

Lecture 2 : using single atoms as controlled single-photon sources

1. Basics of non-classical-light and single photons
2. Generating indistinguishable single photons from single atoms
3. From single atoms to single qubits

Part 1

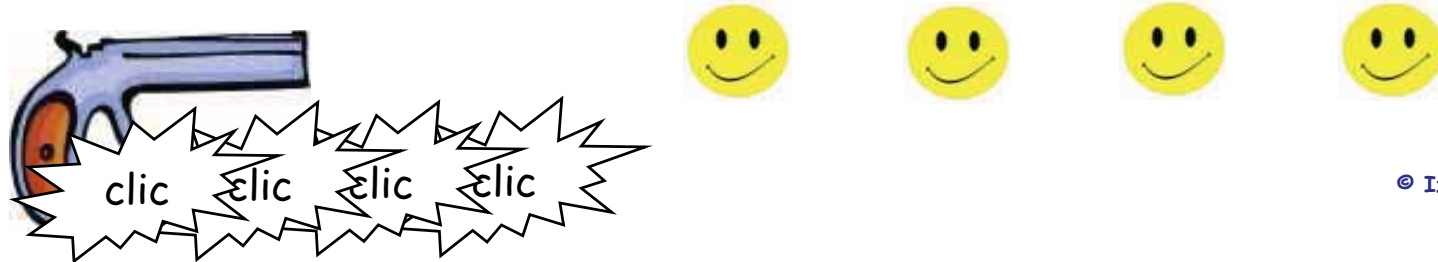
From heralded single photons (1986)

to single-mode single photons

using a single trapped atom (2005)

Darquié et al, Science 309, 454 (2005)

« Photon gun »



© Izo Abram

Deterministic => photons when we want
Efficient => photons each time we ask
Suitable => photons in the format we require

Different applications require different “qualities” of photons:

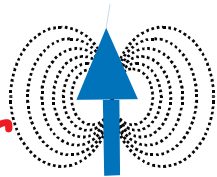
Quantum cryptography : the goal is to eliminate “PNS” attacks
must be simple and efficient

Quantum Gates : “KLM” Linear Quantum Computing
requires indistinguishable photons !

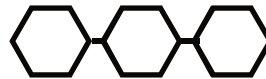
Single Photon Sources

Emitting single photons
on demand :
Quantum cryptography
Quantum Gates

Pulsed
Single Emitter



Single atom or ion in a cavity



Molecule, nanocrystallites

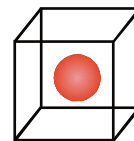
☹ Photobleaching, blinking



Quantum Dot (+ microcavities)

☺ Narrow Spectrum

☹ T = 4K



Color Centers (NV centers)

☺ Stable at Room
Temperature

☺ Easy to Produce

☺ Subpoissonian Statistics:

$$p(2) = c_N(0) \frac{p(1)^2}{2}$$

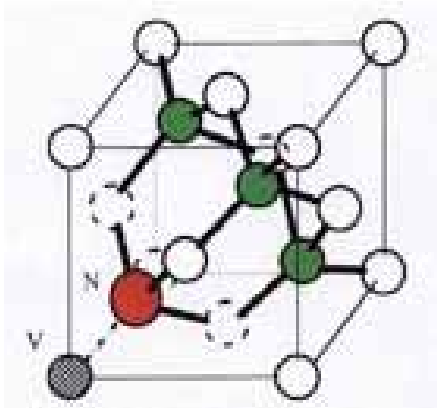
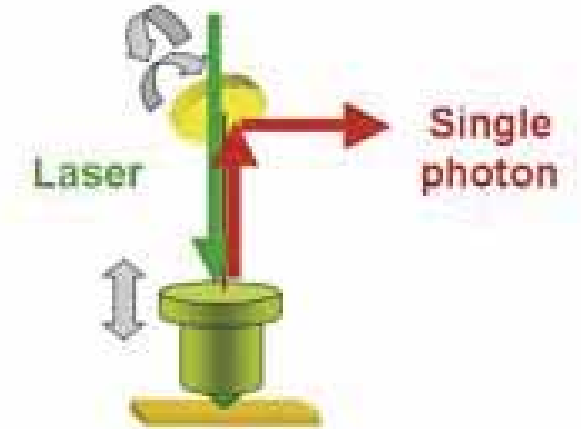
☺ $c_N(0) \ll 1$

Single photon sources : a simple example

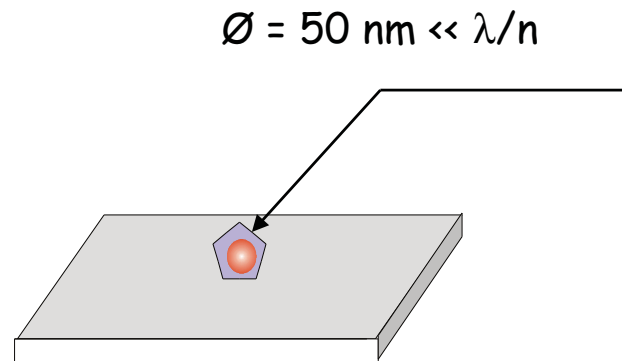
NV centers in diamond nanocrystals

"Single photon quantum cryptography"

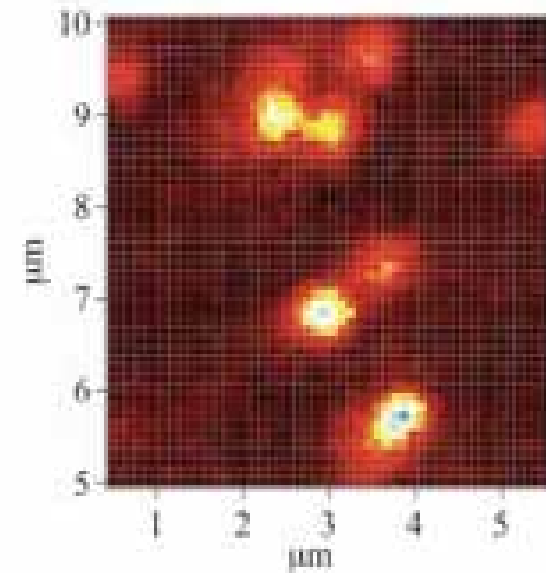
A. Beveratos, R. Brouri, T. Gacoin,
A. Villing, J.P. Poizat and P. Grangier
Phys. Rev. Lett. 89 (18), 187901 (2002)



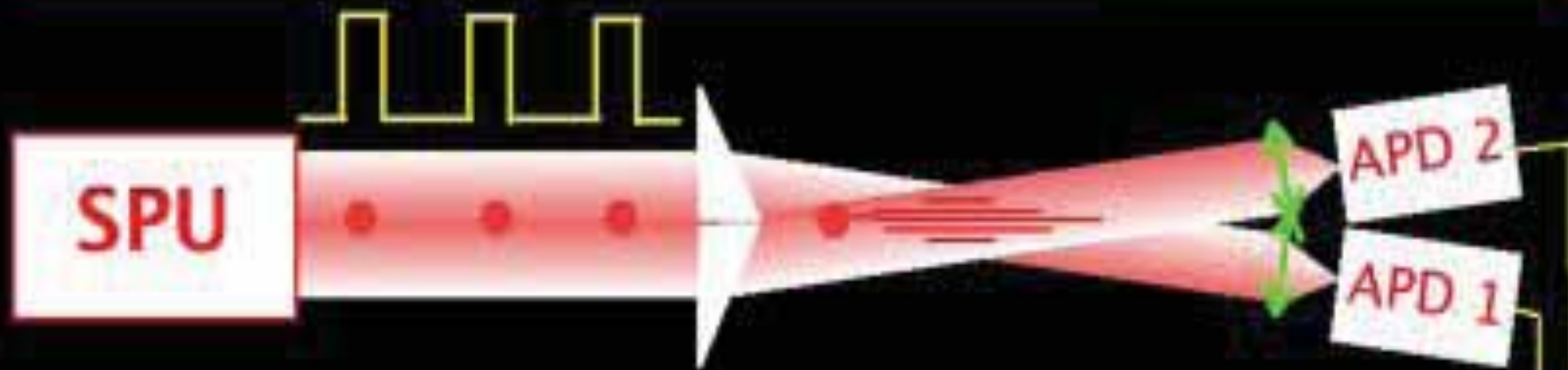
NV =
Nitrogen-
Vacancy



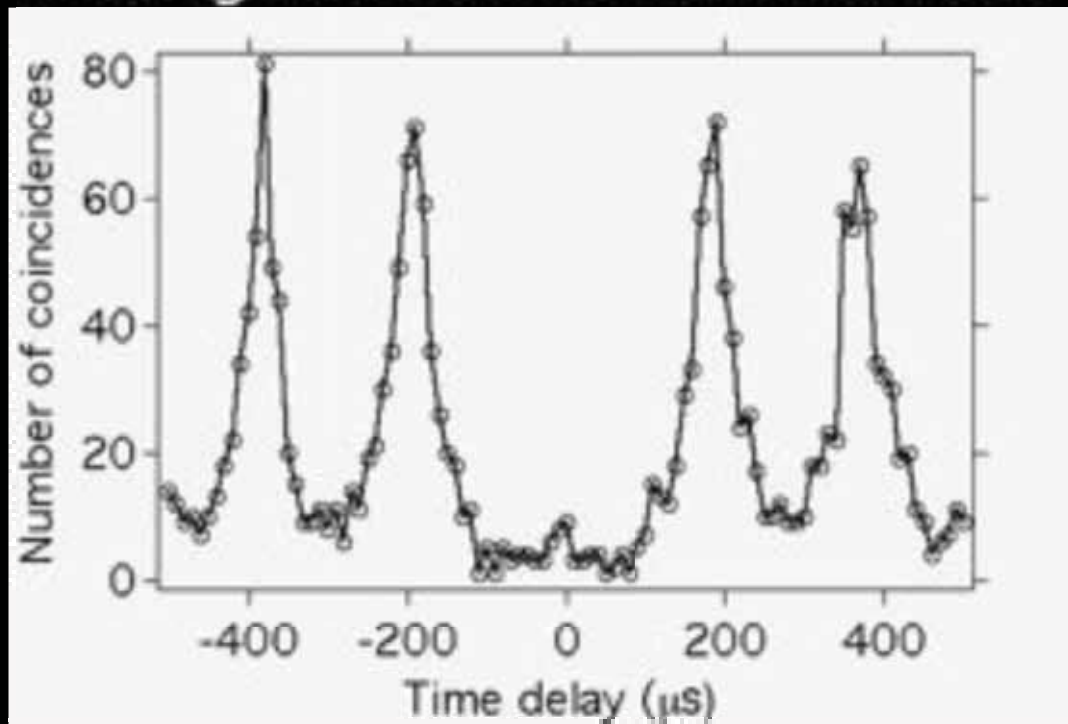
diamond
nanocrystal



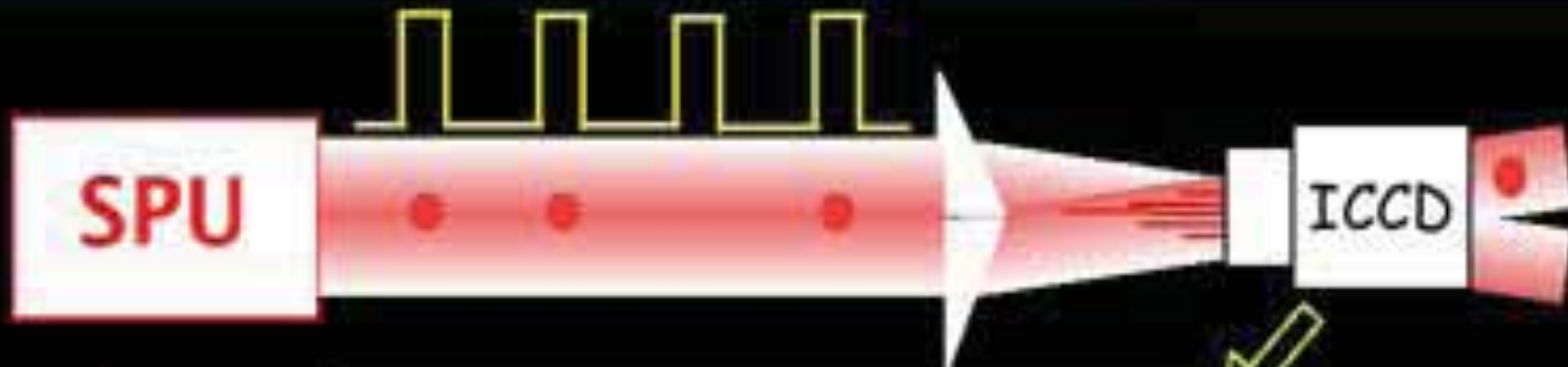
Which way is followed by the photon ?



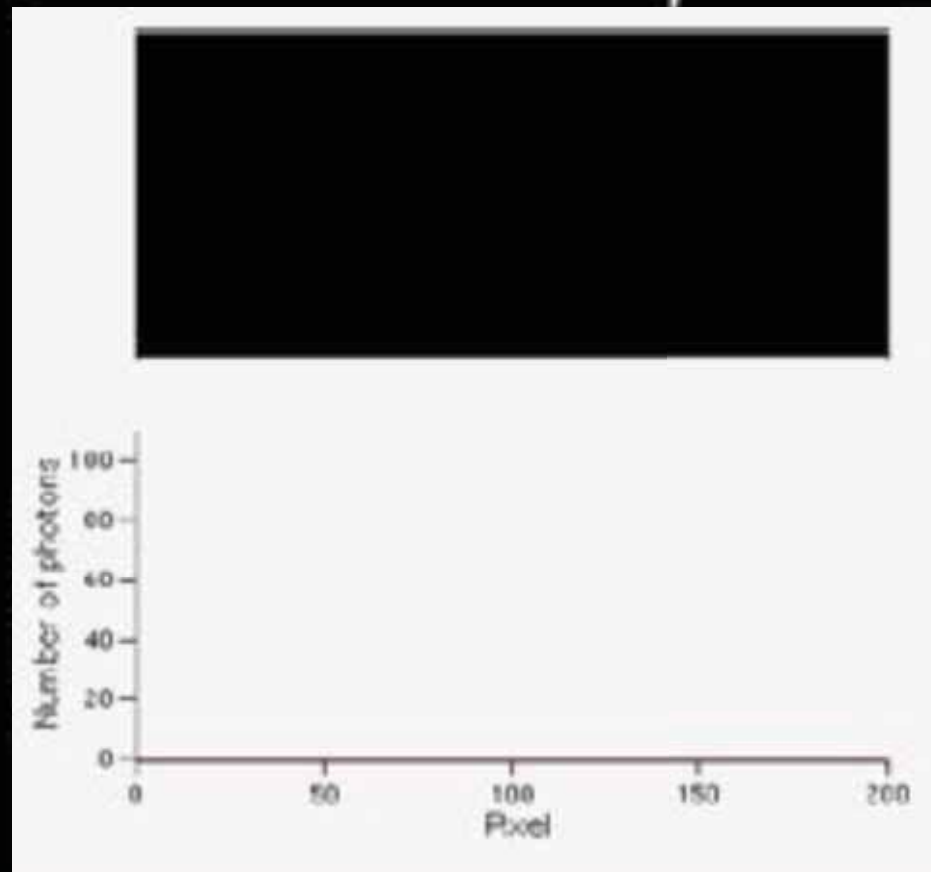
Histogramme des coïncidences



Looking at single photon interferences



Single-photon source :
NV centers in diamond nanocrystals, pulsed excitation



Experiment realized at ENS Cachan :

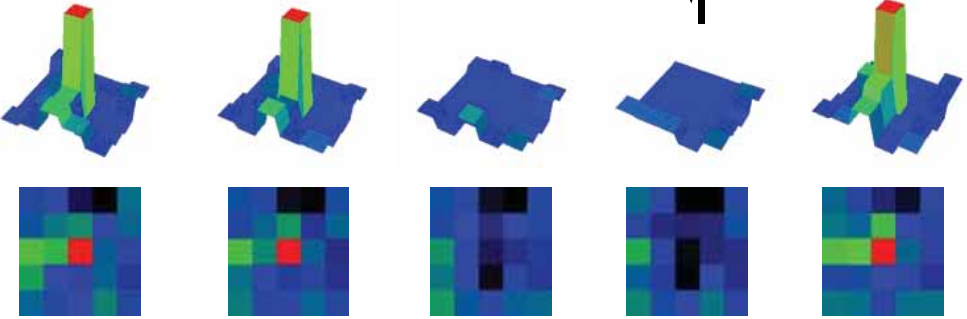
V. Jacques, E. Wu, T. Toury, F. Treussart, A. Aspect, P. Grangier and J.-F. Roch
Eur. Phys. J. D 35, 561-565 (2005)

Free download !

