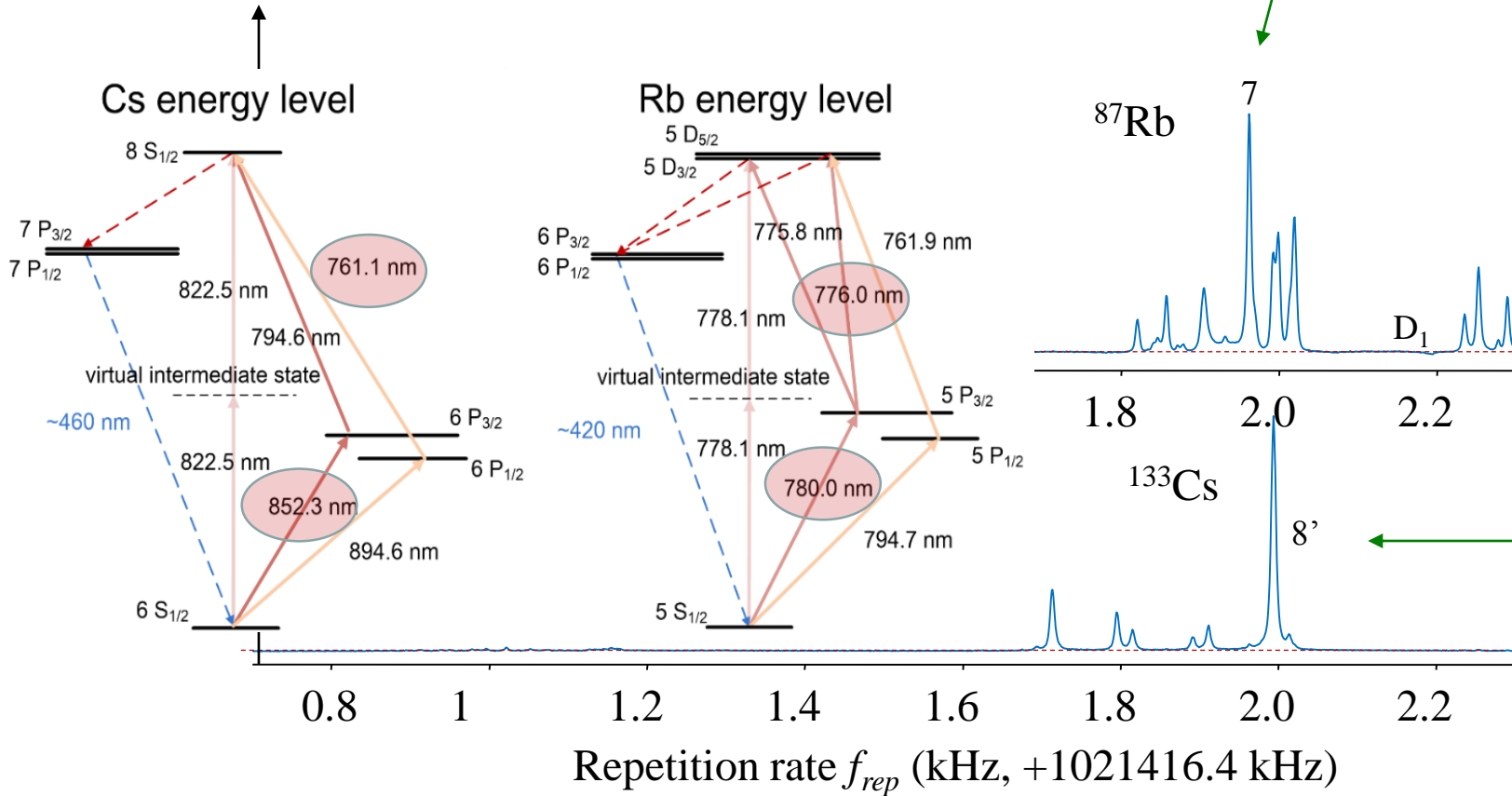
Direct frequency comb spectroscopy in record resolution



