# Advances in photonic quantum information science

<u>Geoff Pryde</u>

## prydelab.net



Centre for Quantum Dynamics



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## Photonic quantum information science

A lecture in two parts:

- 1. Photons, photonic tools, and optical quantum information science
- 2. Quantum steering, demonstrated and studied with photons

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#### Part 1 outline

- 1. Optics **basics**
- 2. Quantum optical encodings
- 3. Quantum optics **technologies** sources and detectors
- 4. Application: Unconditional **quantum metrology** with photons

#### Some reading:

Slussarenko and Pryde, "Photonic quantum information processing: a concise review," arXiv:1907.06331

Ralph and Pryde, "Optical quantum computation," *Progress in Optics* **54**, 209 (2009); arXiv:1103.6071

Banaszek et al., "Quantum states made to measure," Nature Photonics 3, 673 (2009); Griffith arXiv:0912.4092

## Why photons?

#### Optics provides low-noise quantum systems

- Encoded information can be robust
  - e.g. polarization is well maintained in vacuum – light from the Crab nebula is still polarized after travelling 6500 light years



 Technical noise is much lower than optical quantum noise







## Why photons?

#### Optical systems are readily manipulated

- Precision control of optical beams, frequencies, polarization, intensity, etc
- Interferometry, imaging...









## Why photons?

#### Light is excellent for transmitting information

- Existing optical communications industry
- Basis of telephony, internet, long-range sensing etc.







#### **Optics basics**

- Light is a wave...
- ... or a particle...
- ... or both.



• Need two important concepts:

MODES

and

**PHOTONS** 





#### Photons

- Want to quantize optical fields
- Add energy in chunks → photons
- Approx. view: wave packets (modes) with quanta of energy



Mode **b**, 1 photon (say)

$$|1
angle=\hat{b}^{\dagger}|0
angle$$

General (pure) state of mode:  $|\psi
angle=lpha|0
angle+eta|1
angle+\gamma|2
angle+\delta|3
angle+\dots$ 



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## Modes and photons together

- Work in the Heisenberg picture...
  - … how creation operators change as they interact with optical elements
- Transforming photons means manipulating modes







#### Quantum optical encodings

- The idea of quantum information science and technology is to encode information into quantum states
- We'll mostly be concerned with **qubits**
- Let's mention two encodings (others also possible):
  - Coherent states and continuous variables (not discussed today)
  - Dual rail encoding of photons



#### Dual rail encoding

• Encode a qubit in one photon across two modes



• Common case: same spatial mode; a = H; b = V



#### **Dual rail encoding**

• Encode a qubit in one photon across two modes



• Common case: same spatial mode; a = H; b = V

### Rotating and measuring photon polarisation qubits



# Hadamard gate $|H\rangle = \frac{\lambda/2}{2} (|H\rangle + |V\rangle)/\sqrt{2}$

Arbitrary rotation gate



A. White

## Quantum optics technologies

- How do we work with quantum states of light?
- We need to

MAKE,

**MEASURE** and

#### MANIPULATE them.

• Let's take a look at the technologies for each of these, with an emphasis on **photons**.



#### Cartoon picture of optical quantum information tech.

(not necessarily general or completely accurate, but indicative)



#### Photon sources

- What's needed?
  - Sources of single photons and/or
  - Sources of entangled photons



## Making photons

- Want 1 and only 1 photon in a mode
- Can't just attenuate another quantum state, e.g. coherent state from laser







## Making photons

#### Single emitters



Want:

- Deterministic
- Pure
- Short
- Indistinguishable photons



#### **Spontaneous Parametric Down Conversion (basic)**

$$\vec{k}_p = \vec{k}_s + \vec{k}_i \qquad \qquad f_p = f_s + f_i$$



#### **Typical SPDC source**



#### High heralding efficiency source





-43

-29

29

43

Bennink, PRA 81, 053805 (2010)

#### Entangled source (one design)



Output state =  $|HV\rangle - |VH\rangle \equiv |01\rangle - |10\rangle$ 



### Quantum dot sources







## Somaschi et al., Nature Photonics 10, 340 (2016)

## Sources - important ingredients

- Distinguishability of two photons from the same source (M)
- Distinguishability of two photons from different sources (M)
- Efficiency (B)
  - Generation efficiency, Heralding efficiency, Coupling efficiency
- $g^{(2)}(0)$  correlation function (M)
  - (roughly, what is the probability of getting two photons when one expected)
- Speed/rate
- (B, M: see next slide)