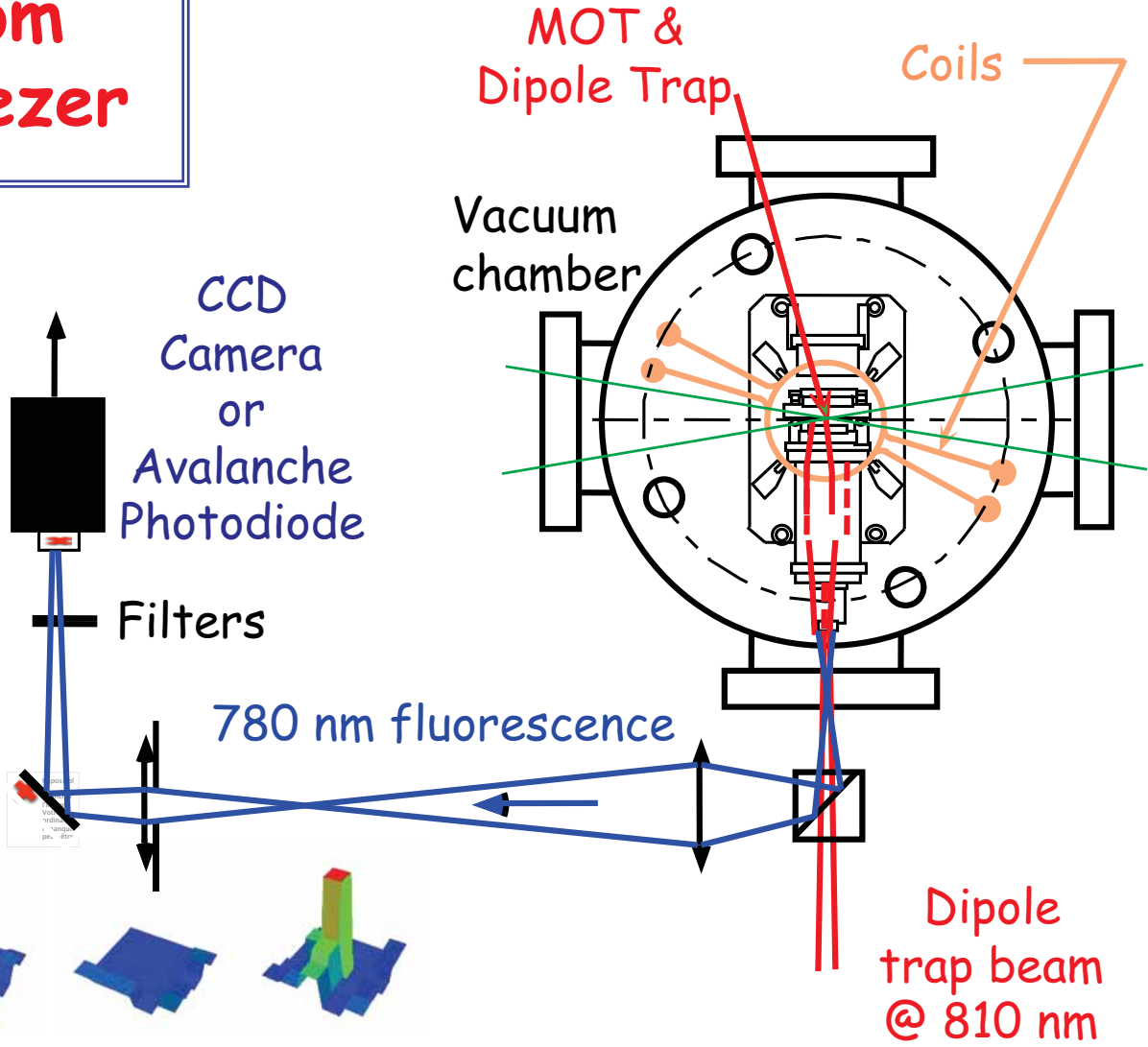
Single atom optical tweezer

Microscopic dipole trap :
 Spot size $< 1 \mu\text{m}$
 Power $< 10 \text{ mW}$
 Trapping time $> 1 \text{ s}$

Imaging : $1 \mu\text{m}/\text{pixel}$

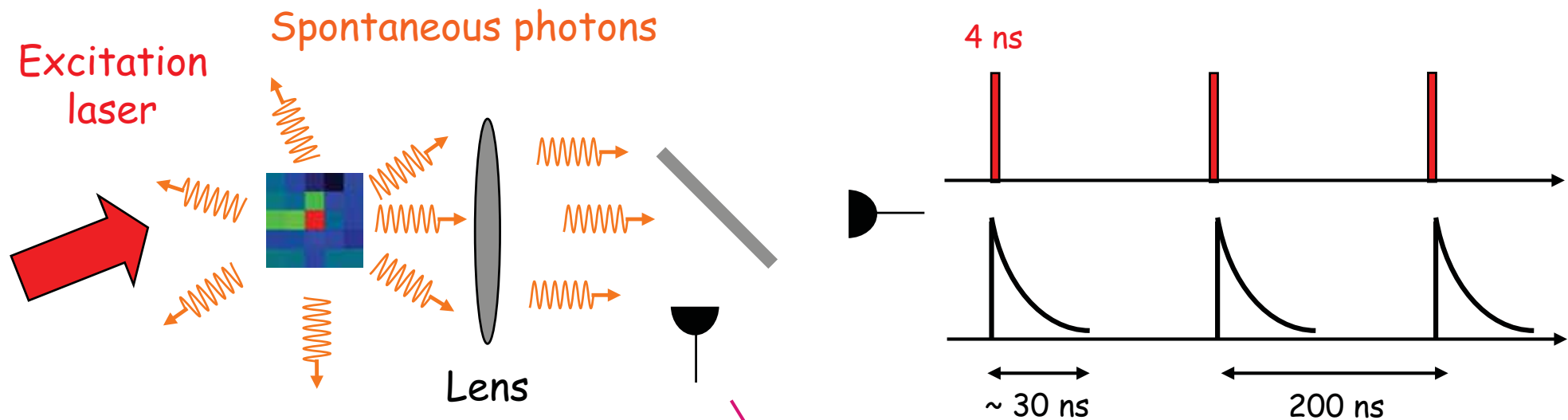


Individual atoms « jumping » in the trap
 « Collisional blockade » : only one atom !

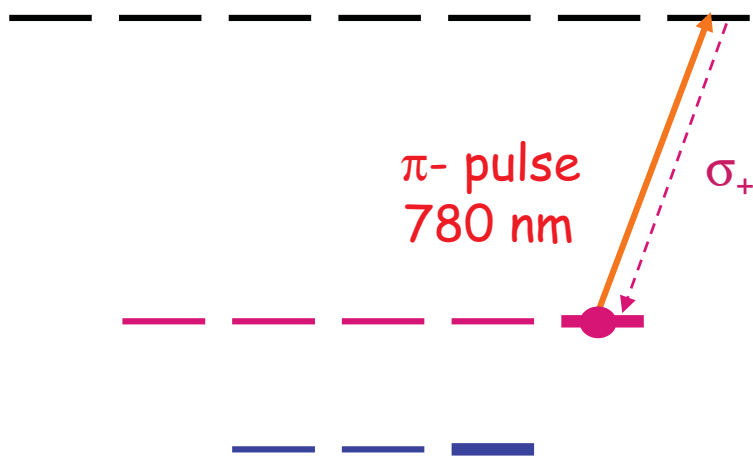


N. Schlosser et al,
 Nature 411, 1024 (2001)
 PRL 89, 023005 (2002)

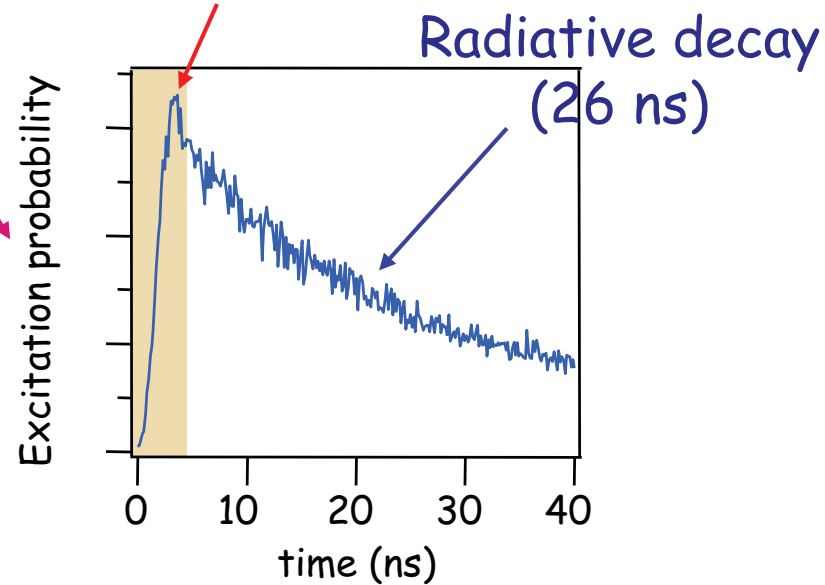
Triggered emission of single photons by an atom



« Coherent » excitation



100% transfer



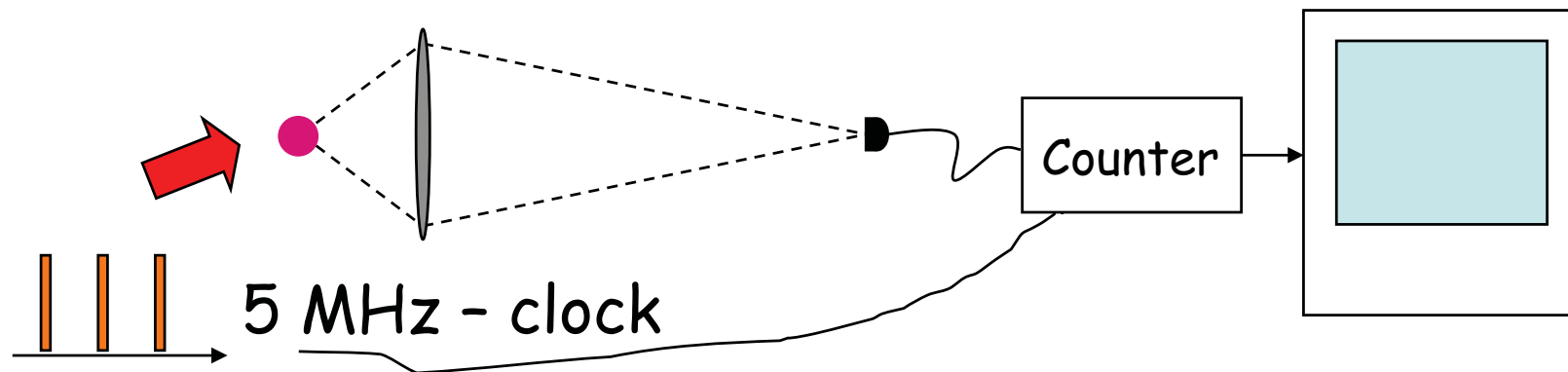
EXCITING THE ATOM

Excitation process based on π - pulse
 \Rightarrow test by observing Rabi oscillations on the 780 nm transition

$$2\text{-level system model : } P_e \propto \sin^2 \Omega T/2$$

Pulse duration (4 ns) \ll lifetime of the atomic transition (26 ns)

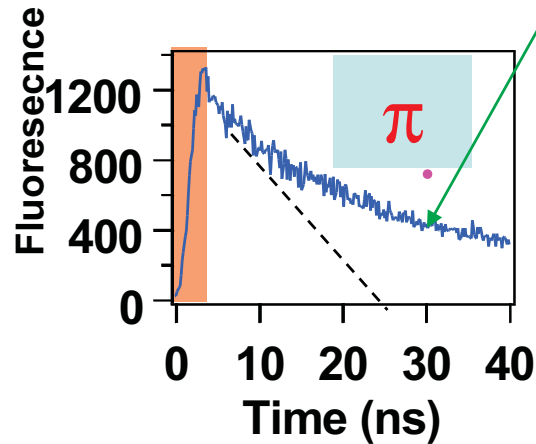
For a fixed pulse duration $T = 4$ ns, change the laser power $\propto \Omega^2$



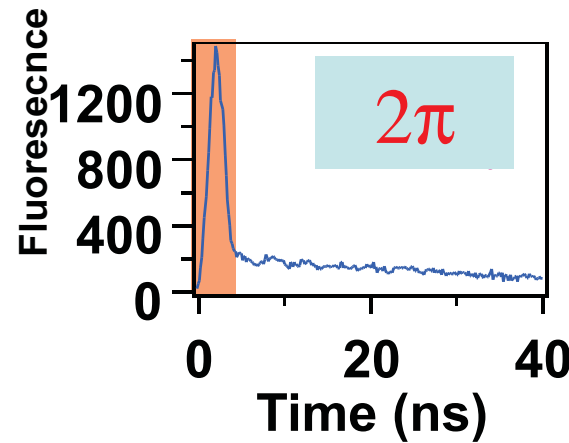
RABI OSCILLATIONS VS TIME

De-excitation (lifetime of the excited state)

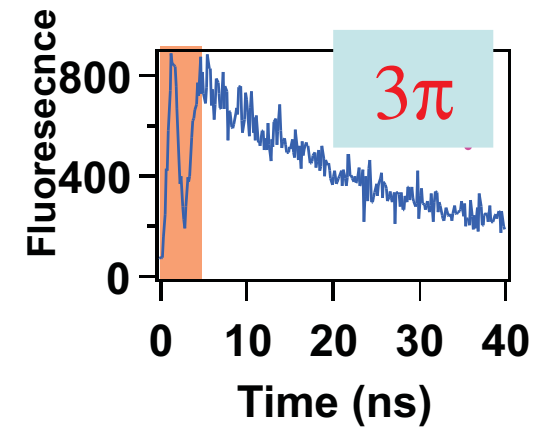
4 ns - pulse



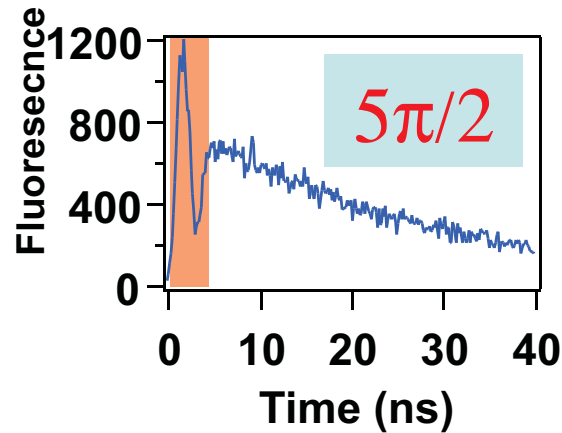
$\sim 20 \text{ W / cm}^2$



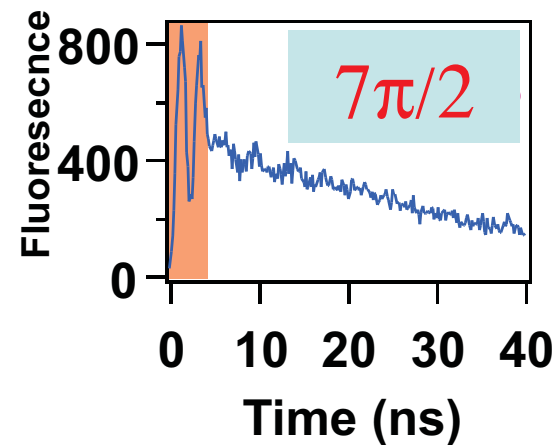
$\sim 80 \text{ W / cm}^2$



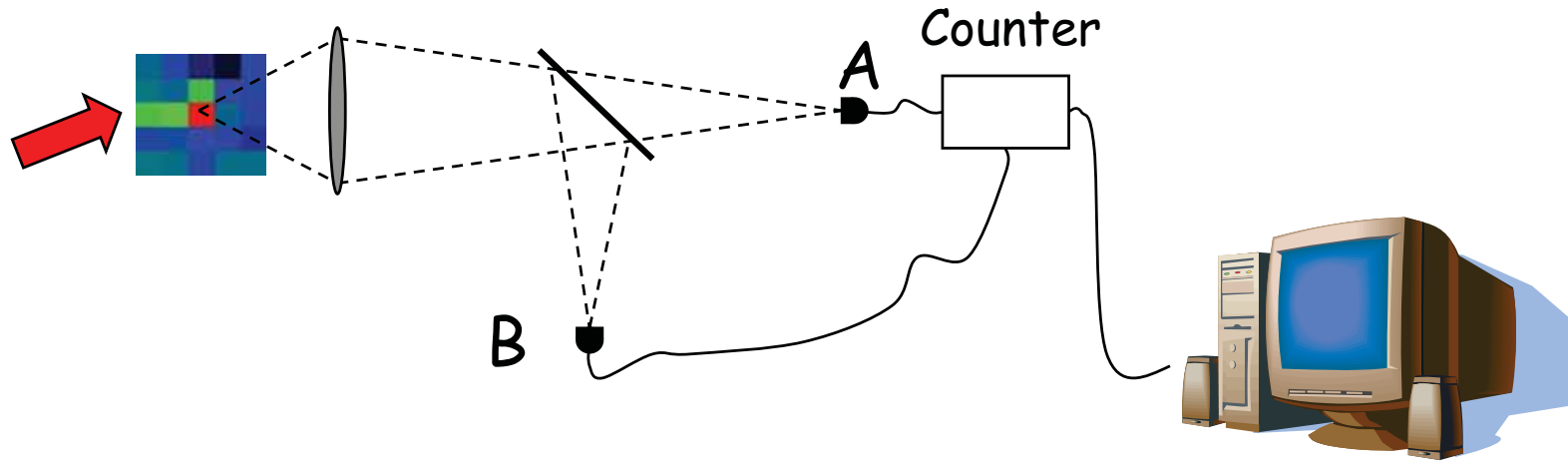
$\sim 180 \text{ W / cm}^2$



$\sim 125 \text{ W / cm}^2$



$\sim 250 \text{ W / cm}^2$



Start - stop configuration:

measure the number of coincidences for different delays τ

-> second-order intensity correlation function $g^{(2)}(\tau)$

= Probability to detect one photon at time t ,
and another one at time $t+\tau$

Some formulas...