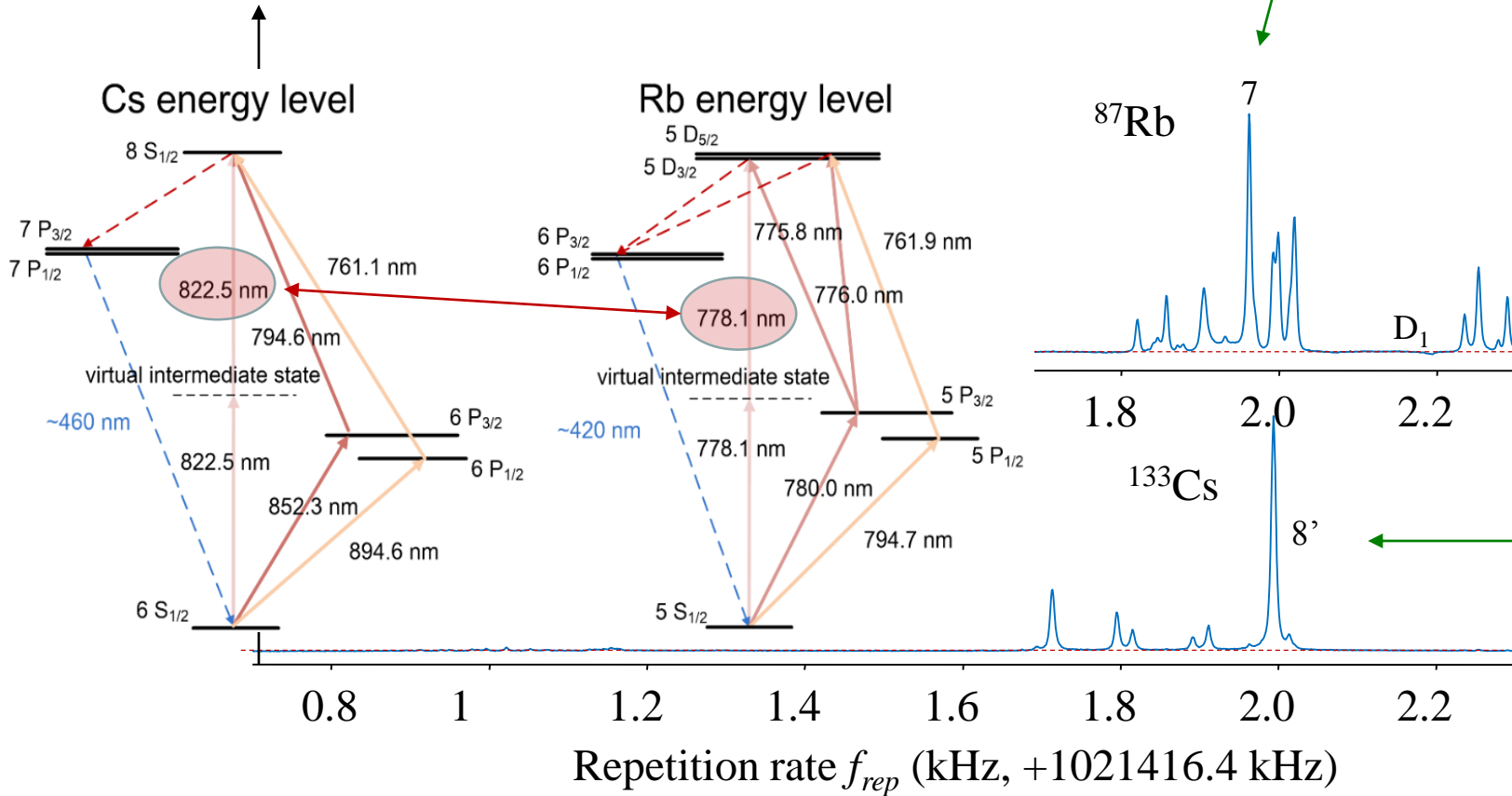
The spectra is NOT sketched by pen



Two clock transitions



The two clocks separates for 40 nm, resolved simultaneously



Some intriguing spectral features (I)

Line narrowing

Doppler-free two-color spectroscopy of the $6_2S_{1/2}-8_2S_{1/2}$ cesium transition using semiconductor diode lasers

C. Fort¹, M. Inguscio¹, P. Raspollini¹, F. Baldes², A. Sasso²

Appl. Phys. B 61, 467-472 (1995)

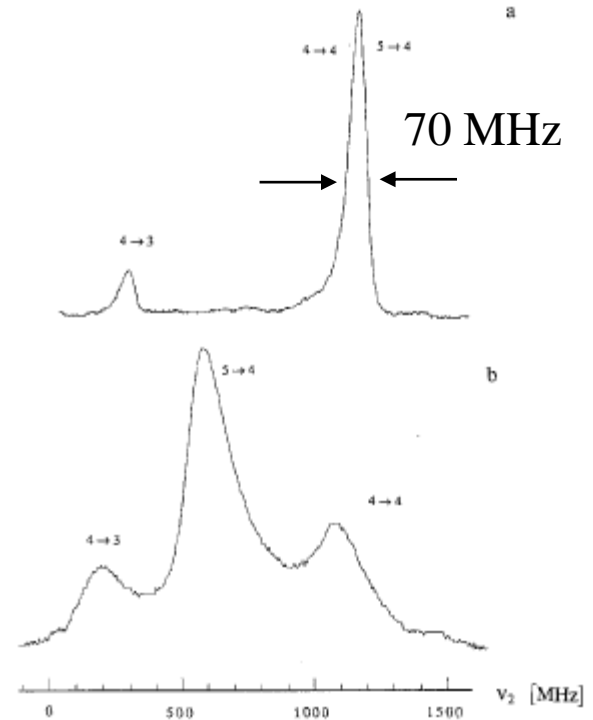
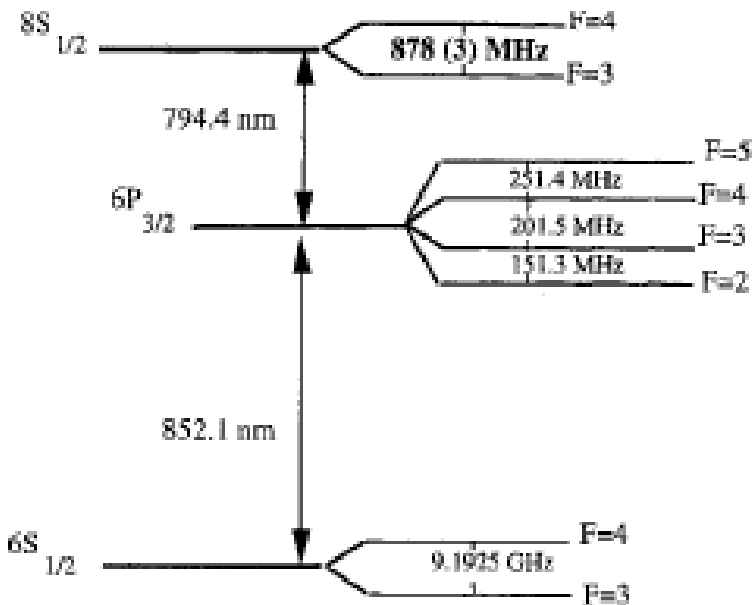


Fig. 6a,b. Two-color transition with DL1 locked onto the $F=4-F=5$ cross-over resonance. The hyperfine structure of the final state $8S$ is partially resolved with the counterpropagating scheme (a) while it is fully resolved with copropagating laser beams (b)

Fig. 4. Energy-level diagram of the relevant cesium states and the relative transitions involved in this experiment

Doppler-free two-color spectroscopy of the $6_2S_{1/2}-8_2S_{1/2}$ cesium transition using semiconductor diode lasers