#### Sources

What is needed is to MUX/DEMUX sources

Somaschi et al., Nat. Phot. 10, 340 (2016)





Lenzini et al., Laser & Photonics Reviews 11, 1600297 (2017)



#### Sources

What is needed is to MUX/DEMUX sources

Somaschi et al., Nat. Phot. 10, 340 (2016)



Time-multiplexed source



#### Experimental setup (periodic time-multiplexed HSPS)



Kaneda and Kwiat, arXiv:1803.04803





#### Heralded *entangled* photons (one way)



#### Measuring photons

- Need to detect a very small energy: ~ 10<sup>-19</sup> J for visible/near IR photons
- Some options:
  - Avalanche photodiodes
  - Superconductors








## **Photon detection**

- Desired photon detector
  - High efficiency
  - Fast
  - Photon number resolving
- Limitations at <u>Telecom</u> (~ 1500 nm)

Detector type	Detection efficiency (%)	Max count rate (CPS)	Timing jitter (ns)	Photon number resolution	System dark count rate (CPS)	Operation temperature (K)
InGaAs APD	10	10 <sup>8</sup>	0.05	No	10 <sup>4</sup>	240
W TES	99	< 10 <sup>4</sup>	100	Full	< 1	0.1
WSi SNSPD	95	$10^7 - 10^8$	0.2	No	< 10	1

Based on Rev. Sci. Instrum. 82, 071101 ('11) with some updates and interpretations\*

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#### Summary of quantum photonics overview

- Photons (and other optical quantum states) are robust and mobile
- Need to make, manipulate and measure photons
- Sources and detectors are approaching exceptional performance levels



#### Application: true quantum advantage in entangled-photon metrology

- Photonic entanglement-enhanced interferometry
- The shot noise limit hasn't been surpassed unconditionally, until now
- We unconditionally surpass the shot noise limit

S. Slussarenko et al., Nature Photonics <u>11</u>, 700 (2017)



### Photonic quantum metrology – **interferometry**

 "Photonic" means explicitly using photons, e.g. states of definite photon number and/or the use of photon counting (*not squeezing*)

. . .

- Promise of extracting the maximum phase information per photon
- Promise of extracting the better-than-classical phase information per unit of "destruction"

Wolfgramm et al., Nature Phot. 7, 28 (2013)

Genuine quantum-enhanced performance has been a goal for ~ 30 years

B. Yurke, Phys. Rev. Lett. 56, 1515 (1986)
B. C. Sanders, Phys. Rev. A 40, 2417 (1989)
A. N. Boto *et al.*, Phys. Rev. Lett. 85, 2733 (2000)



Resource (= *N*): Number of photons in the interferometer in a defined mode

#### NOON states with reduced interference visibility



"Period 1/N" fringes

<sup>1</sup> e.g. McCusker and Kwiat, *PRL* **103**, 163602 (2009)

#### NOON with low arm efficiency (modes, loss, dets ...)



"Period 1/N" fringes

<sup>1</sup> e.g. McCusker and Kwiat, *PRL* **103**, 163602 (2009)

# Phase sensitivity heuristic

 $\Delta \phi = \frac{\Delta A}{\left| d\langle A \rangle / d\phi \right|}$ Phase sensitivity: Fringe pattern:  $\frac{1}{2}(1 - V \cos N\phi) \times \eta^N$ Gradient:  $d\langle A \rangle / d\phi = \frac{1}{2}NV \sin N\phi \times \eta^N$ Classical (SNL):  $\Delta \phi_{\text{classical}} = \frac{1}{\sqrt{N}}$ 

Quantum enhancement if:

$$\eta^N V^2 N > 1$$

- $\eta$  Heralding (arm) efficiency
- V Interference visibility
- N Number of photons

Resch et al., PRL **98**, 223601 (2007) Okamoto et al, NJP **10** 073033 (2008)

More rigorous: A. Datta et al., PRA 83, 063836 (2011)



Back-of-the-envelope calculation

# $\eta \approx 0.82$ $V \approx 0.99$ N = 2

 $\eta^2 V^2 N \approx 1.32 > 1$ 

#### Two experiments

- We characterise the performance with two experiments
- 1. From the fringes, we can determine the Fisher information, and compare it with theory
- 2. We can use multiple, *k*, trials (detections) to infer a phase value at a given phase setting.