Definition of the intensity correlation function $g^{(2)}(\tau)$:

$$g^{(2)}(t, t + \tau) = \frac{P(t, t + \tau)}{P(t)P(t + \tau)}$$

Classically P is proportionnal to the intensity :

$$I(t) = \langle \mathcal{E}^*(t)\mathcal{E}(t) \rangle$$

and thus :

$$g_{class}^{(2)}(\tau) = \frac{\langle \mathcal{E}^*(t)\mathcal{E}^*(t + \tau)\mathcal{E}(t + \tau)\mathcal{E}(t) \rangle}{\langle \mathcal{E}^*(t)\mathcal{E}(t) \rangle^2} = \frac{\langle I(t + \tau) I(t) \rangle}{\langle I(t) \rangle^2}$$

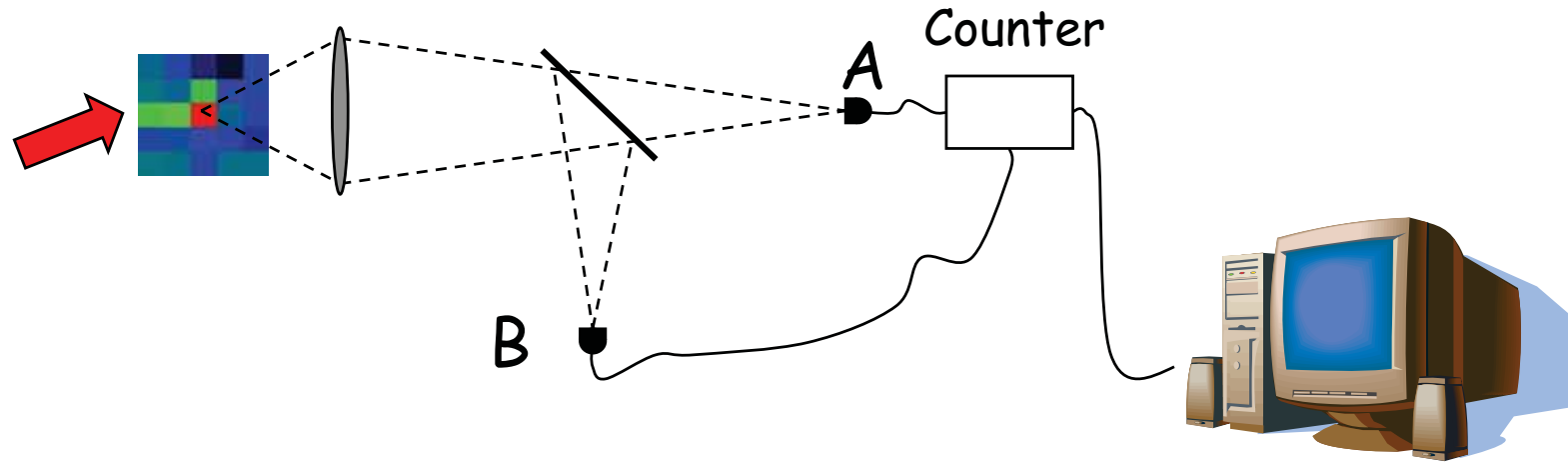
En utilisant les inégalités $\langle I^2(t) \rangle \geq \langle I(t) \rangle^2$ et $\langle I^2(t) \rangle \geq \langle I(t + \tau) I(t) \rangle$ (inégalités de Cauchy-Schwartz), on voit que :

$$g_{class}^{(2)}(0) \geq 1 \quad g_{class}^{(2)}(0) \geq g_{class}^{(2)}(\tau)$$

Quantum expression of $g^{(2)}(\tau)$:

$$g^{(2)}(\tau, \vec{r}) = \frac{\langle \hat{E}^{(-)}(t, \vec{r})\hat{E}^{(-)}(t + \tau, \vec{r})\hat{E}^{(+)}(t + \tau, \vec{r})\hat{E}^{(+)}(t, \vec{r}) \rangle}{\langle \hat{E}^{(-)}(t, \vec{r})\hat{E}^{(+)}(t, \vec{r}) \rangle^2}$$

For a single photon one can have $g^{(2)}(\tau) = 0$!



Start - stop configuration:
measure the number of coincidences for different delays τ

-> second-order intensity correlation function $g^{(2)}(\tau)$

Antibunching : $g^{(2)}(0) < g^{(2)}(\tau)$

Anticorrelation : $g^{(2)}(0) < 1$
(related to sub-poissonian photon statistics)



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ANTIBUNCHING : $g^{(2)}(0) < g^{(2)}(\tau)$



QIPC/SAP

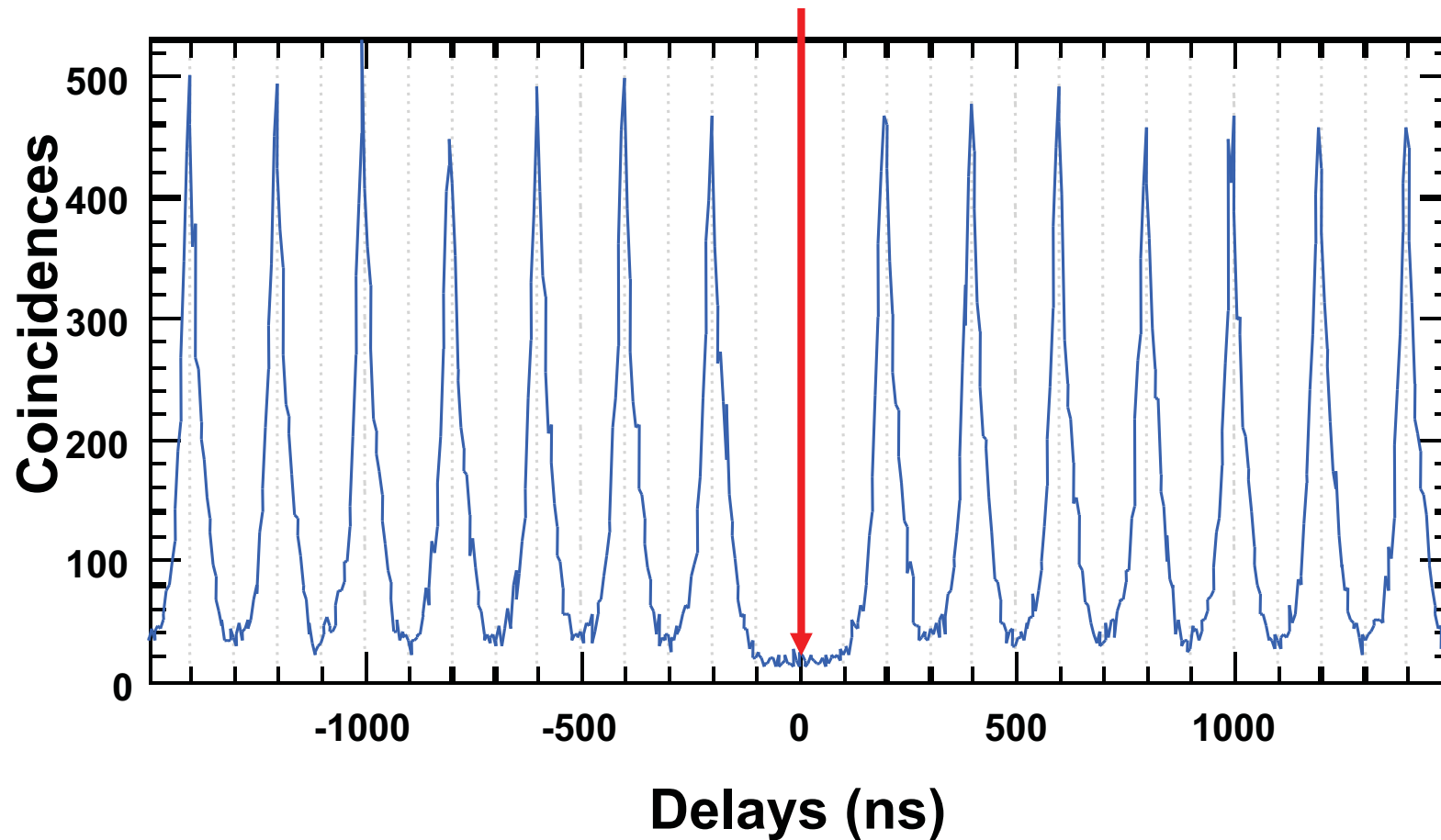
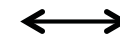
4 - hour acquisition (4×10^6 photons)

Resolution 1 ns, binning $\times 4$

No background correction

Time between 2 pulses

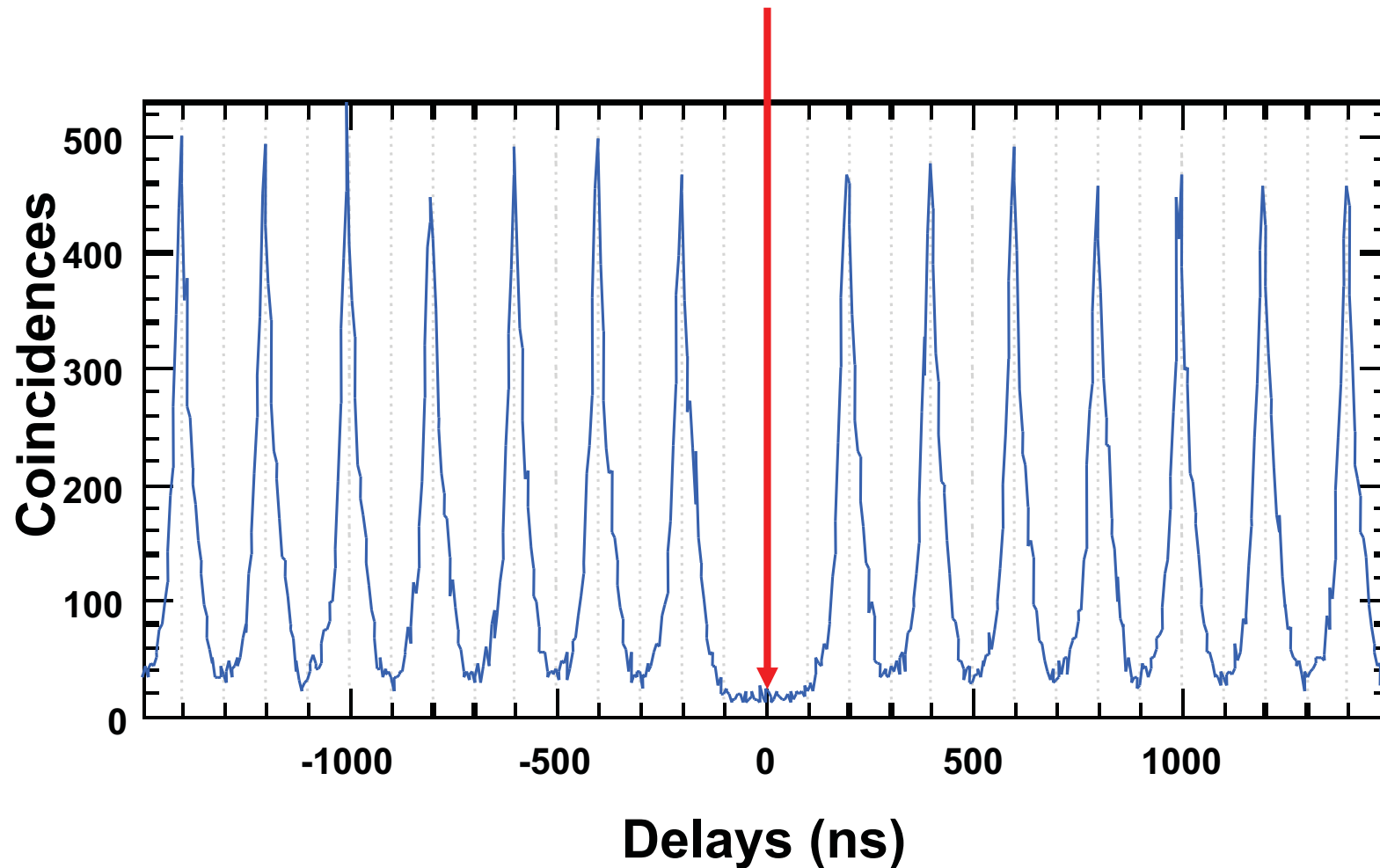
Antibunching



**ANTICORRELATION : $g^{(2)}(0) < 1$
(sub-poissonian photon statistics)**

$$C_N(0) = 2 p(2) / p(1)^2 = 0.034 = 1/30$$

\Rightarrow Probability to emit 2 photons during a pulse, $p(2) = 0.018$



Part 2

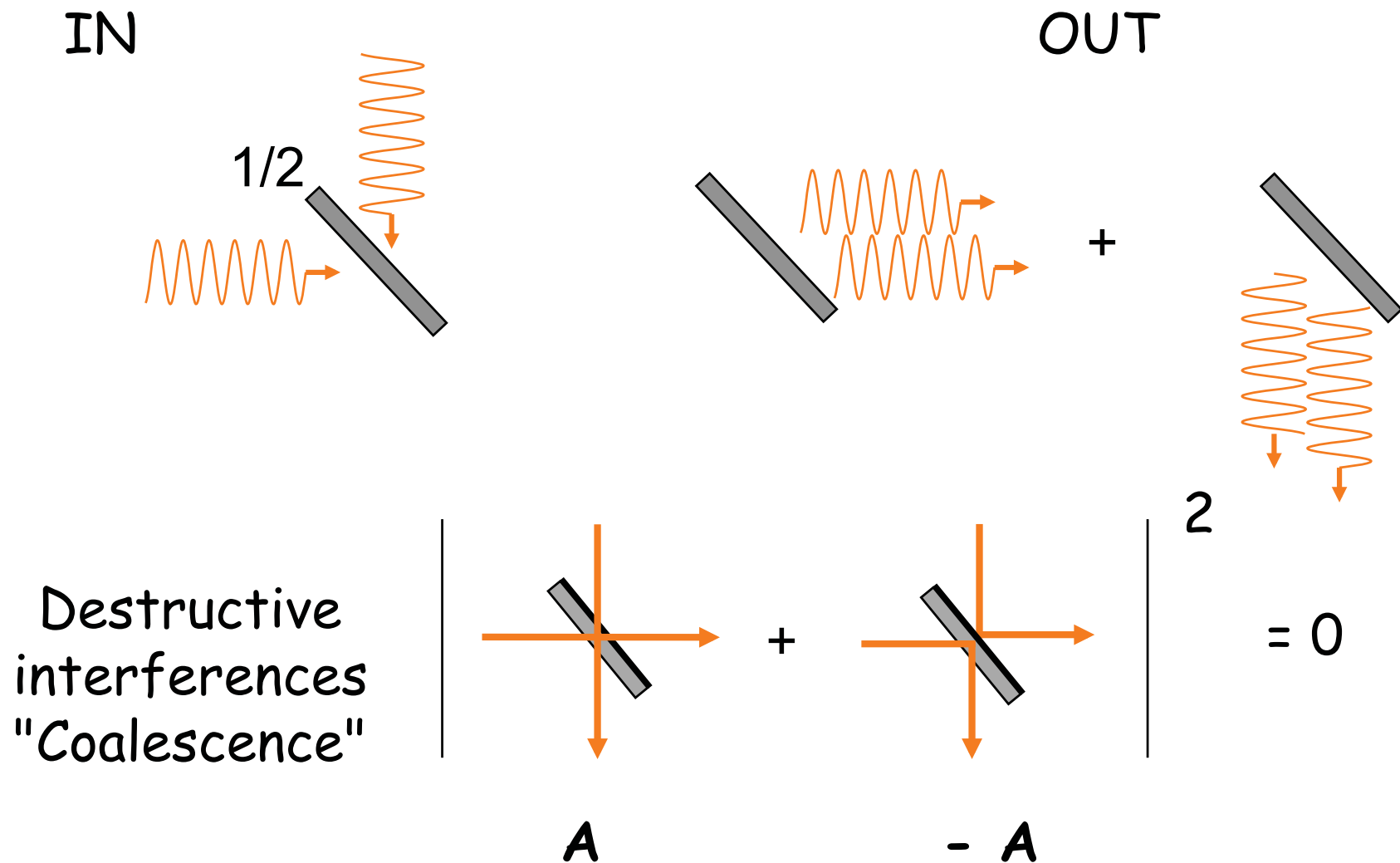
Two-photon coalescence

from two independantly trapped atoms

- * direct demonstration that the photons are single-mode
- * essential step towards scalability of the KLM scheme