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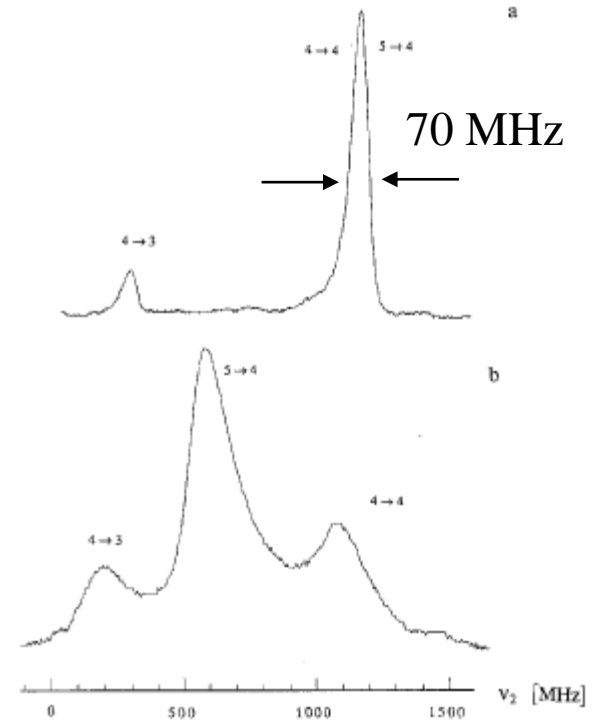
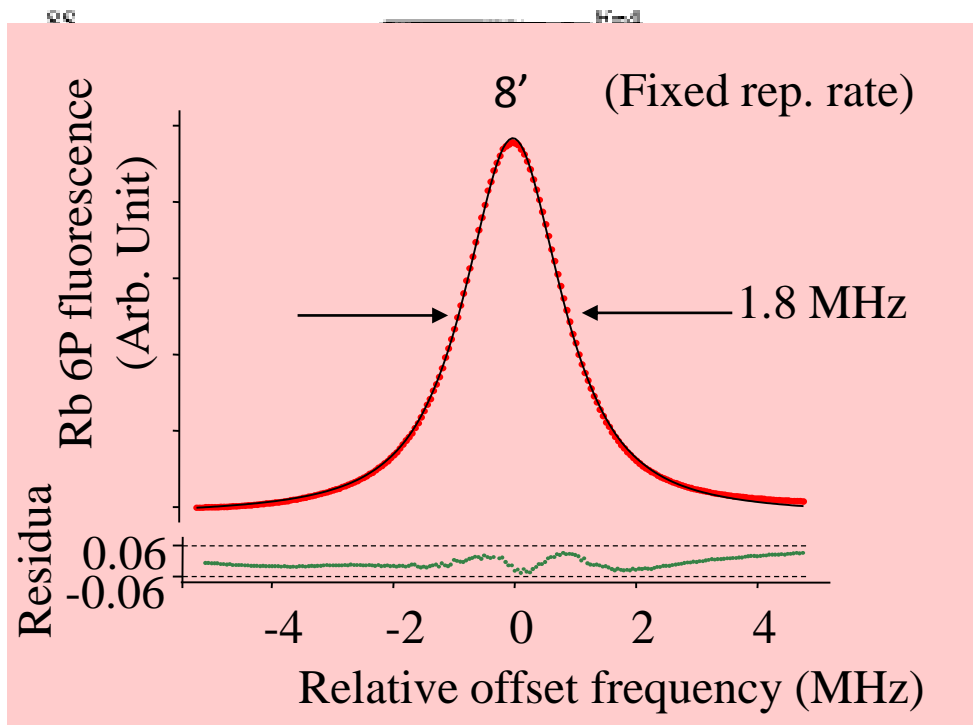
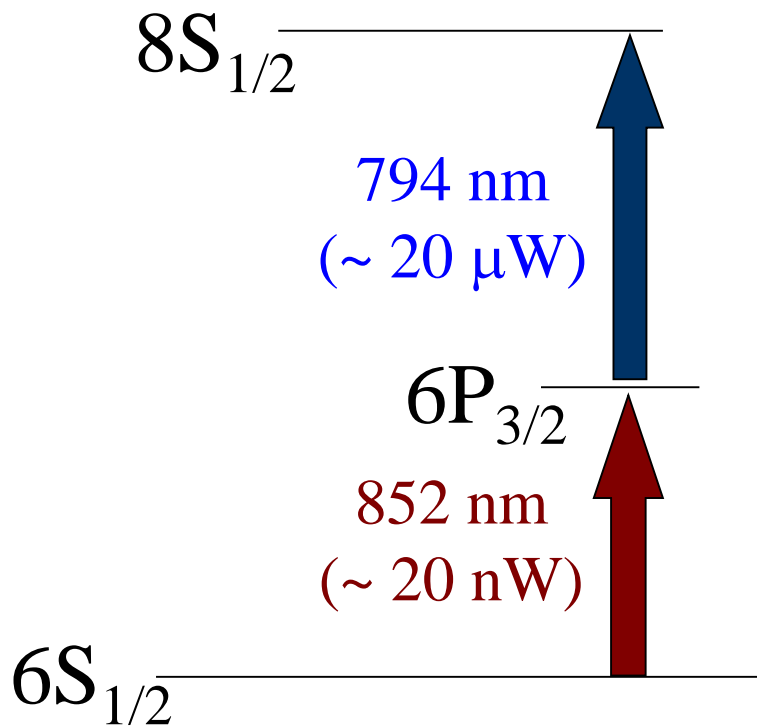


Fig. 6a,b. Two-color transition with DL1 locked onto the $F=4-F=5$ cross-over resonance. The hyperfine structure of the final state 8S is partially resolved with the counterpropagating scheme (a) while it is fully resolved with copropagating laser beams (b)



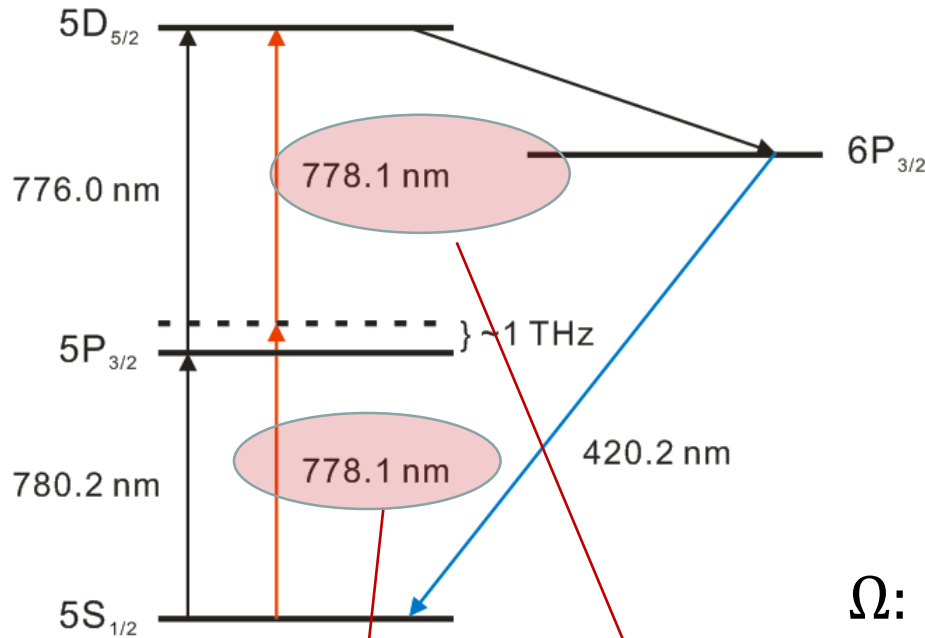
The intermediate state is **transparent?**

Some intriguing spectral features (II)