We can then use multiple, *s*, such phase samples to determine the uncertainty in the inferred phase.

We use *k* = 10,000 trials and *s* = 14,500 samples.

SNL:  $N^{tot} = N \times k \times s \times correction factor = 304,375,500$ 



(Not in this talk)

#### Experimental phase estimates



Slussarenko et al., N. Phot. 11, 700 (2017)

# ... on to part 2 !

#### Part 2: quantum steering

- **1.** What is quantum steering and how is it different to entanglement and Bell inequality violations?
- 2. Practical advantages of quantum steering
  - Loss tolerance
- 3. The asymmetry of quantum steering
  - The one-way steering effect

Griffith UNIVERSITY Oueensland, Australia

Wiseman, Jones, Doherty *PRL* **98**, 140402 (2007)

#### Entanglement sharing in a quantum network



- Entanglement is a resource for quantum communications and processing (amongst other things)
- Alice and Bob can communicate securely if they share entanglement
- E.g., if they can violate a loophole-free Bell inequality, they can perform deviceindependent QKD

e.g. Ekert, PRL 67, 661 (1991); Acin et al., PRL 98, 230501 (2007)

# Steering quantum information task

For Alice and Bob to demonstrate to Charlie that they can create entanglement between their labs.



a) With no trust, they must demonstrate Bell-nonlocality.b) With a trustworthy Bob, Alice must show EPR-steering.c) With both trusted, all that is needed is non-separability.

Wiseman, Jones, Doherty PRL 98, 140402 (2007)

# Three types of inequality

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Consider two pairs of binary measurements:  $A, A', B, B' \in \{-1, 1\}$ 

These can arise from measuring a Pauli operator (e.g.  $\hat{\sigma}_{X}$ ) on a qubit.

Bell-nonlocality (CHSH, 1969)

$$\left\langle AB\right\rangle + \left\langle A'B\right\rangle + \left\langle AB'\right\rangle - \left\langle A'B'\right\rangle \leq 2$$

EPR-steering (Cavalcanti, Jones, Wiseman, Reid, PRA 2009)

$$\left\langle A\hat{\sigma}_{X}^{B}\right\rangle + \left\langle A'\hat{\sigma}_{Z}^{B}\right\rangle \leq \sqrt{2}$$

Non-separability (entanglement witness, mid-90s)

$$\left\langle \hat{\sigma}_X^A \hat{\sigma}_X^B \right\rangle + \left\langle \hat{\sigma}_Z^A \hat{\sigma}_Z^B \right\rangle \leq 1$$



# Steering task – convincing a skeptical Bob

 Bob receives his quantum state, 2. announces his measurement setting, 3. measures and records his result as well as Alice's announced result, 4. calculates the steering parameter





# Steering is a superset of Bell inequality violation

#### (Result # 1)

D. J. Saunders, S. J. Jones, H. M. Wiseman and G. J. Pryde, *Nature Physics* **6**, 845 (2010)

#### Steering noise tolerance

Werner state

$$W_{\mu} = \mu \left| \Psi^{-} \right\rangle \left\langle \Psi^{-} \right| + (1 - \mu) \mathbf{I}/4 \qquad \mu \in [0, 1]$$

n = # of different measurement settings used by Alice & Bob.

- for n = 2, Bell-nonlocality exists if  $\mu > 0.707$  [CHSH'69]
- for n = 465, Bell-nonlocality exists *if*  $\mu > 0$ . 7056 [Vertesi'08]
- for  $n = \infty$ , Bell-nonlocality exists *only if*  $\mu > 0.6595$  [Acin+'06]

How about for EPR-steering?

Traditionally (i.e. following EPR) one considers only n = 2.