Two-photon interferences (Hong-Ou-Mandel "HOM" effect)

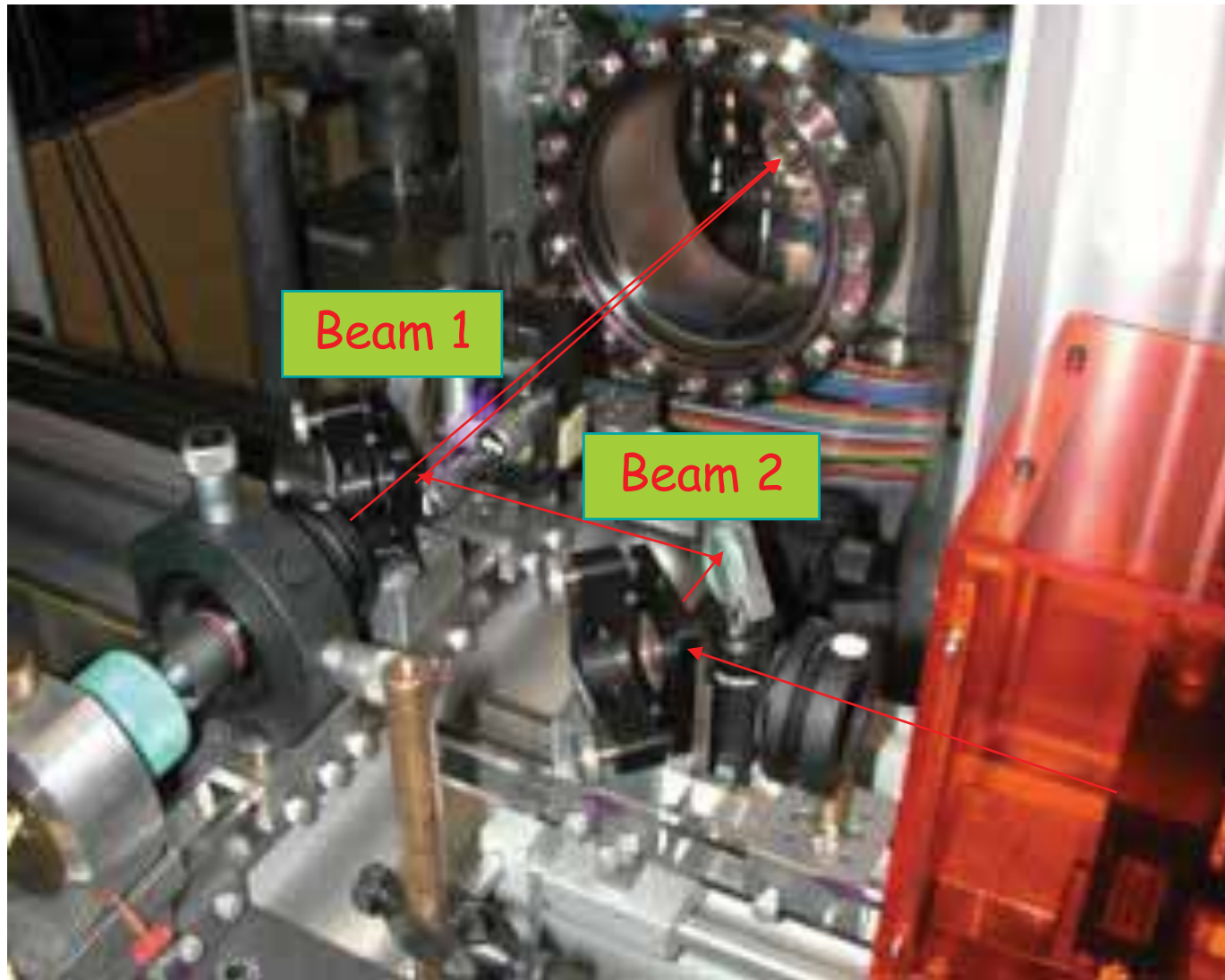
Rb atoms are all the same -> Indistinguishable photons !



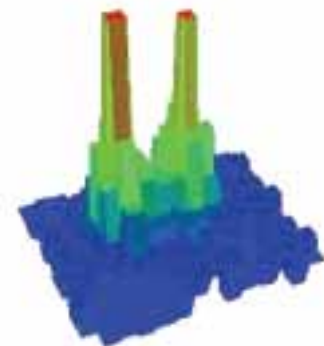
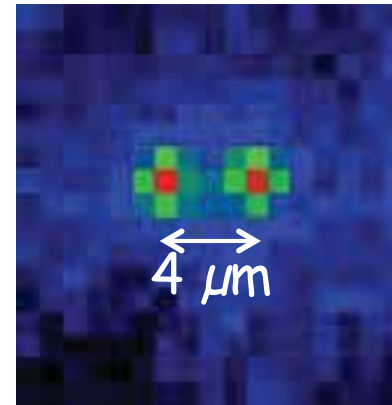
Two atoms at your fingertips

N. Schlosser et al, Nature 411, 1024 (2001)

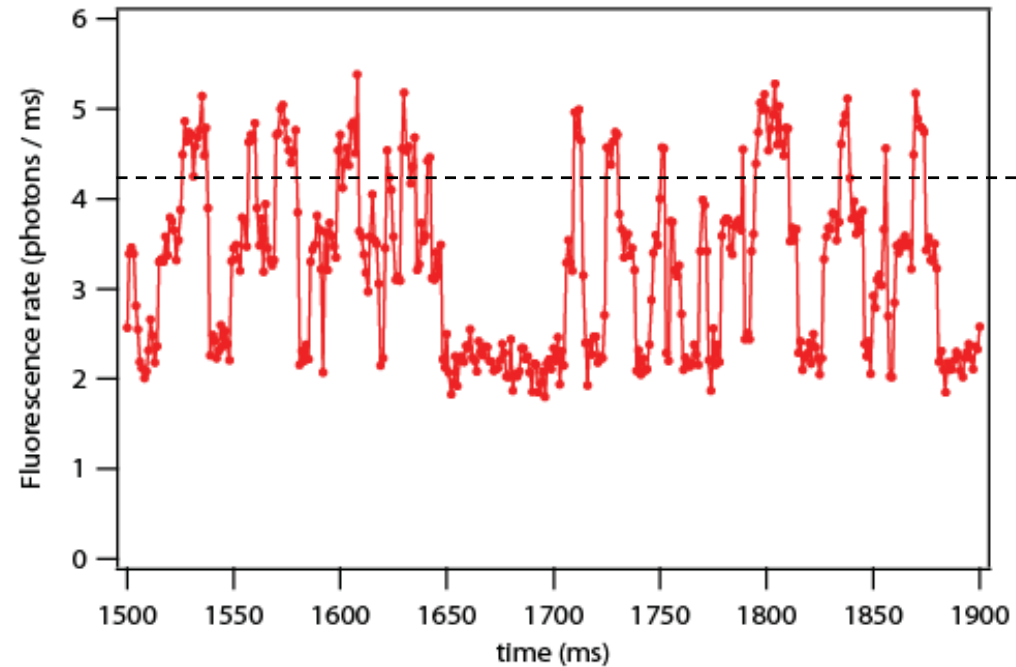
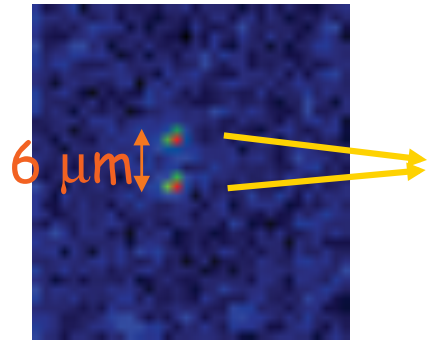
PRL 89, 023005 (2002)



Resolution of the
imaging system:
1 micron / pixel

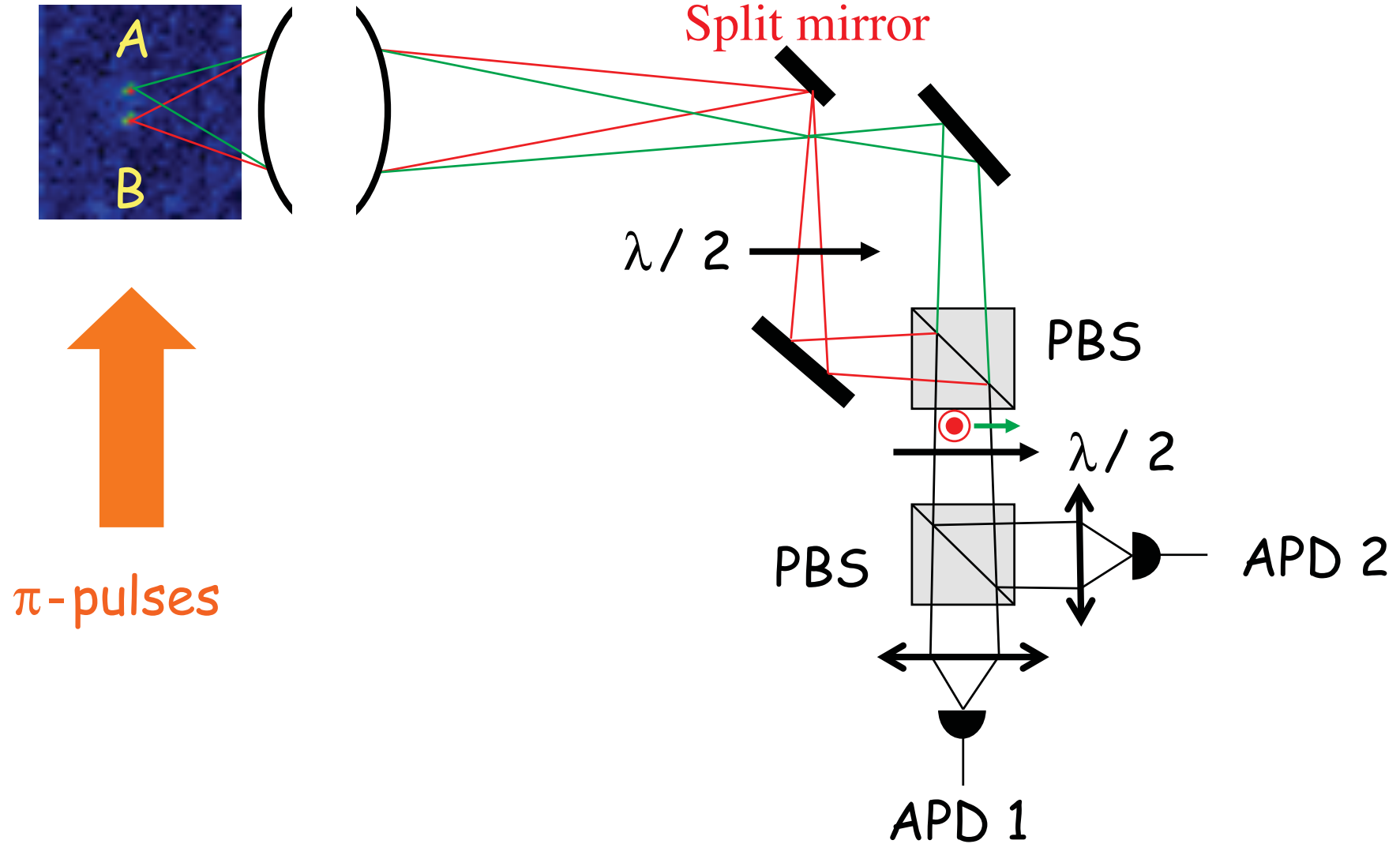


Repeatedly trapping 2 atoms



- Detect 2 atoms (signal above threshold)
- Launch 15 cycles containing 575 pulses (115 μs)
followed by 885 μs cooling
- Release the remaining atom(s)
- Catch 2 atoms again (~ 300 ms) and loop

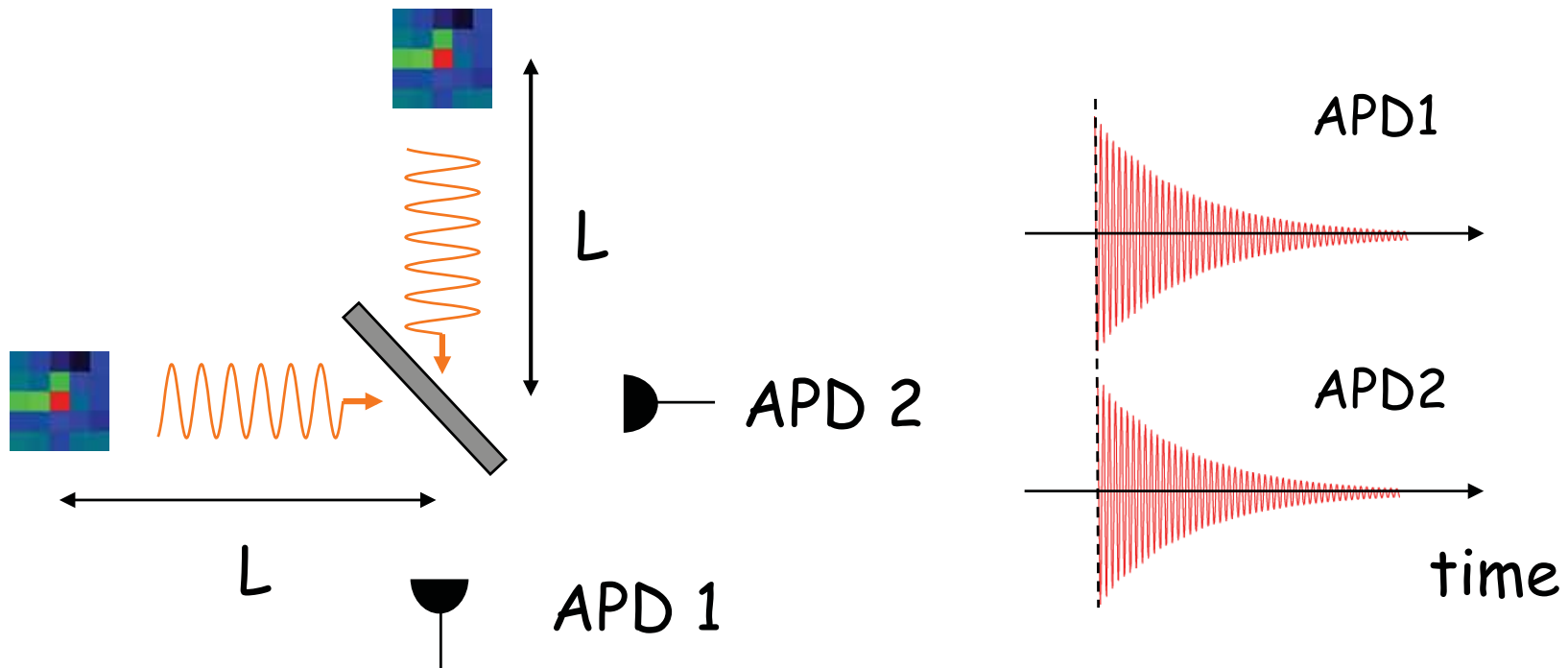
Experimental set-up



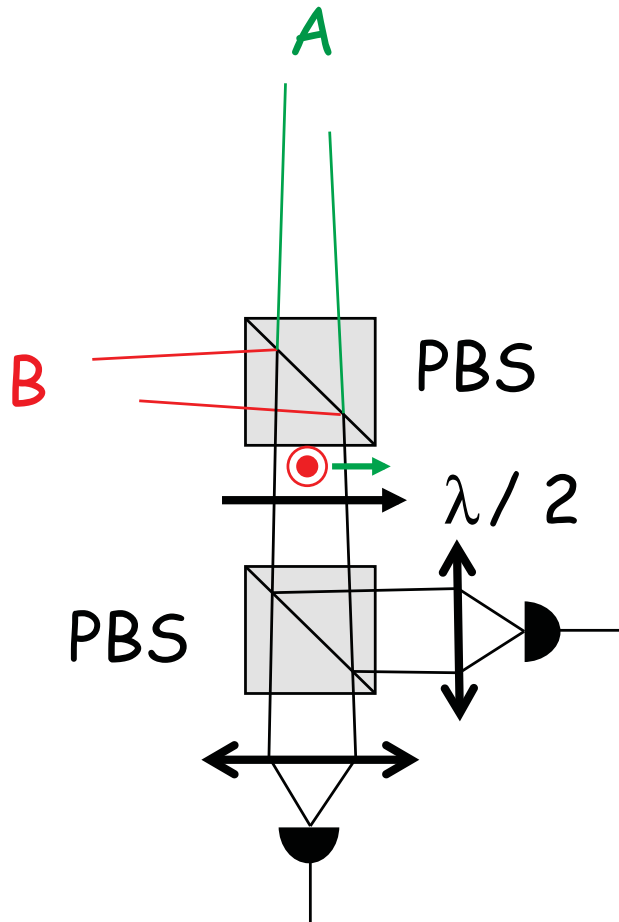
Time-domain matching

Exactly balanced optical paths

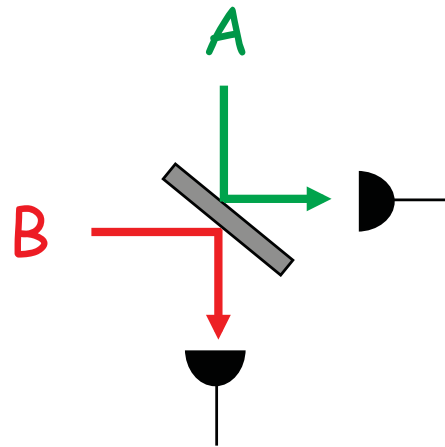
⇒ The two « photon wavepackets » (« 8 m long ») arrive **simultaneously** onto the detectors