Multi-pathway AC stark shift

CW-clocks

^{85}Rb

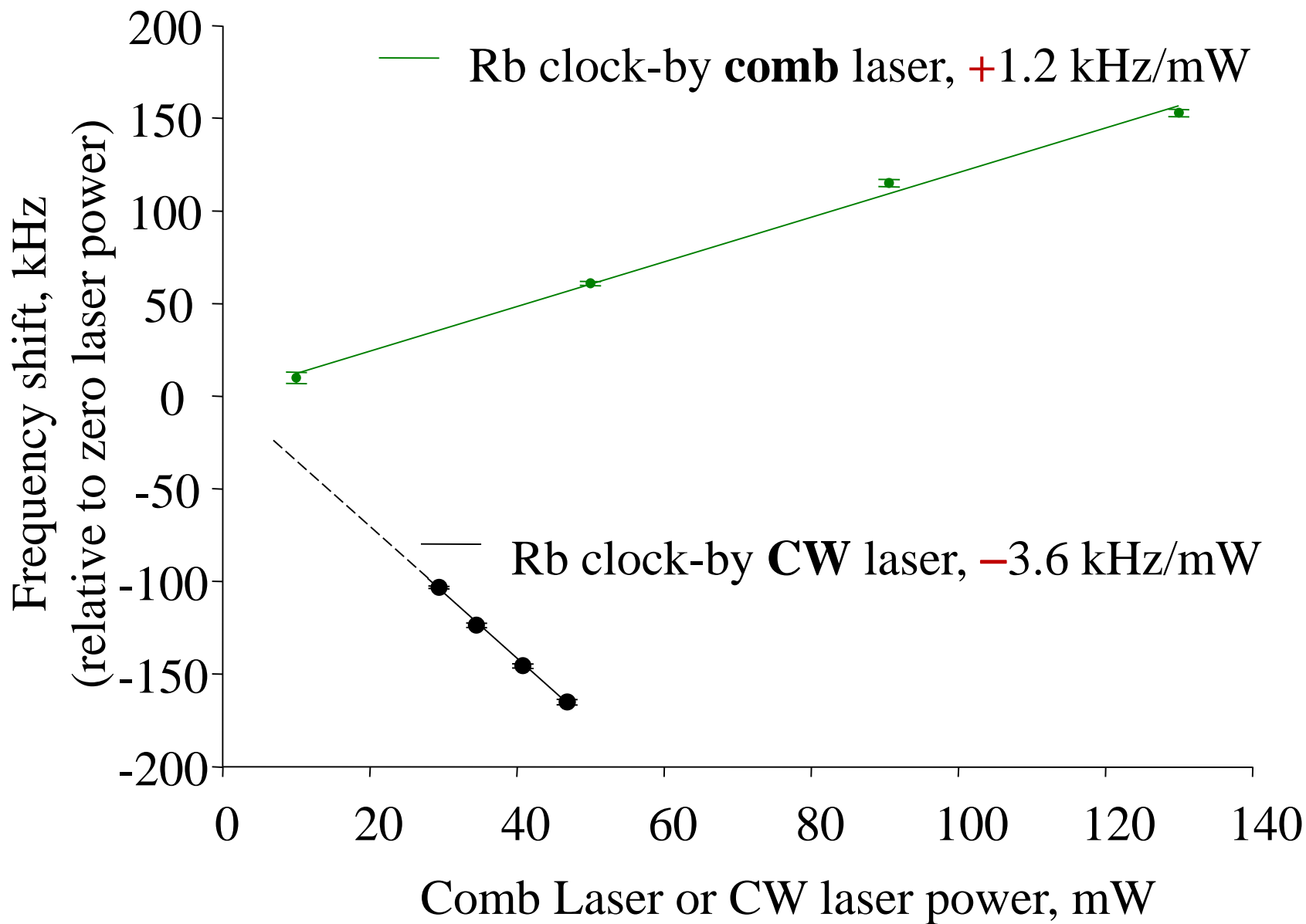


Ω : Rabi frequency
 S_i : frequency shift

$$S_{fg} = S_f - S_g = - \sum_m \left(\frac{\Omega_{mg}^2}{\omega_L - \omega_{mg}} + \frac{\Omega_{fm}^2}{\omega_{fm} - \omega_L} \right)$$

Single pathway: Ladder direct two-photon yields red shift

Most concerned issue in clock !!

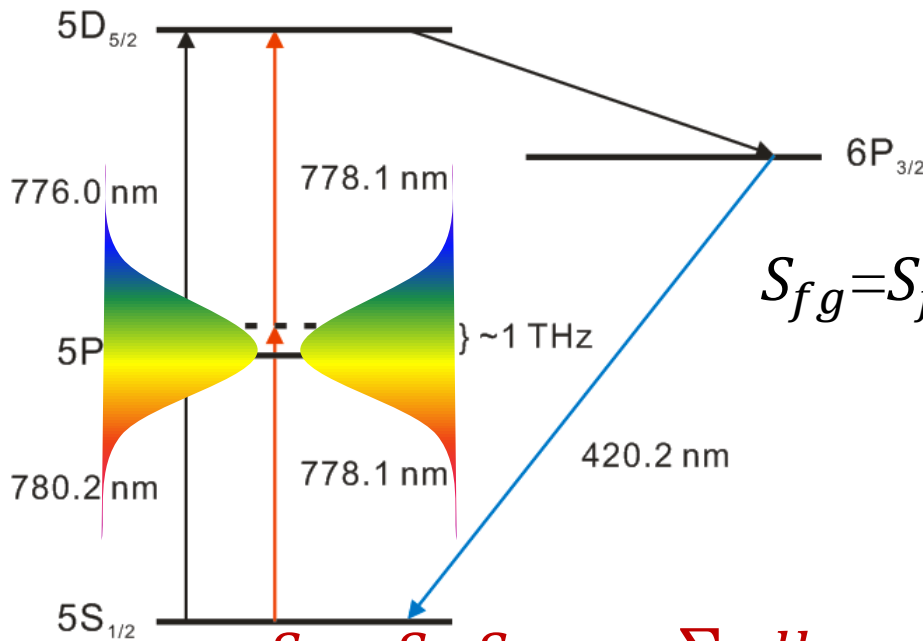


CW-clocks

Multi-paths induced AC stark shift



^{85}Rb



$$S_{fg} = S_f - S_g = - \sum_{\mathbf{m}} \left(\frac{\Omega_{mg}^2}{\omega_L - \omega_{mg}} + \frac{\Omega_{fm}^2}{\omega_{fm} - \omega_L} \right)$$



$$S_{fg} = S_f - S_g = - \sum \text{all comb modes} \sum_{\mathbf{m}} \left(\frac{\Omega_{mg}^2}{\omega_L - \omega_{mg}} + \frac{\Omega_{fm}^2}{\omega_{fm} - \omega_L} \right)$$

Question: Would it be possible to quantum controlling the AC stark shift to be zero by pulse shaping?