- for n = 2, EPR-steering exists if  $\mu > 0.707$  [Cavalcanti+'09]
- for  $n = \infty$ , EPR-steering exists *if and only if*  $\mu > 0.5$  [Wiseman+'07]



### Quantum steering of Bell-local states



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## Steering tolerant to loss

#### (Results # 2 & #3)

A. J. Bennet, D. A. Evans, D. J. Saunders, C. Branciard, E. G. Cavalcanti, H. M. Wiseman and G. J. Pryde, *Physical Review X* **2**, 031003 (2012)

M. M. Weston, S. Slussarenko, H. M. Chrzanowski, S. Wollmann, L. K. Shalm, V. B. Verma, M. S. Allman, S. W. Nam, G. J. Pryde, *Science Advances* **4**, e1701230 (2018)

### Verification of remote shared entanglement

To guarantee security offered by quantum mechanics a verification protocol must be performed loophole-free



**a.k.a. fair sampling assumption:** detected particles represent a fair sample of the entire ensemble

= Violation of Bell inequality with no loopholes

- 3 main loopholes closed simultaneously [1]:
  - ✓ Locality loophole
  - ✓ Freedom of choice loophole
  - ✓ Detection loophole [2]
- Demonstrated by recent experiments:
  - L. Shalm, et. al., PRL **115**, 250402 (2015)
  - M. Giustina, et. al., PRL **115**, 250401 (2015)
  - B. Hensen, et. al., Nature 526, 682 (2015)



[1] J.A. Larsson, J. Phys. A, 47, 424003 (2014); [2] P. Pearle, Phys. Rev. D, 2, 1418 (1970)

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#### Completely photonic loophole-free Bell tests

#### A strong loophole-free test of local realism

Lynden K. Shalm,<sup>1</sup> Evan Meyer-Scott,<sup>2</sup> Bradley G. Christensen,<sup>3</sup> Peter Bierhorst,<sup>1</sup> Michael A. Wayne,<sup>3,4</sup> Martin J. Stevens,<sup>1</sup> Thomas Gerrits,<sup>1</sup> Scott Glancy,<sup>1</sup> Deny R. Hamel,<sup>5</sup> Michael S. Allman,<sup>1</sup> Kevin J. Coakley,<sup>1</sup> Shellee D. Dyer,<sup>1</sup> Carson Hodge,<sup>1</sup> Adriana E. Lita,<sup>1</sup> Varun B. Verma,<sup>1</sup> Camilla Lambrocco,<sup>1</sup> Edward Tortorici,<sup>1</sup> Alan L. Migdall,<sup>4,6</sup> Yanbao Zhang,<sup>2</sup> Daniel R. Kumor,<sup>3</sup> William H. Farr,<sup>7</sup> Francesco Marsili,<sup>7</sup> Matthew D. Shaw,<sup>7</sup> Jeffrey A. Stern,<sup>7</sup> Carlos Abellán,<sup>8</sup> Waldimar Amaya,<sup>8</sup> Valerio Pruneri,<sup>8,9</sup> Thomas Jennewein,<sup>2,10</sup> Morgan W. Mitchell,<sup>8,9</sup> Paul G. Kwiat,<sup>3</sup> Joshua C. Bienfang,<sup>4,6</sup> Richard P. Mirin,<sup>1</sup> Emanuel Knill,<sup>1</sup> and Sae Woo Nam<sup>1</sup> Phys. Rev. Lett. 115, 250402 (2015)

#### A significant-loophole-free test of Bell's theorem with entangled photons

Marissa Giustina,<sup>1, 2</sup>,<sup>\*</sup> Marijn A. M. Versteegh,<sup>1, 2</sup> Sören Wengerowsky,<sup>1, 2</sup> Johannes Handsteiner,<sup>1, 2</sup> Armin Hochrainer,<sup>1, 2</sup> Kevin Phelan,<sup>1</sup> Fabian Steinlechner,<sup>1</sup> Johannes Kofler,<sup>3</sup> Jan-Åke Larsson,<sup>4</sup> Carlos Abellán,<sup>5</sup> Waldimar Amaya,<sup>5</sup> Valerio Pruneri,<sup>5, 6</sup> Morgan W. Mitchell,<sup>5, 6</sup> Jörn Beyer,<sup>7</sup> Thomas Gerrits,<sup>8</sup> Adriana E. Lita,<sup>8</sup> Lynden K. Shalm,<sup>8</sup> Sae Woo Nam,<sup>8</sup> Thomas Scheidl,<sup>1, 2</sup> Rupert Ursin,<sup>1</sup> Bernhard Wittmann,<sup>1, 2</sup> and Anton Zeilinger<sup>1, 2</sup>,<sup>†</sup>