Separation vs recombination

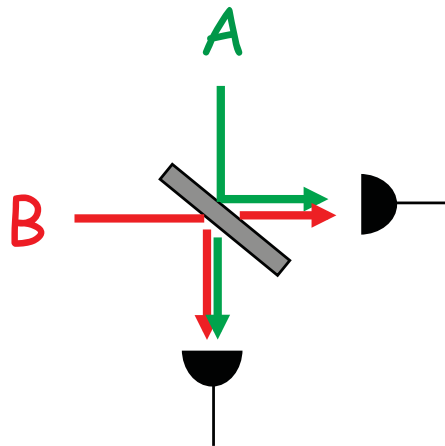


Axis $\lambda/2$ at 0° from pol. axis



Two-sided mirror :
uncorrelated counts

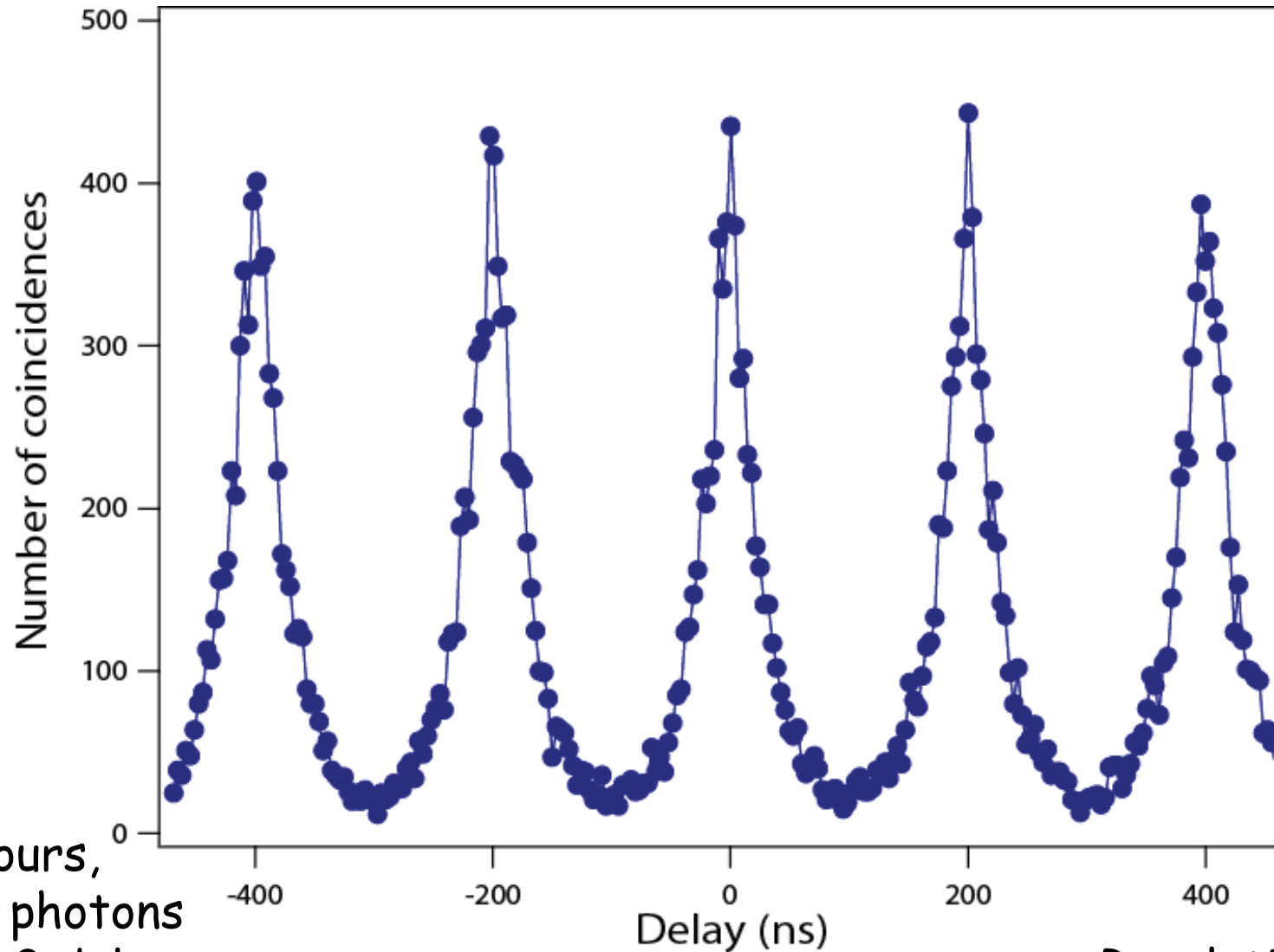
Axis $\lambda/2$ at $22,5^\circ$ of pol. axis



50-50 beamsplitter :
coalescence

Two-atoms coincidences counting

Calibration : « Distinguishable Photons »

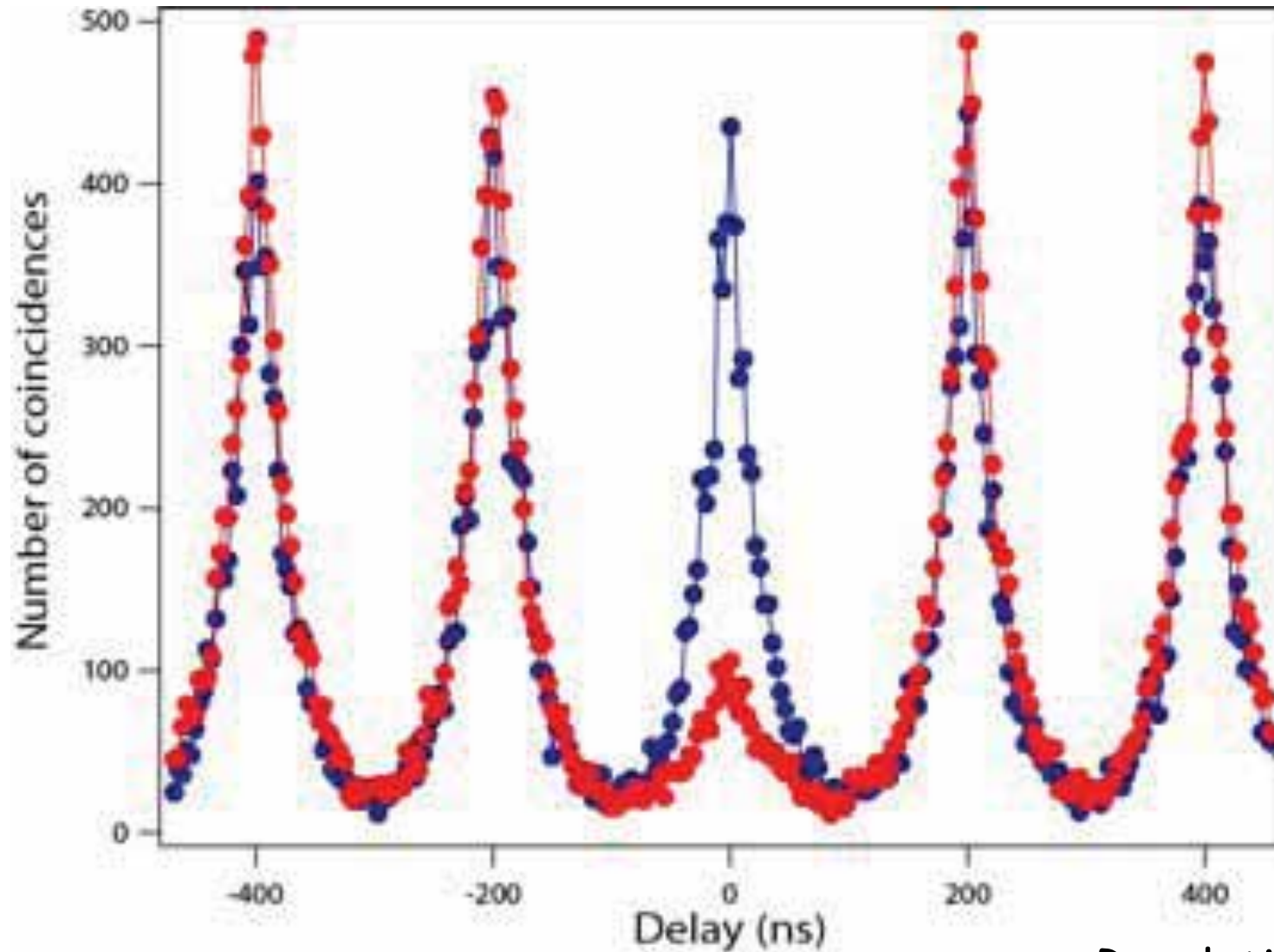


4 hours,
~ 3700 photons
around 0 delay

Resolution 3.6 ns

Coincidences counting

« Indistinguishable Photons »



Resolution 3.6 ns

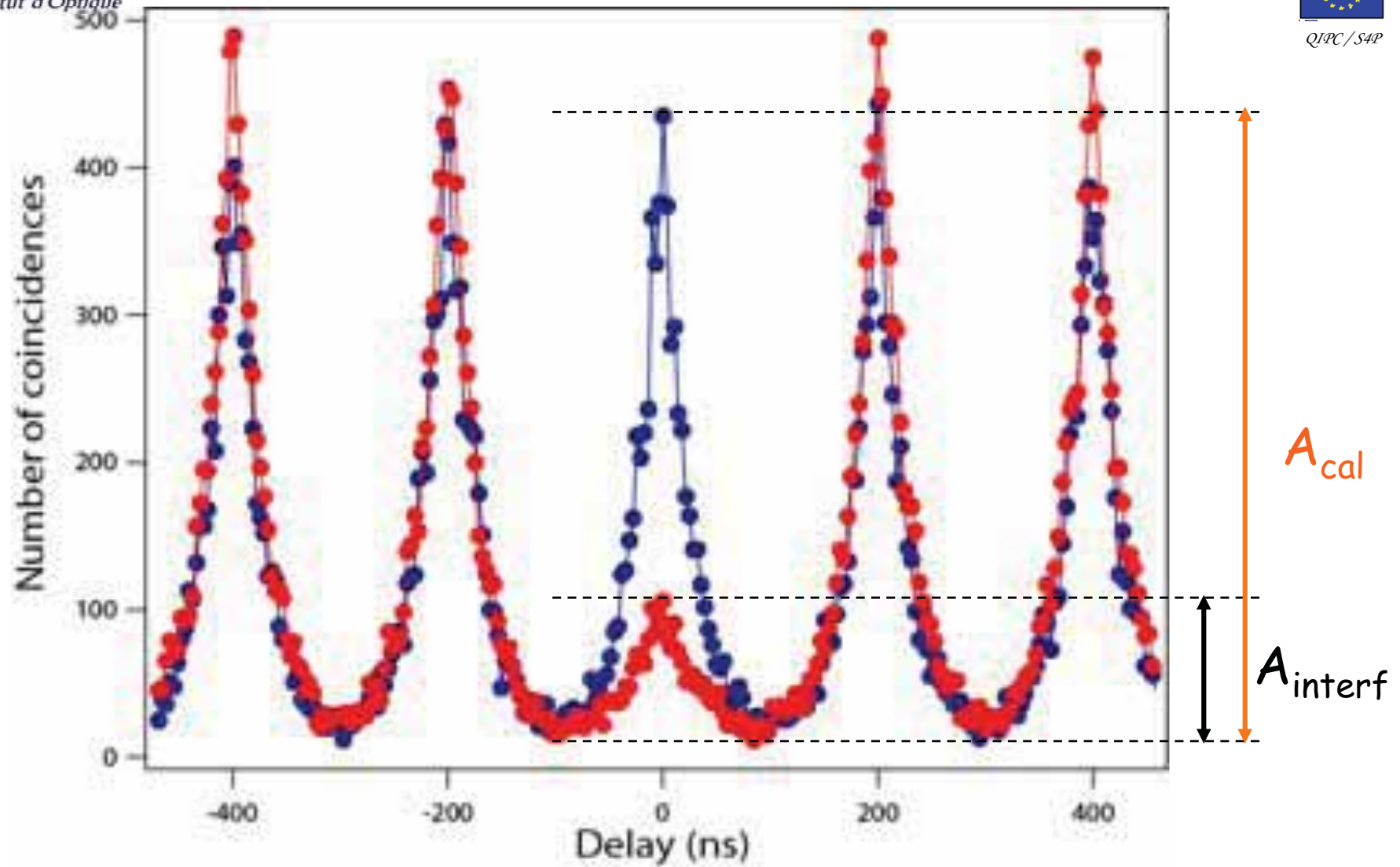


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Coincidences counting



QIPC/S4P



$$\text{Ratio} = A_{\text{interfering}} / A_{\text{calibration}} = 0.19 \pm 0.02$$

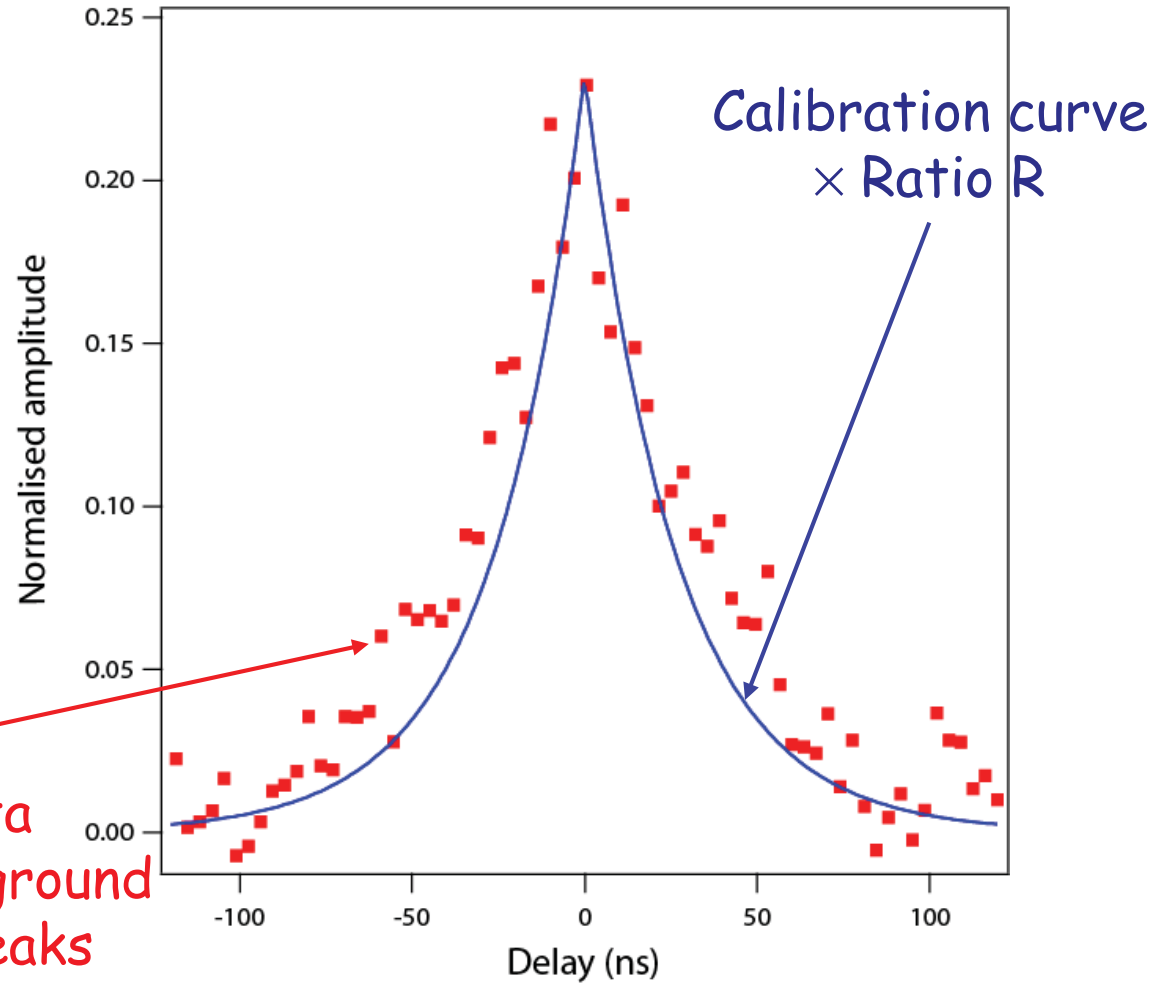
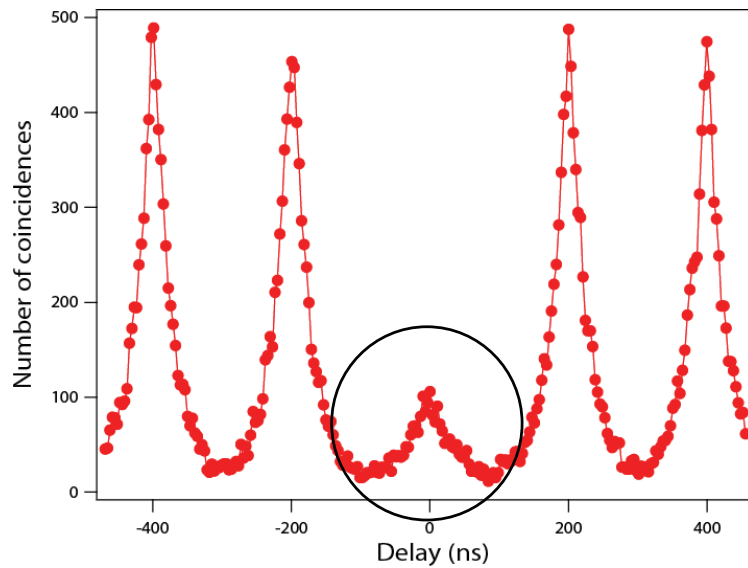