陽明交通大學

寺西慶哲 教授

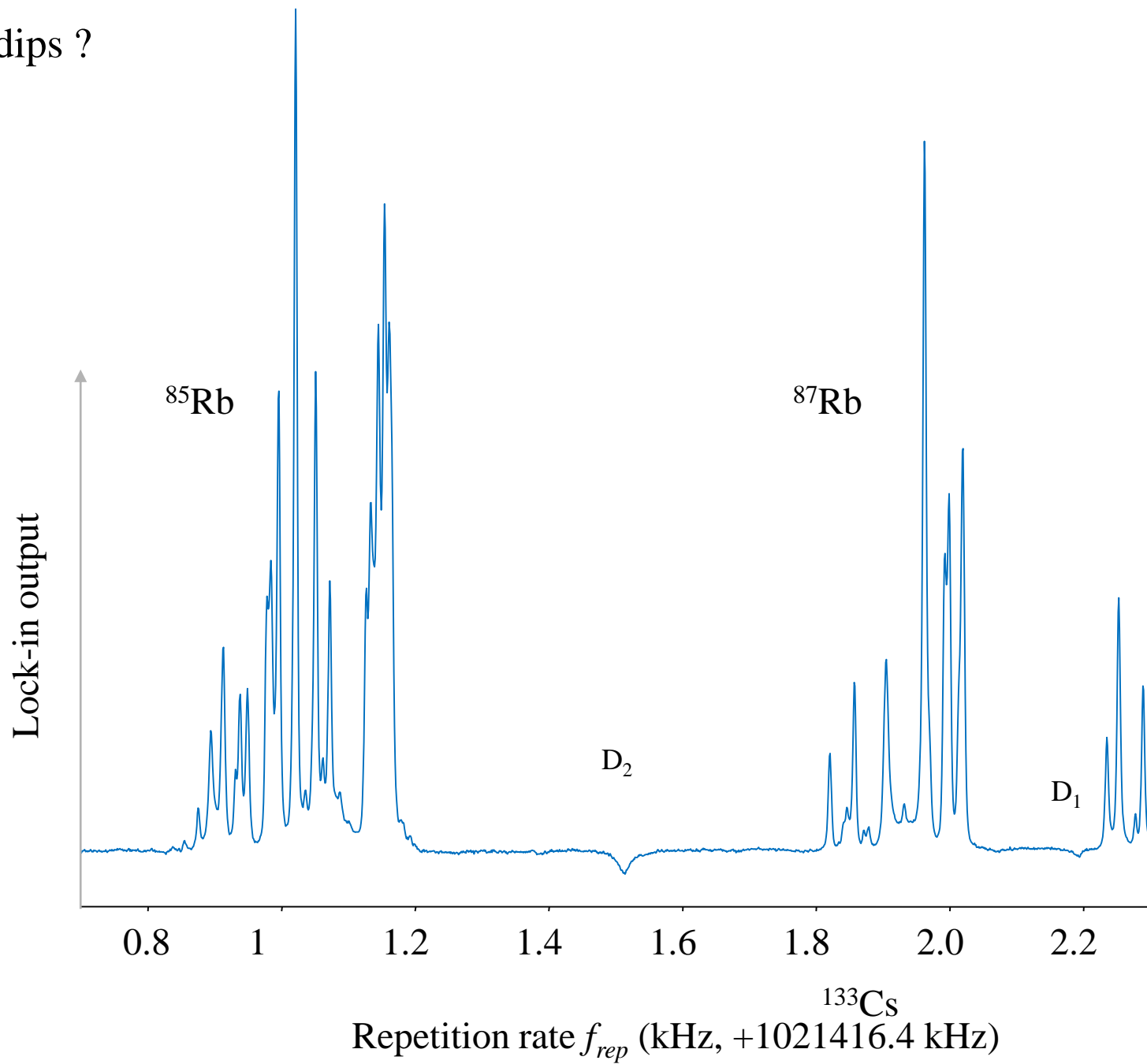
•[物理研究所](#)

Most concerned issue in clock !!

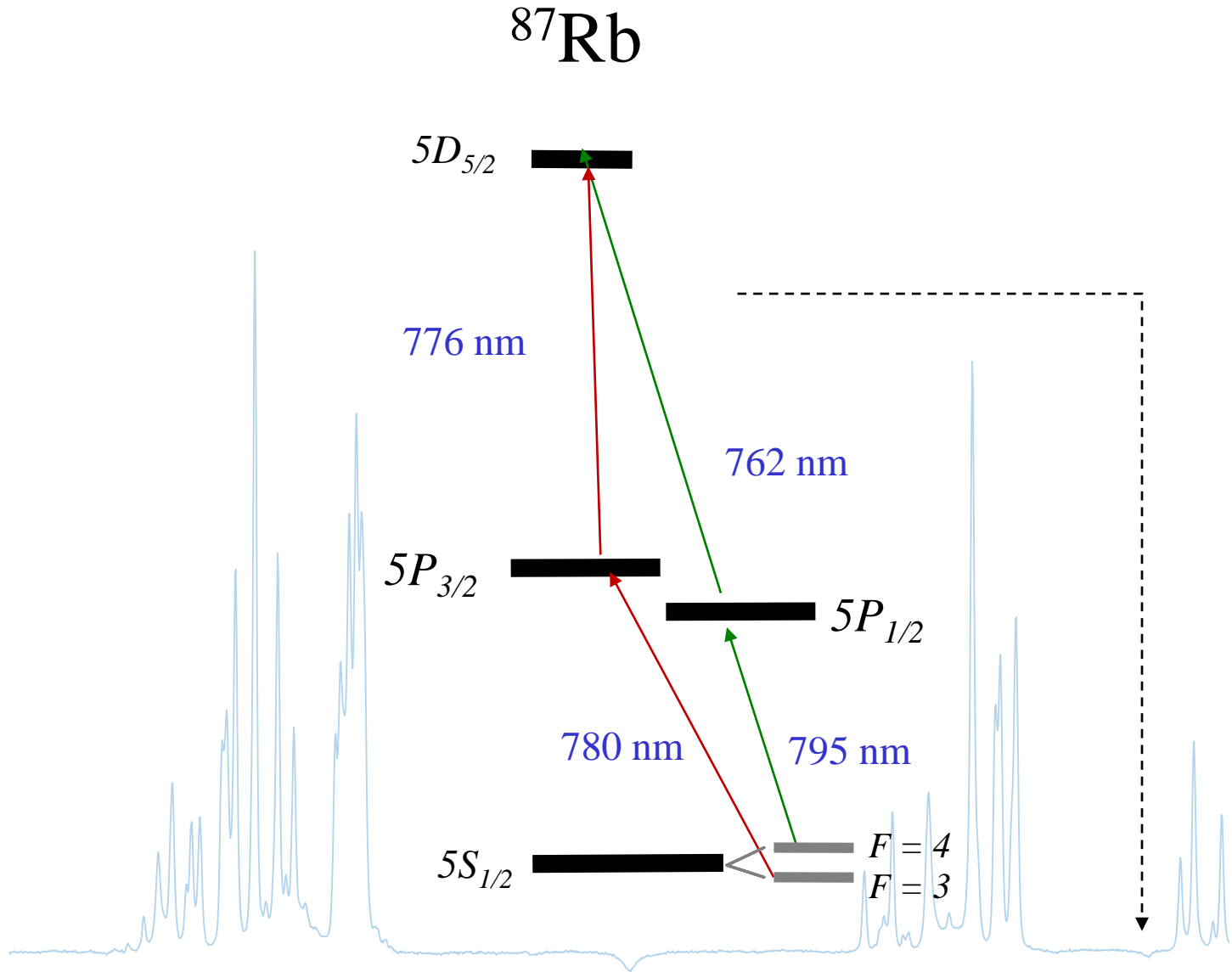
Some intriguing spectral features (III)

Quantum interference by different comb modes

Why dips ?