#### Phys. Rev. Lett. 115, 250401 (2015)

#### **Practical limitations**

Closing detection loophole requires channel transmission to be higher than a certain (high) threshold [1]



> Losses through the fiber open up the detection loophole

# Want to achieve: Entanglement verification over high-loss channel with detection loophole closed



[1] P. H. Eberhard, Phys. Rev. A, 47, R747 (1993)

#### Alternative test

Quantum

steering

Untrusted  $|\psi\rangle$   $|\psi\rangle$   $|\psi\rangle$   $|\psi\rangle$ Trusted

- Additional assumption required:
  - Bob trusts quantum mechanics to describe his own measurements
- Uses entanglement to steer the state of distant quantum system by local measurements
- More robust to loss



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Detection loophole in nonlocality tests?



Detection loophole in nonlocality tests?



<sup>°</sup>Fair sampling cheating strategy

Alice can use the detection loophole to cheat



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# <sup>19</sup> Fair sampling cheating strategy

• Alice can use the detection loophole to cheat



- Her heralding efficiency (fraction of times she announces a result) is only 1/n...
- ... but these announcements lead to steering parameter of S<sub>n</sub> = 1, the maximum!

# <sup>20</sup> Loss-Dependent EPR-Steering Bound



## Entangled source (one design)



Output state =  $|HV\rangle - |VH\rangle \equiv |01\rangle - |10\rangle$ 

## Measured steering parameters



Related experiments:

Smith *et al.*, Nature Comms 3, 625 (2012) Wittmann *et al.*, New J. Phys 14, 053030 (2012)

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#### Loss-tolerant steering bounds

Secure steering with arbitrarily high loss  $\rightarrow$  max entangled state ( $S_n = 1$ )  $\rightarrow n = \infty$ Imperfect states & finite n?





Better than Bell test, but still not ready for real life applications



[1] A. Bennet, et.al., PRX 2, 031003 (2012)
## The "event-ready" approach

- Record an additional "heralding" signal to indicate successful sharing
- > Failed distribution events are excluded upfront from tests
- Allows Alice to maintain her effective heralding efficiency with loss



Event-ready: M. Zukowski, et. al., PRL 71, 4287 (1993); Entanglement swapping: J. Pan, et.al., PRL 80, 3891 (1998)

### Heralded quantum steering



# **Experimental requirements**

High visibility Hong-Ou-Mandel interference
 High entangled state fidelity
 High heralding efficiency (on Alice's side)

### Made possible by:

 Group velocity matched source: M. Weston, et. al., Opt. Exp. 24, 10869 (2016)
 Superconducting nanowire photon dets: F. Marsili, et al., Nat. Photonics 7, 210 (2013)





High-efficiency SNSPDs:



Sae Woo Nam

(+ team)



- > Heralding efficiencies up to  $(82 \pm 2)\%$
- HOM interference visibilities up to 100%
- > Singlet state fidelities up to  $(99.0 \pm 0.2)\%$





### **Experimental demonstration**

-PA BSM **S1** Alice Bob **S**2 PBS **Dual HWP Dichroic Mirror** FPC HWP 50:50 BS Dual PBS Coupler QWP PP-KTP Loss (ND filter) SNSPD GT **BP** filter Mirrors Lens

Channel loss 7.7dB, 11.3dB, 14.8dB

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# The asymmetry of quantum steering

(Result # 4)

S. Wollmann, N. Walk, A. J. Bennet, H. M. Wiseman and G. J. Pryde, *Physical Review Letters* **116**, 160403 (2016)

# <sup>30</sup> Steering quantum information task

For Alice and Bob to demonstrate to Charlie that they can create entanglement between their labs.



a) With no trust, they must demonstrate Bell-nonlocality.
b) With a trustworthy Bob, Alice must show EPR-steering. Wiseman, Jones, Doherty PRL 98, 140402 (2007)

# Can steering be one-way?



**Steering demonstrated** 



# Can steering be one-way?



# Requires an asymmetric state

• Easiest way is to add *loss* to one side.