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Shape of the peak around zero delay



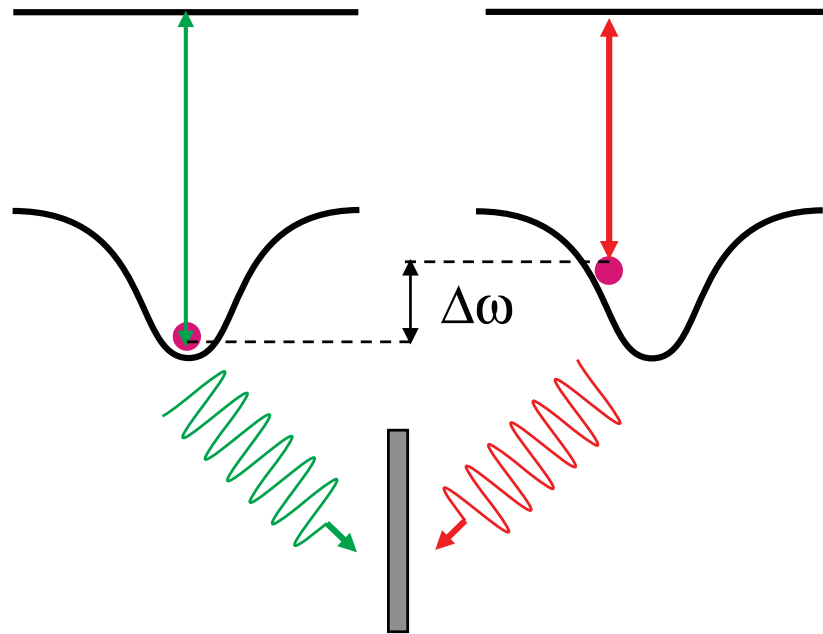
QIPC/SAP



Experimental data corrected from background and neighbouring peaks

Taking into account the atoms' motion

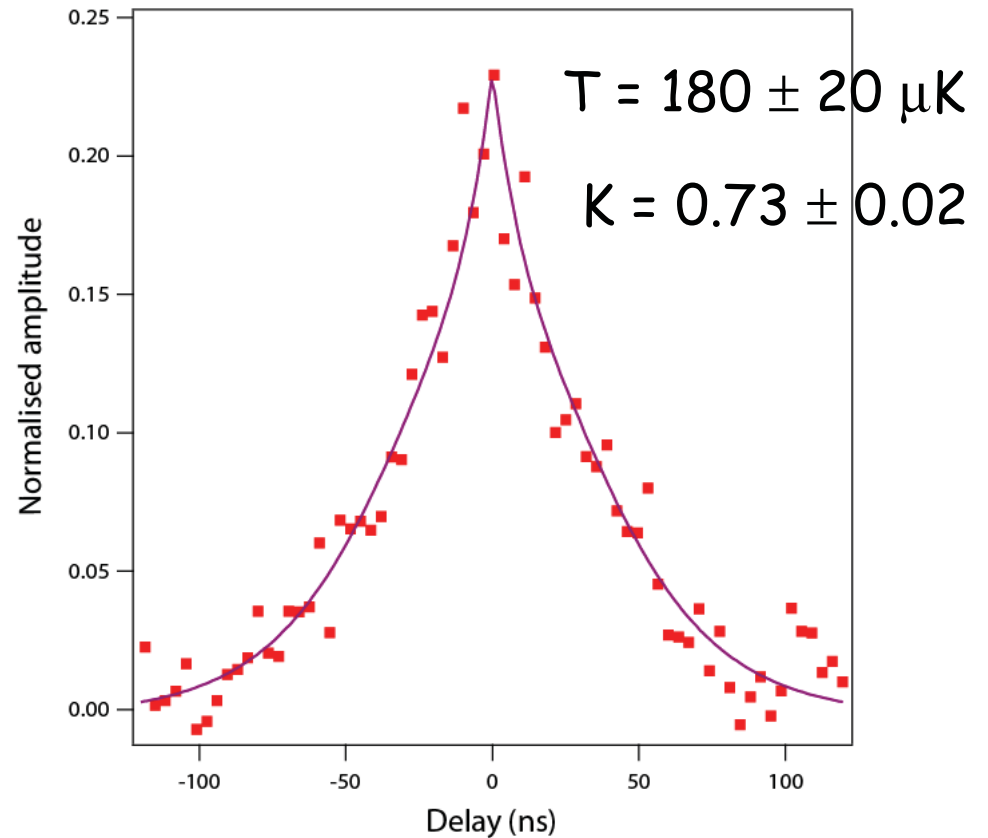
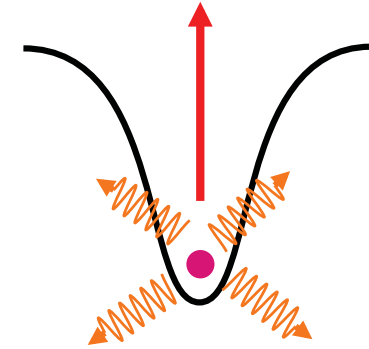
$$\tau = 60 \mu\text{K}$$



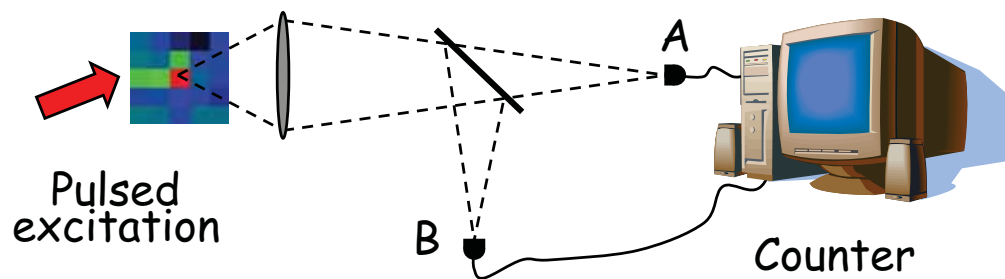
Beat note between the two photons, frequency $\Delta\omega$

Averaged beat note over the distribution of light-shifts \Rightarrow broadening

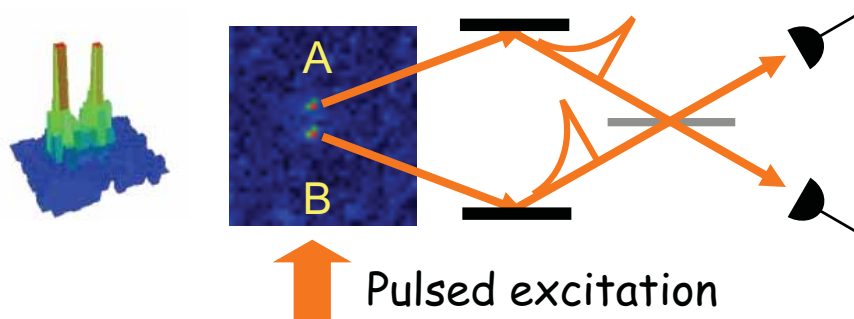
+ heating effect



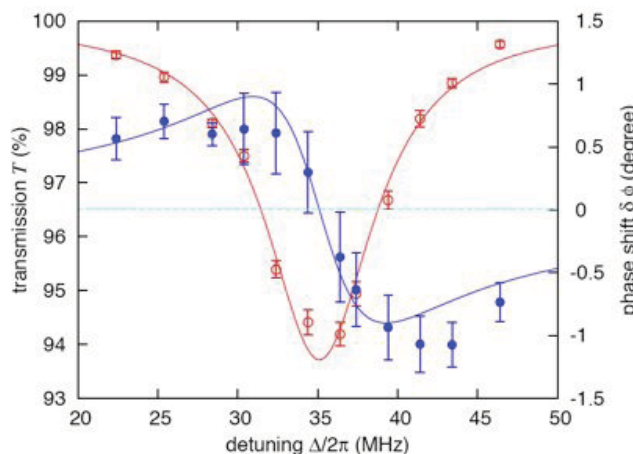
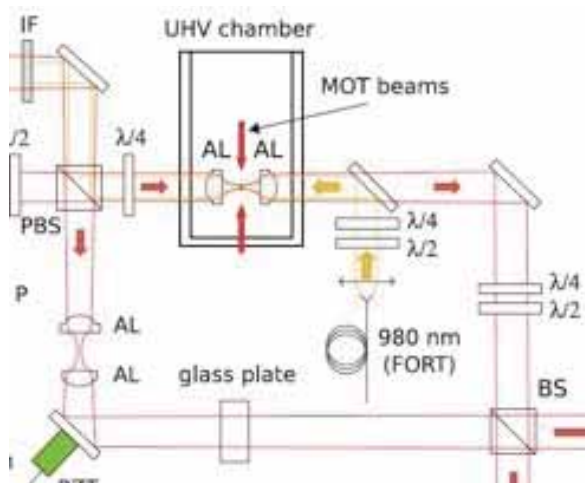
Experiments with single trapped atoms



One single atom emits a transform-limited single photon
 B. Darquié et al,
 Science 309, 454 (2005)



Two single atoms emit two indistinguishable single photons :
 « coalescence » on a beamsplitter
 J. Beugnon et al,
 Nature 440, 776 (2006)



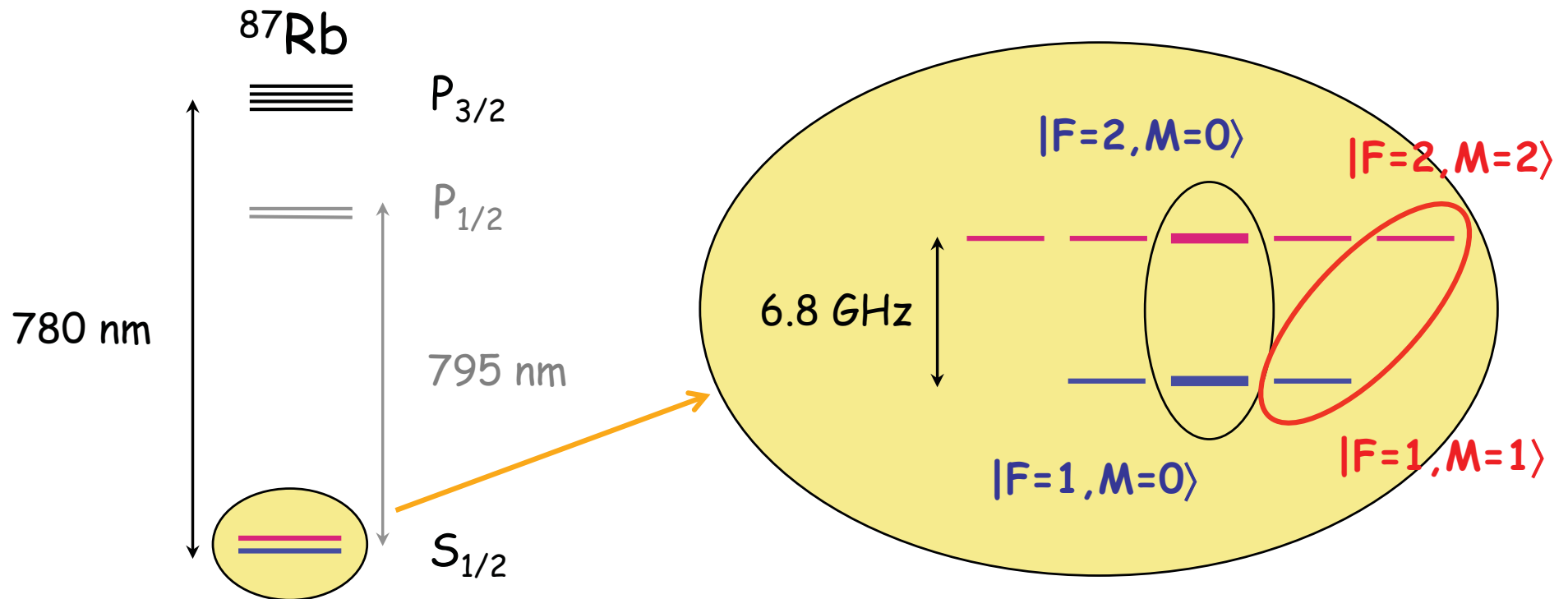
Absorption and dispersion from one single atom
 C. Kurtsiefer et al,
 arXiv:0905.3734v1
 22 May 2009

Part 3

From single atoms to single qubits

The quantum bit

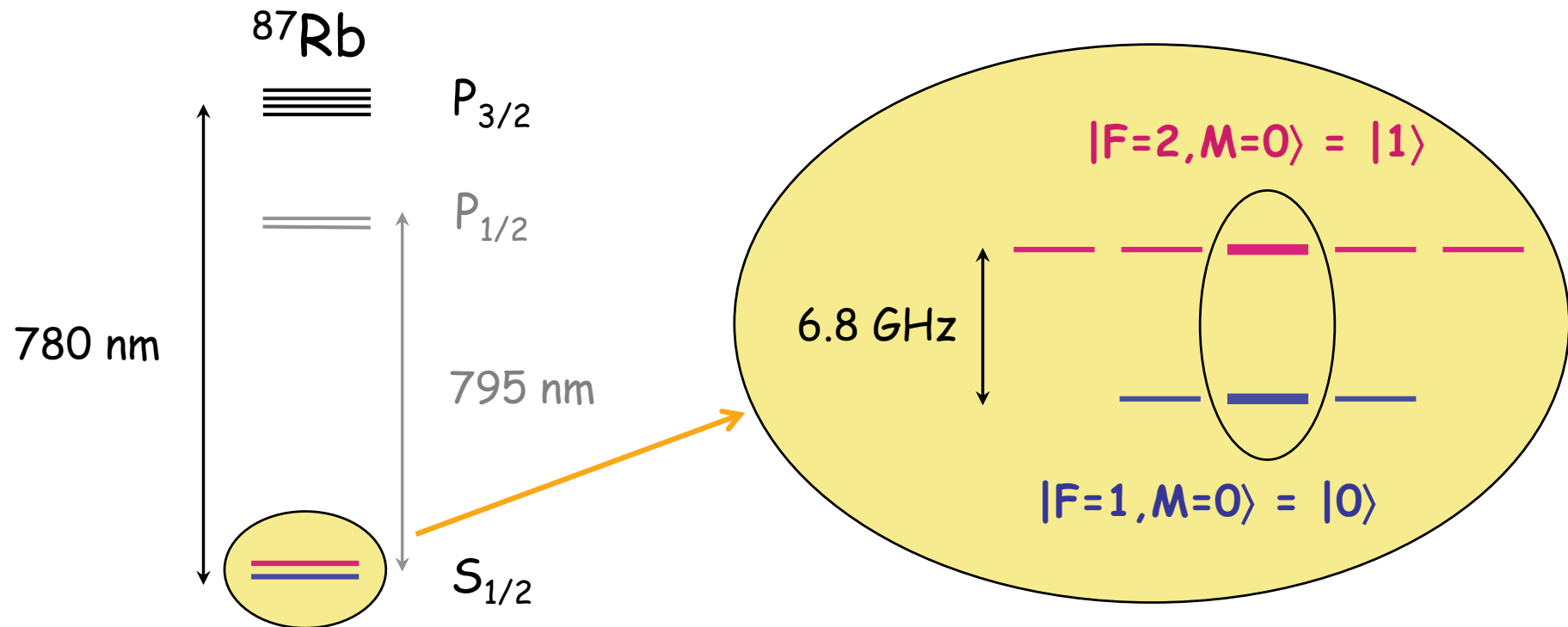
Choose a quantum two-state system with good coherence !