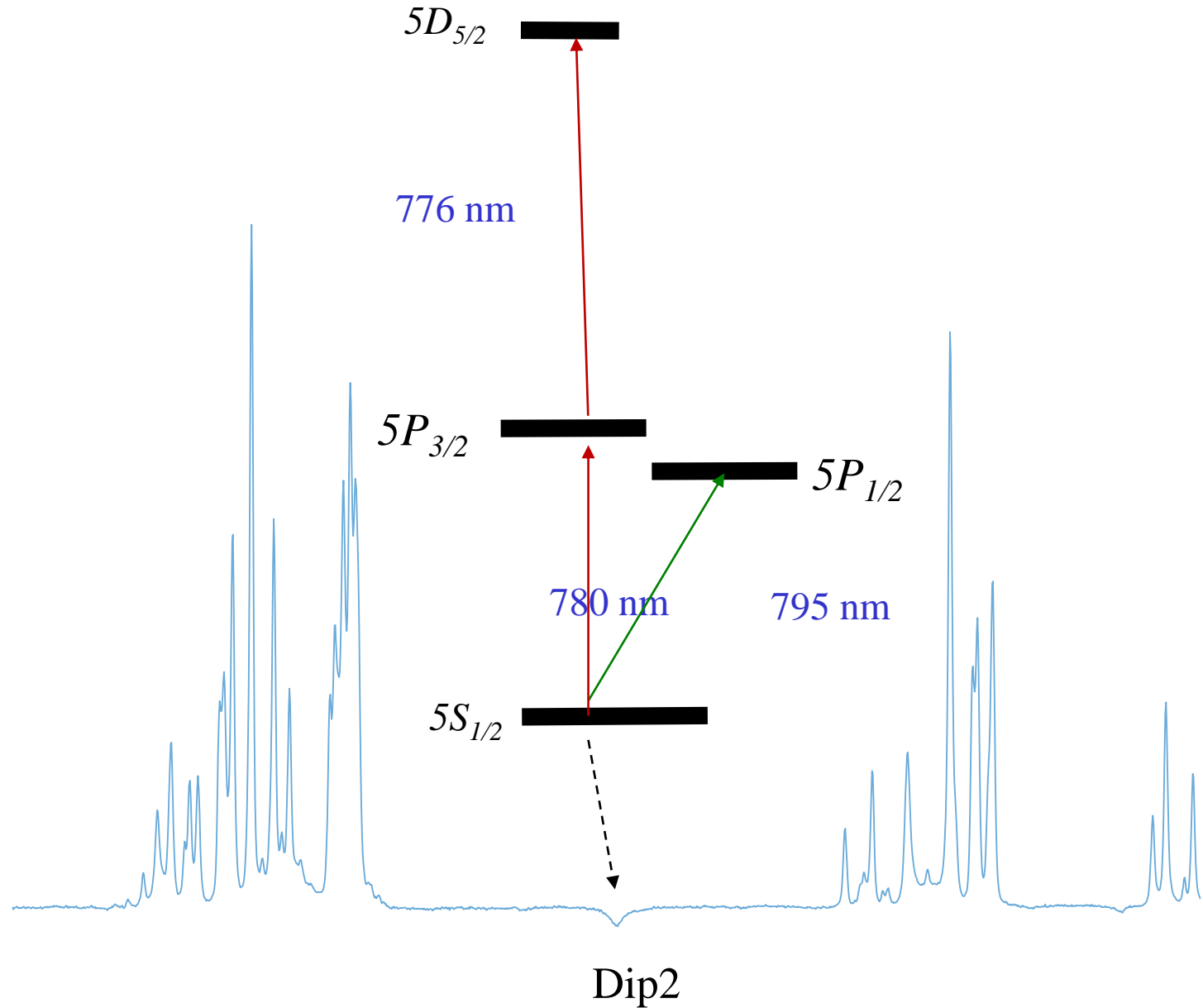
Two-pathway quantum interference



Dip1

V type EIT interference

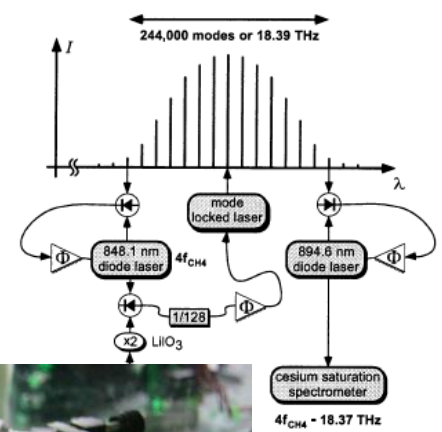
^{87}Rb



Application:

Direct comb clocks

Ted Hansch



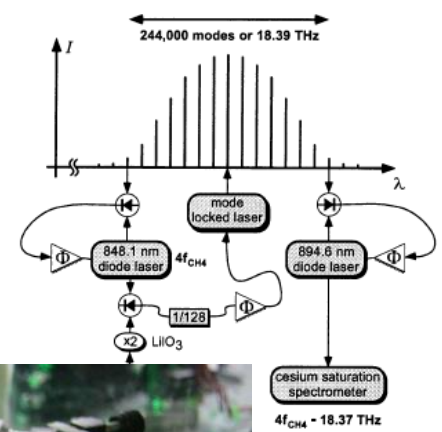
Jan Hall



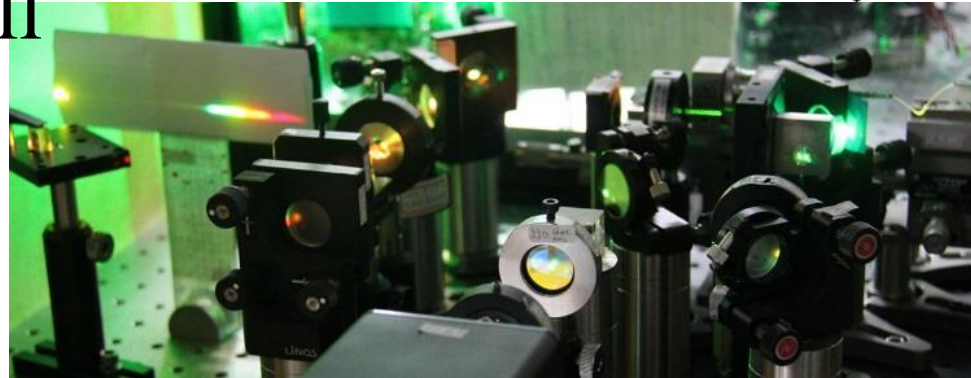
6 182 599 937 (23) Hz

They all need a Cs clock to lock rep. rate!!