# Homodyne detection of Gaussian states



V. Handchen et al., Nat. Photon 6, 598 (2012)

Successful Gaussian one-way steering with two-mode squeezed states

#### But:

Gaussian measurements are insufficient to capture the full nonlocality of Gaussian states

Explicit examples of one-way steerable Gaussian states which are two-way steerable for appropriate measurements

S. Wollmann et al., Phys. Rev. Lett. 116, 160403 (2016)

#### Do states exist which are one-way steerable for arbitrary measurements?

## Do any genuinely one-way steerable states exist? YES!

PHYSICAL REVIEW A 92, 032107 (2015)

Inequivalence of entanglement, steering, and Bell nonlocality for general measurements

Marco Túlio Quintino,<sup>1</sup> Tamás Vértesi,<sup>1,2</sup> Daniel Cavalcanti,<sup>3</sup> Remigiusz Augusiak,<sup>3</sup> Maciej Demianowicz,<sup>3</sup> Antonio Acín,<sup>3,4</sup> and Nicolas Brunner<sup>1</sup> Theoretical proof for infinite-setting POVMs

PHYSICAL REVIEW A 90, 012114 (2014)

Optimal measurements for tests of Einstein-Podolsky-Rosen steering with no detection loophole using two-qubit Werner states

D. A. Evans and H. M. Wiseman

One-way steerable state for projective measurements

J. Bowles et al., Rev. Lett. 112, 200402 (2014), P. Skrzypczyk et al., PRL 112, 180404 (2014), R. F. Werner, PRA 40, 4277 (1989).

### What is a genuine one-way steerable state?



Using the theorem of Quintino et al. to extend to arbitrary measurements

$$\rho_{AB} = \left(\frac{1-p}{3}\right)\rho_W + \left(\frac{p+2}{3}\right)\left(\frac{l_A}{2} \otimes |v\rangle_B \langle v|_B\right)$$

$$\rho_W = \mu |\psi_s\rangle \langle \psi_s| + \frac{1-\mu}{4} I_4 \qquad \text{with } \mu = [0,1]$$

What this means: Just add a lot more loss

one-way steerable for arbitrary measurements if

$$p > \frac{2\mu + 1}{3}$$



S. Wollmann et al., Phys. Rev. Lett. 116, 160403 (2016)

## Experimental generation of steerable state



A. Fedrizzi et al., Opt. Exp. 15, 15377 (2007)

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# <sup>38</sup>Two-way steering





For Alice  $S_{16} = 0.966 \pm 0.005$  at  $\eta_A = (16.98 \pm 0.02)\%$ For Bob  $S_{16} = 0.954 \pm 0.005$  at  $\eta_B = (16.94 \pm 0.02)\%$ 

# <sup>39</sup>One way steering



For Alice  $S_{16} = 0.960 \pm 0.005$  at  $\eta_A = (17.17 \pm 0.04)\%$ For Bob  $S_{16} = 0.951 \pm 0.006$  **no violation** for n measurement directions on Bloch sphere, here: n=16

#### 40 One-way steering for arbitrary measurements



for n measurement directions on Bloch sphere, here: n=16

0.20

Wollmann et al., *Physical Review Letters* **116**, 160403 (2016)

# Not so fast!



- This result assumes that the state is exactly a Werner state.
- Our Werner state fidelity is 99% 99.5%
- Close enough, right?
- WRONG!

### Solution:

- (1) Derive a more general bound; and/or (2) Make a better state
- We did both, then demonstrated conclusive one-way steering

Tischler et al., Phys. Rev. Lett. 121, 100401 (2018)

### 42 Conclusions

- Quantum steering is an asymmetric form of nonlocality that is different from Bell inequality violations and entanglement witnessing
- It is more robust to noise and loss than Bell inequality violation
- It can be configured into a heralded protocol in order to verify nonlocality over a channel with many dB of loss, with the detection loophole closed
- It is a fundamentally asymmetric protocol, and can be shown to be unidirectional for arbitrary choice of measurements
- Steering requires trust in one party, and in QM. There are a variety of scenarios in which this trust seems to be justified, and so steering may be useful for rigorously verifying entanglement in those cases.