Various choices of M states are possible
0-0, B - insensitive (clock transition)
1-2, easy to prepare (stretched state)

The quantum bit

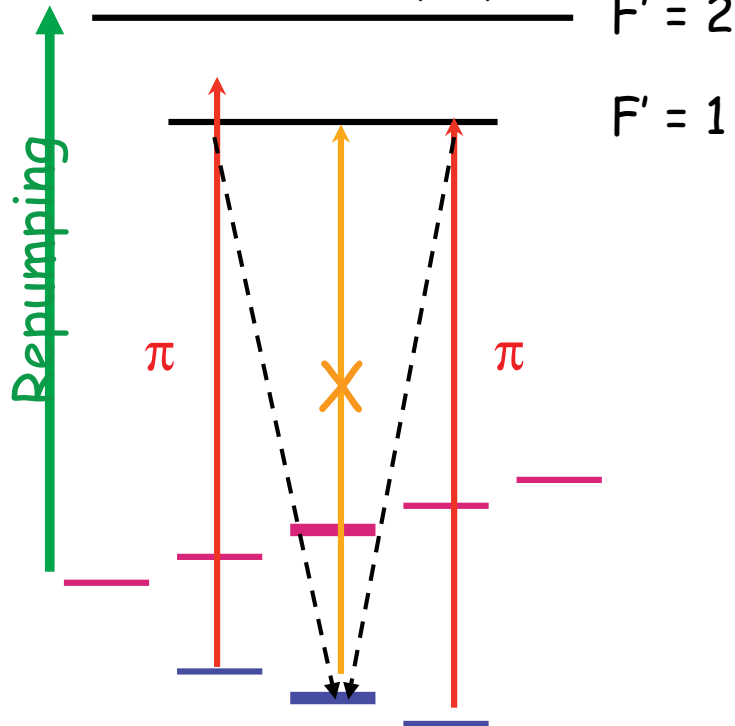
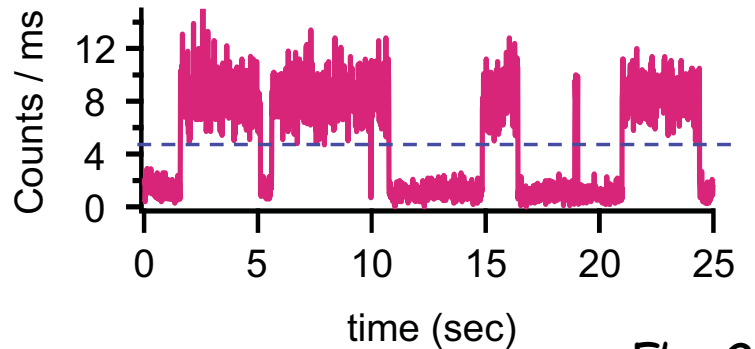
Choose a quantum two-state system with good coherence !



Various choices of M states are possible
Preferred choice : 0-0, B - insensitive
(clock transition)

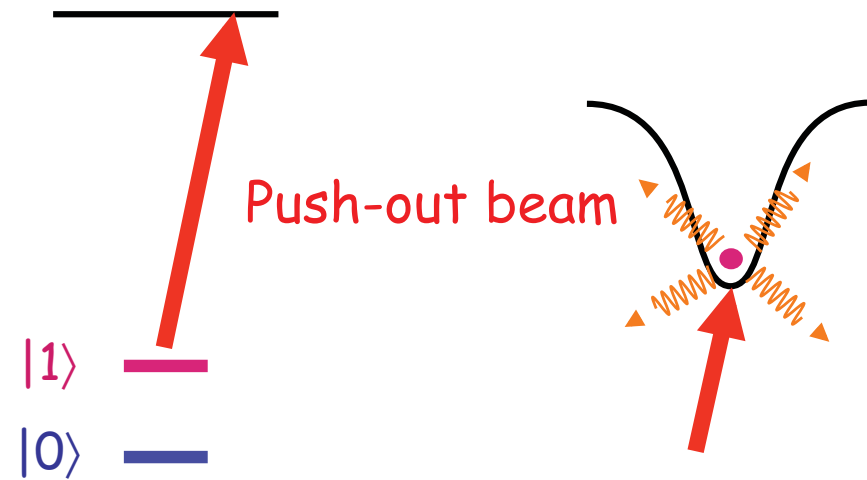
The toolbox: initialization and readout of the qubit

Detection + Initialization



Efficiency: 85% in $|0\rangle$

State-selective detection



Check for the presence of the atom

No atom $\Rightarrow |1\rangle$
Atom $\Rightarrow |0\rangle$

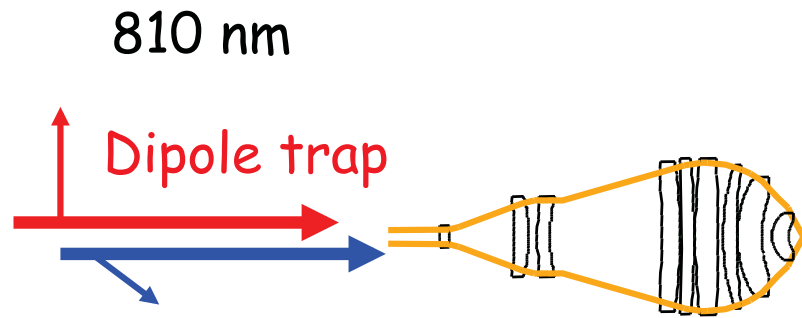
98% efficiency, quantum projection noise limited

Single qubit rotation

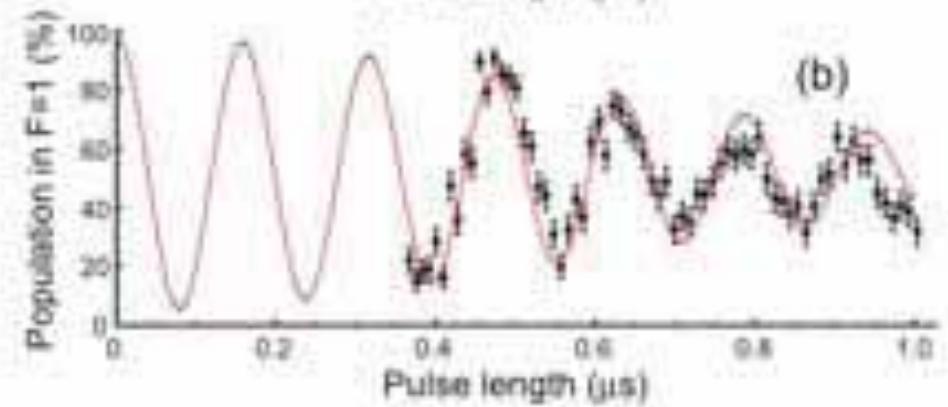
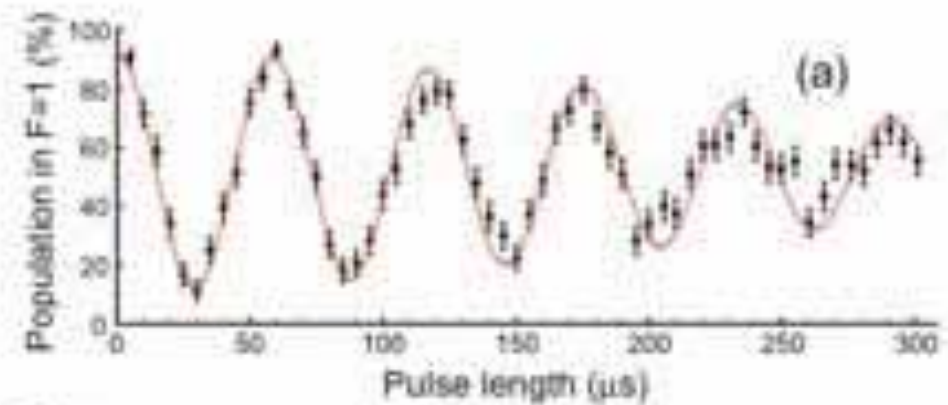
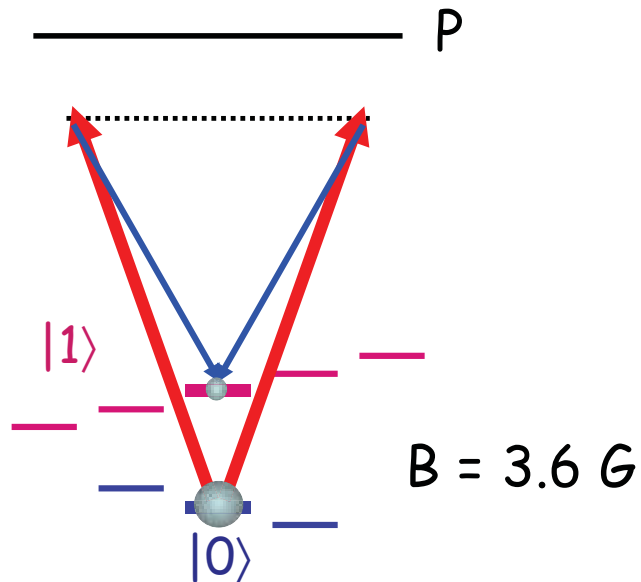
Prepare $|\Psi\rangle = \cos\theta |0\rangle + \sin\theta |1\rangle$

Average ~ 200 times

Low intensity: $\pi/2$ pulse in $13 \mu\text{s}$



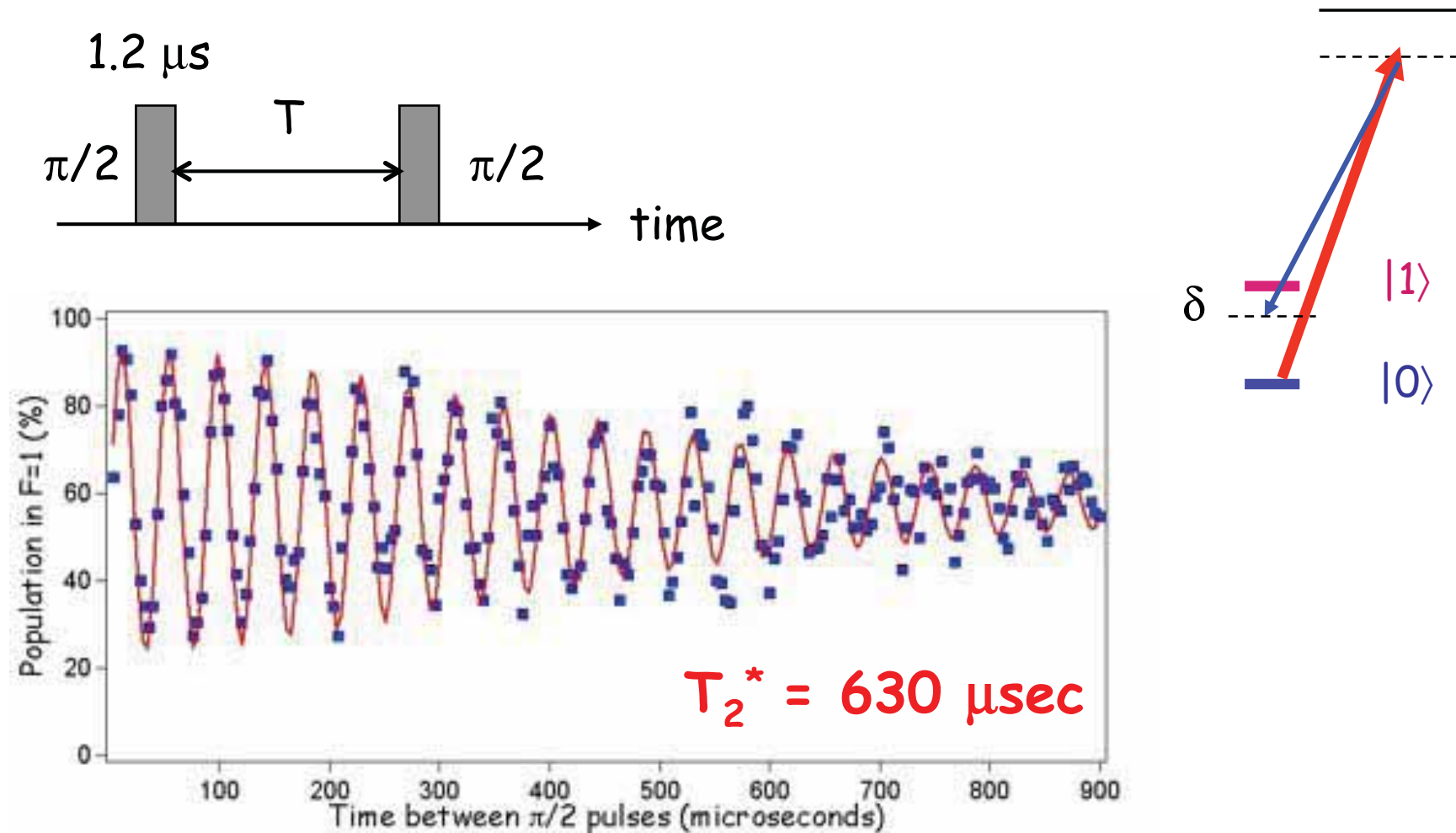
Raman transitions
(2 phase-locked laser diodes)



High intensity: $\pi/2$ pulse in 37 ns

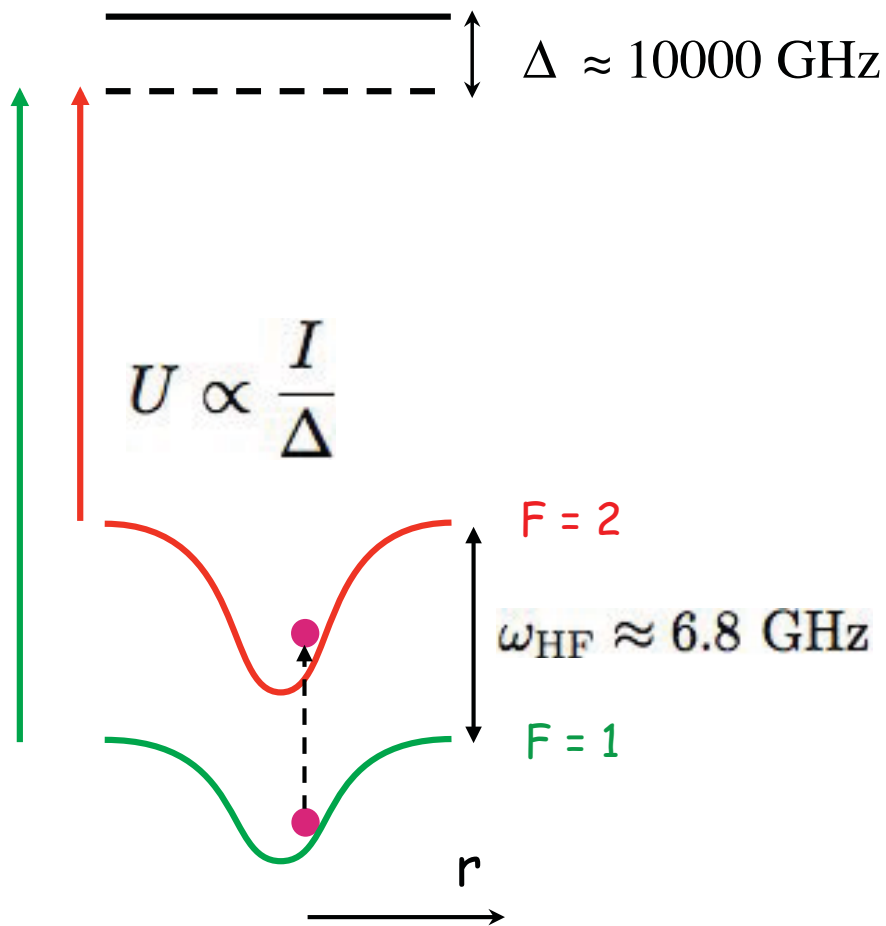
Coherence of the qubit: Ramsey spectroscopy

How stable is φ in $\cos\theta |0\rangle + \sin\theta e^{i\varphi} |1\rangle$?