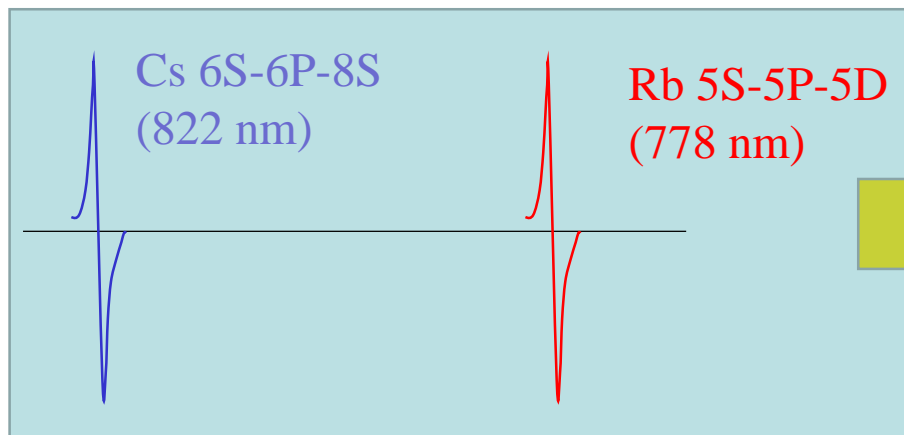
Ted Hansch



Jan Hall

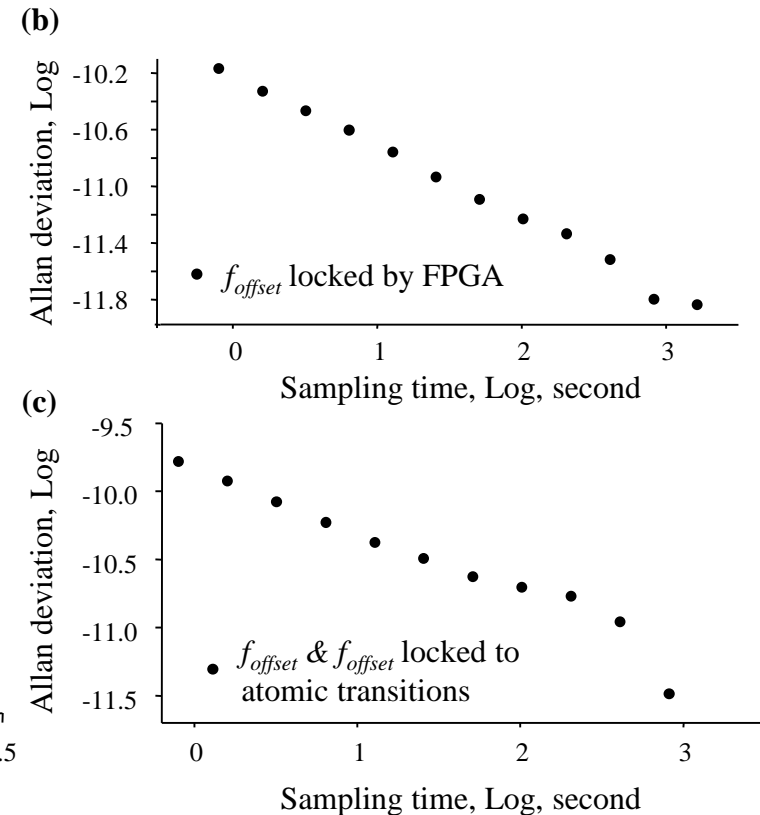
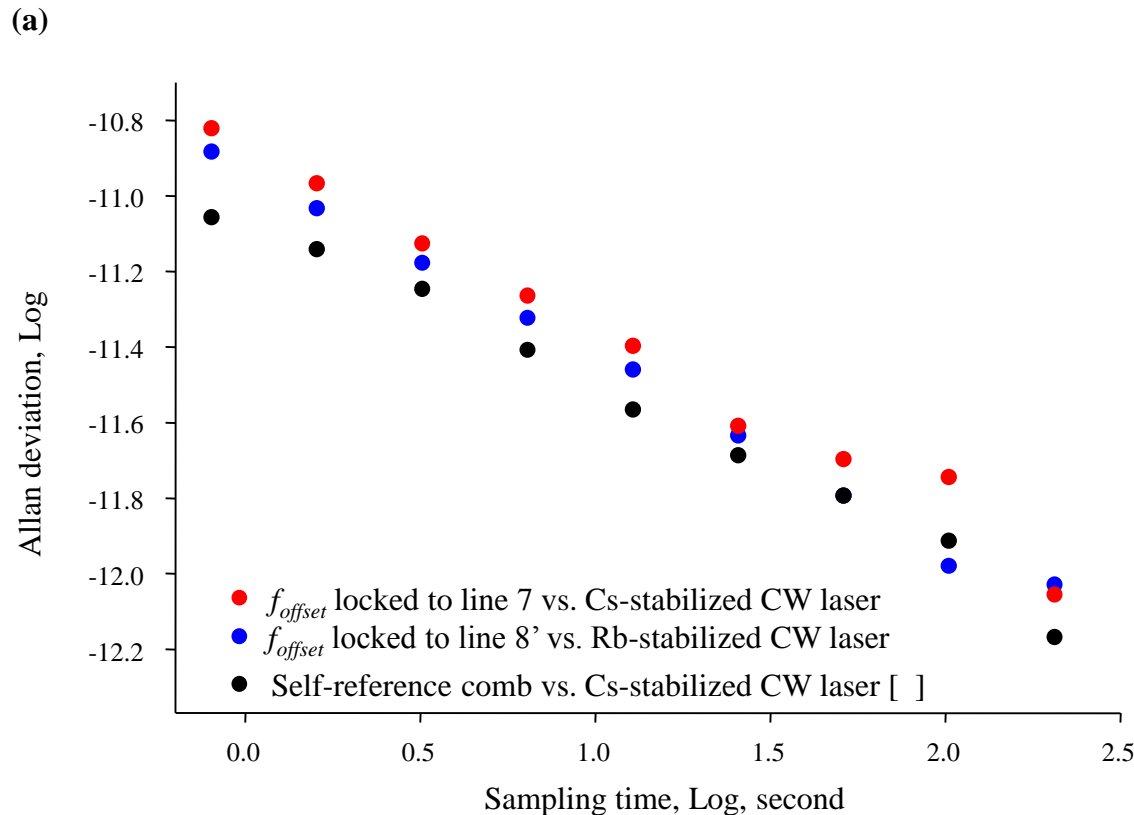