Decay : limited by residual motion of the atom in the trap

Decay of the Ramsey fringes: coupling external/internal



$$\eta = \frac{\omega_{\text{HF}}}{\Delta} \approx 7 \times 10^{-4}$$

Averaged over the motion of the atom during the pulse
+
Different energy from one atom to another (thermal)

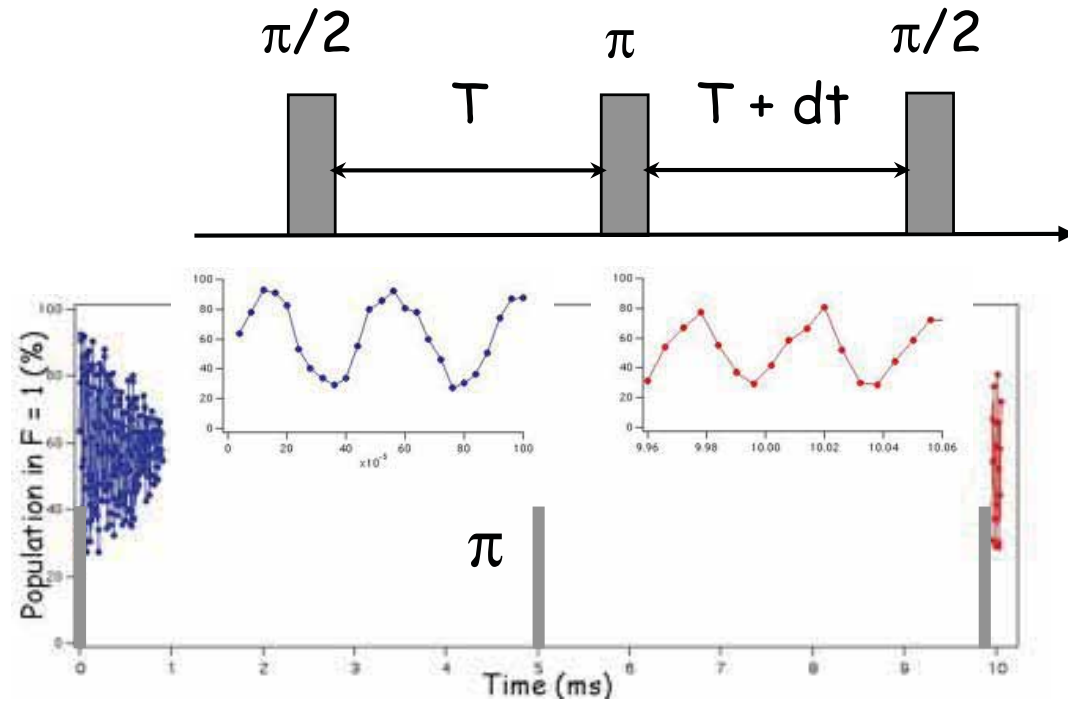
$$\Delta\omega \sim \eta \frac{k_{\text{B}}T}{\hbar} \sim 700\text{Hz}$$

Differential light shift

$$\propto \frac{\omega_{\text{HF}}}{\Delta} U(r(t))$$

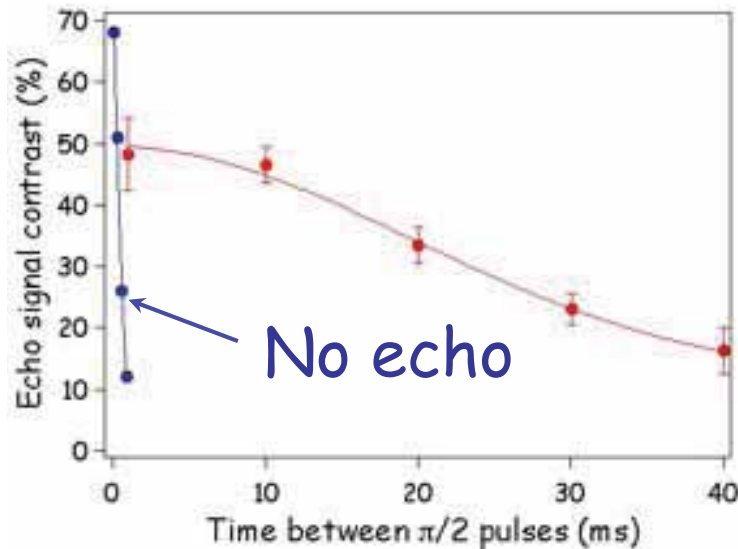
\Rightarrow « dephasing » : ok

Reversible dephasing: spin echo



π pulse:
 $|0\rangle \rightarrow |1\rangle$
 $|1\rangle \rightarrow -|0\rangle$

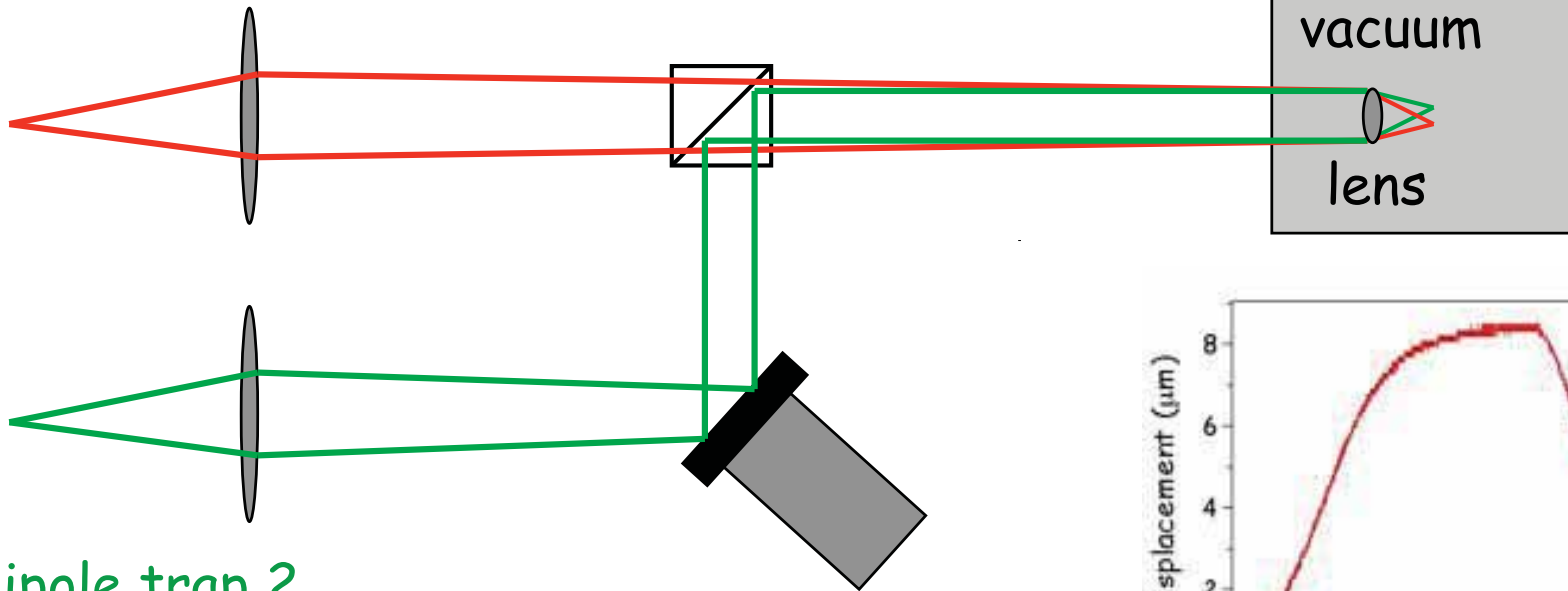
We can « rephase » the atoms after ~ 40 ms
 = $70 \times$ coherence time



Irreversible decoherence time (40 ms)
 = $10^6 \times$ the $\pi/2$ Rabi flopping time (40 ns)

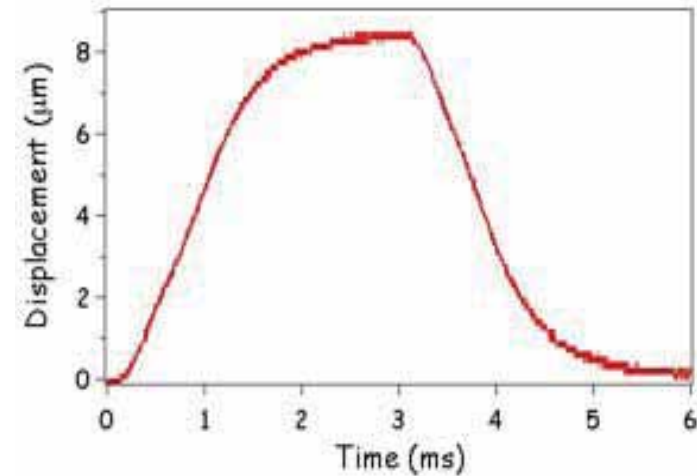
Moving the qubits

Dipole trap 1



Dipole trap 2

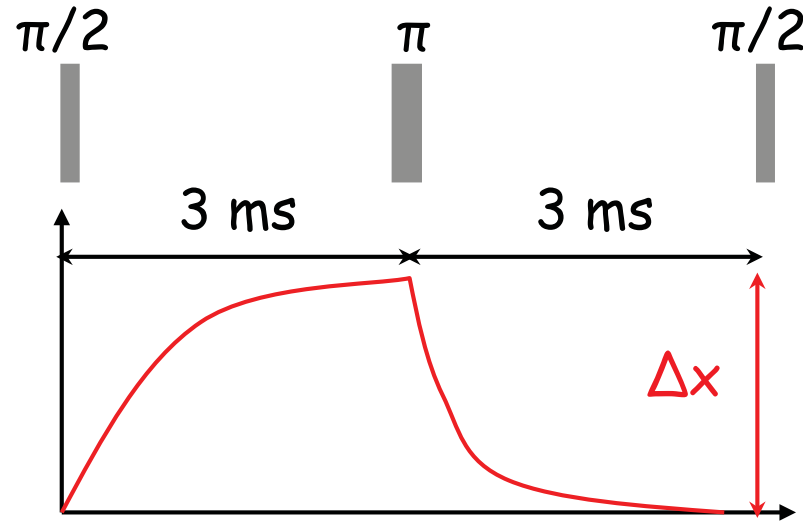
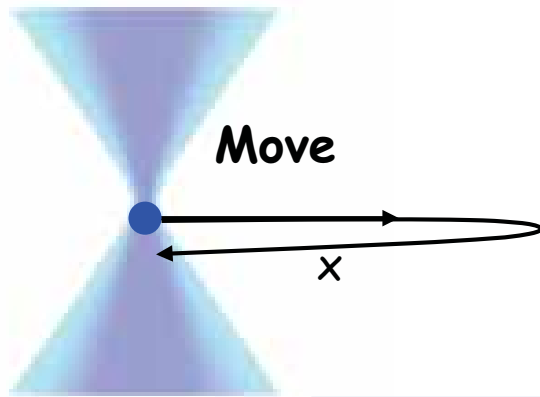
Tip-tilt platform (x-y)



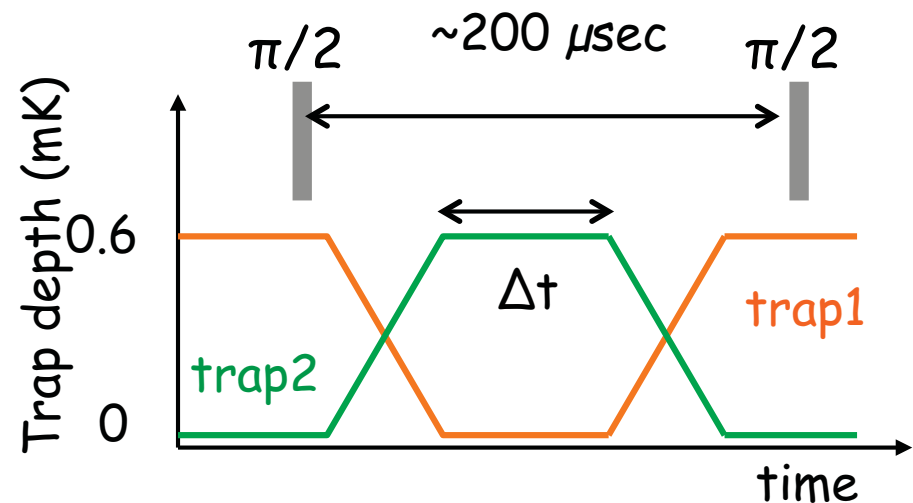
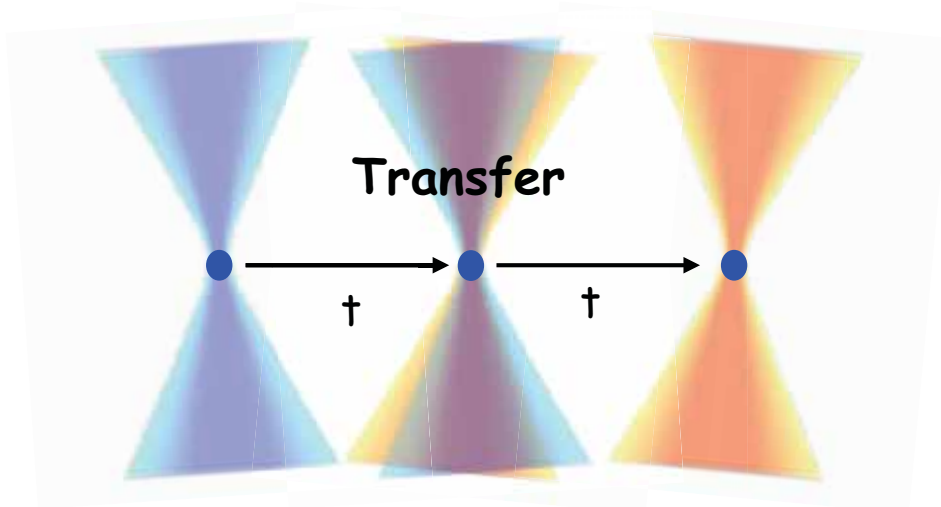
- Scale of the motion :
a few μm in a few ms
- OK for a quantum register
(coherence time : tens of ms)

Motion and transfer of single qubits

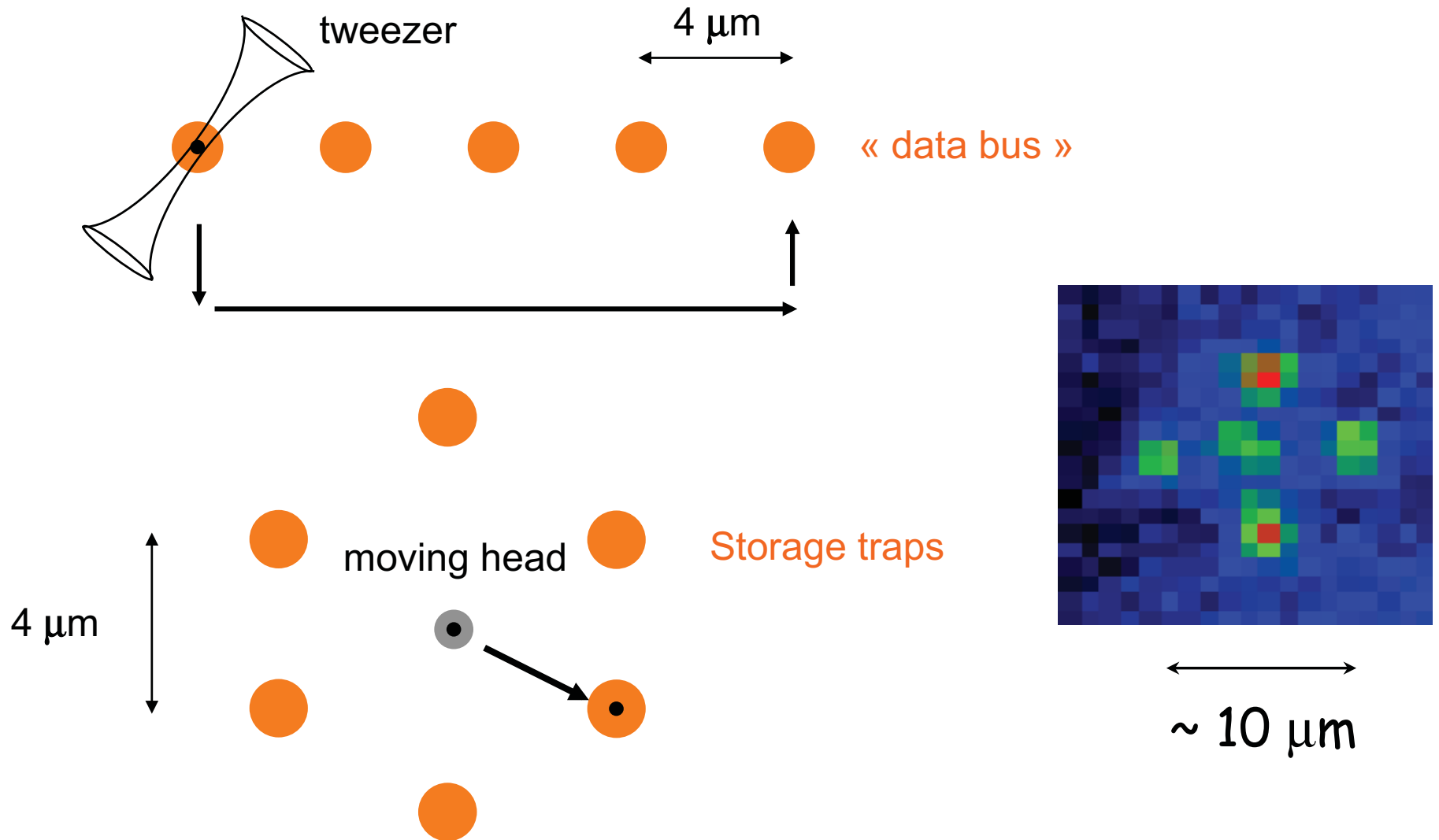
J. Beugnon et al,
Nature Physics 3, 696 (2007)



No loss; no heating on motion, little heating on transfer; no qubit decoherence : OK !



Looking to the future : "quantum register"



Moving head in a quantum register ?
Requires entanglement !

Thank you for your attention...

(and see you tomorrow !)