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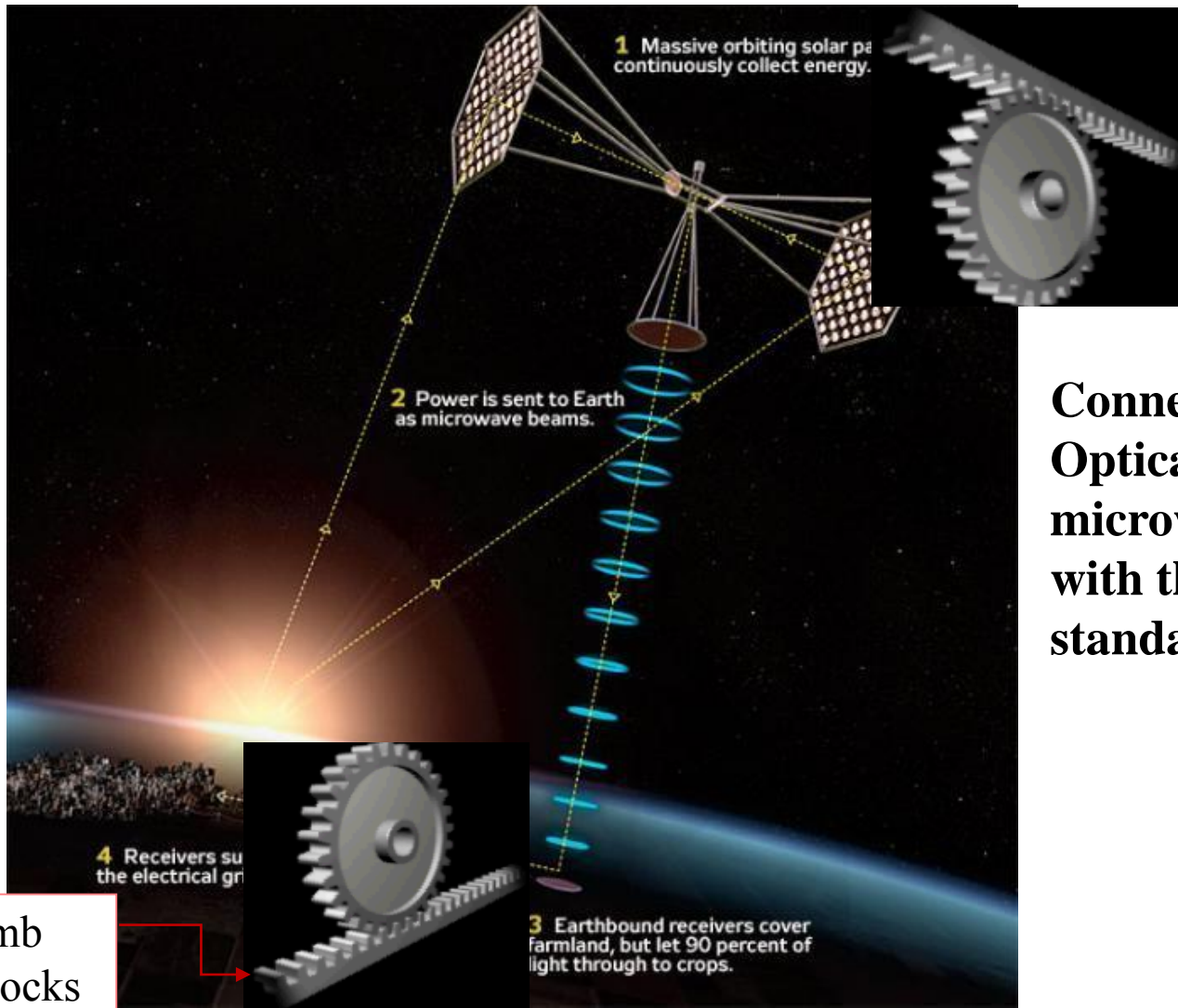
We locked two parameters directly with two spectra (without Cs clock)

Now we need merely one 6-cm Cs/Rb mixed cell to build up comb clocks



Future direction (1)

Comb laser in artificial satellite



**Connects both
Optical and
microwave clocks
with the ground
standards**

Ground comb
laser and clocks

Future direction (2)

You can entangle comb photon

PRL 107, 030505 (2011)

PHYSICAL REVIEW LETTERS

week ending
15 JULY 2011

Parallel Generation of Quadripartite Cluster Entanglement in the Optical Frequency Comb

Matthew Pysher,¹ Yoshichika Miwa,² Reihaneh Shahrokhsahi,¹ Russell Bloomer,¹ and Olivier Pfister^{1,*}

You can squeeze comb photon

PRL 108, 083601 (2012)

PHYSICAL REVIEW LETTERS

week ending
24 FEBRUARY 2012

Generation and Characterization of Multimode Quantum Frequency Combs

Olivier Pinel,¹ Pu Jian,¹ Renné Medeiros de Araújo,¹ Jinxia Feng,^{1,2} Benoît Chalopin,^{1,3}
Claude Fabre,^{1,*} and Nicolas Treps¹

You can apply comb photon on quantum computation

PRL 101, 130501 (2008)

 Selected for a [Viewpoint](#) in *Physics*
PHYSICAL REVIEW LETTERS


week ending
26 SEPTEMBER 2008

One-Way Quantum Computing in the Optical Frequency Comb

Nicolas C. Menicucci,^{1,2} Steven T. Flammia,³ and Olivier Pfister⁴

You can use comb laser to entangle atomic Qubits

PRL **104**, 140501 (2010)

 Selected for a Viewpoint in *Physics*
PHYSICAL REVIEW LETTERS

week ending
9 APRIL 2010



Entanglement of Atomic Qubits Using an Optical Frequency Comb

D. Hayes,^{*} D. N. Matsukevich, P. Maunz, D. Hucul, Q. Quraishi, S. Olmschenk, W. Campbell, J. Mizrahi,
C. Senko, and C. Monroe

Acknowledgement:

Telecommun. Labs. (中華電信研究所)

Ministry of Science and Technology (科技部)

partner in next step:



陽明交通大學

寺西慶哲 教授

• 物理研究所



中央研究院

張銘顯 研究員

• 原子分子研究所



中央大學

陳彥宏 教授

• 光電研究所



中央大學

李依珊 教授

• 電機研究所