

“RHIC Serves a Near-Perfect Fluid” --- a Paradigm Shift

Jiunn-Wei Chen

National Taiwan U.

QCD Phase Diagram

2

M. Stephanov

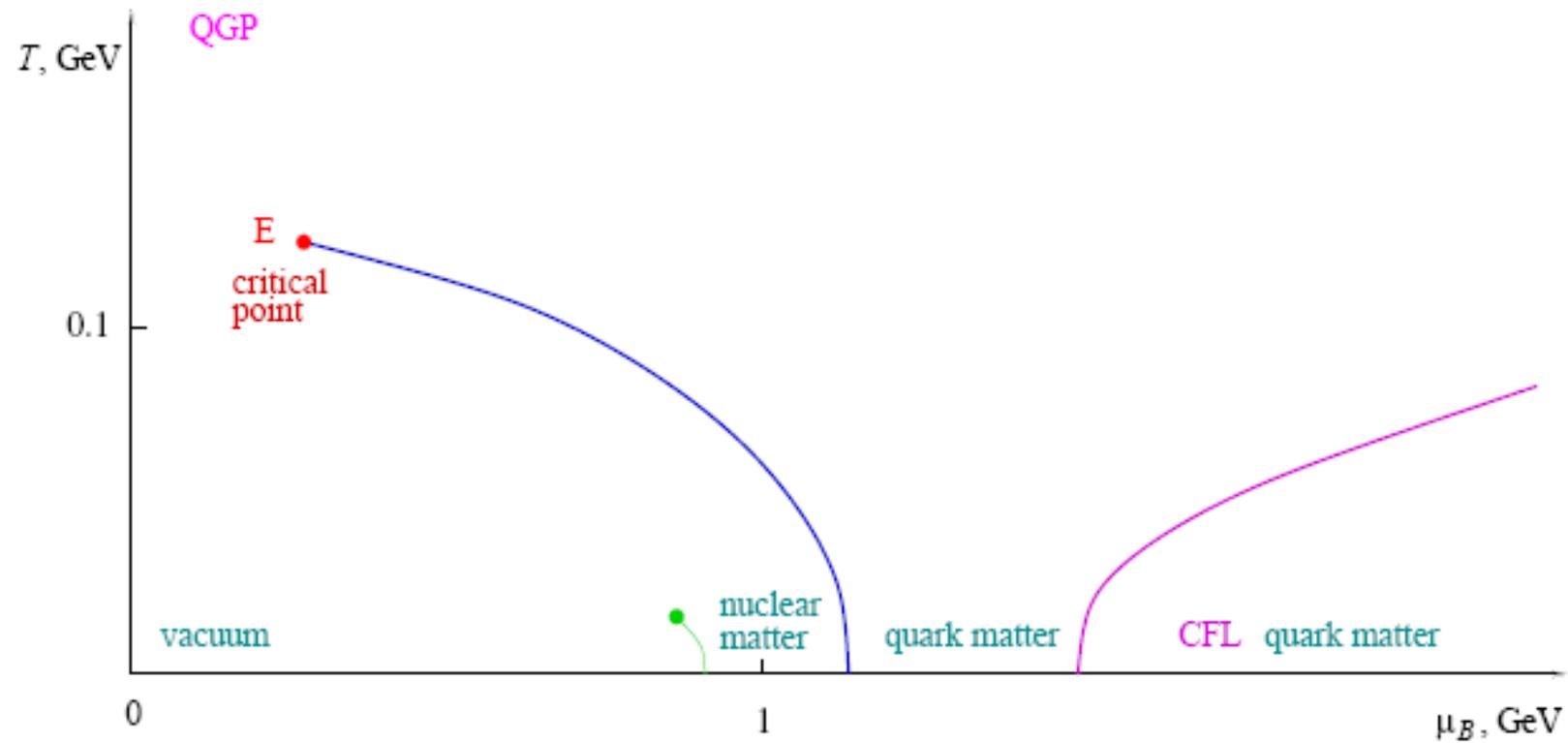


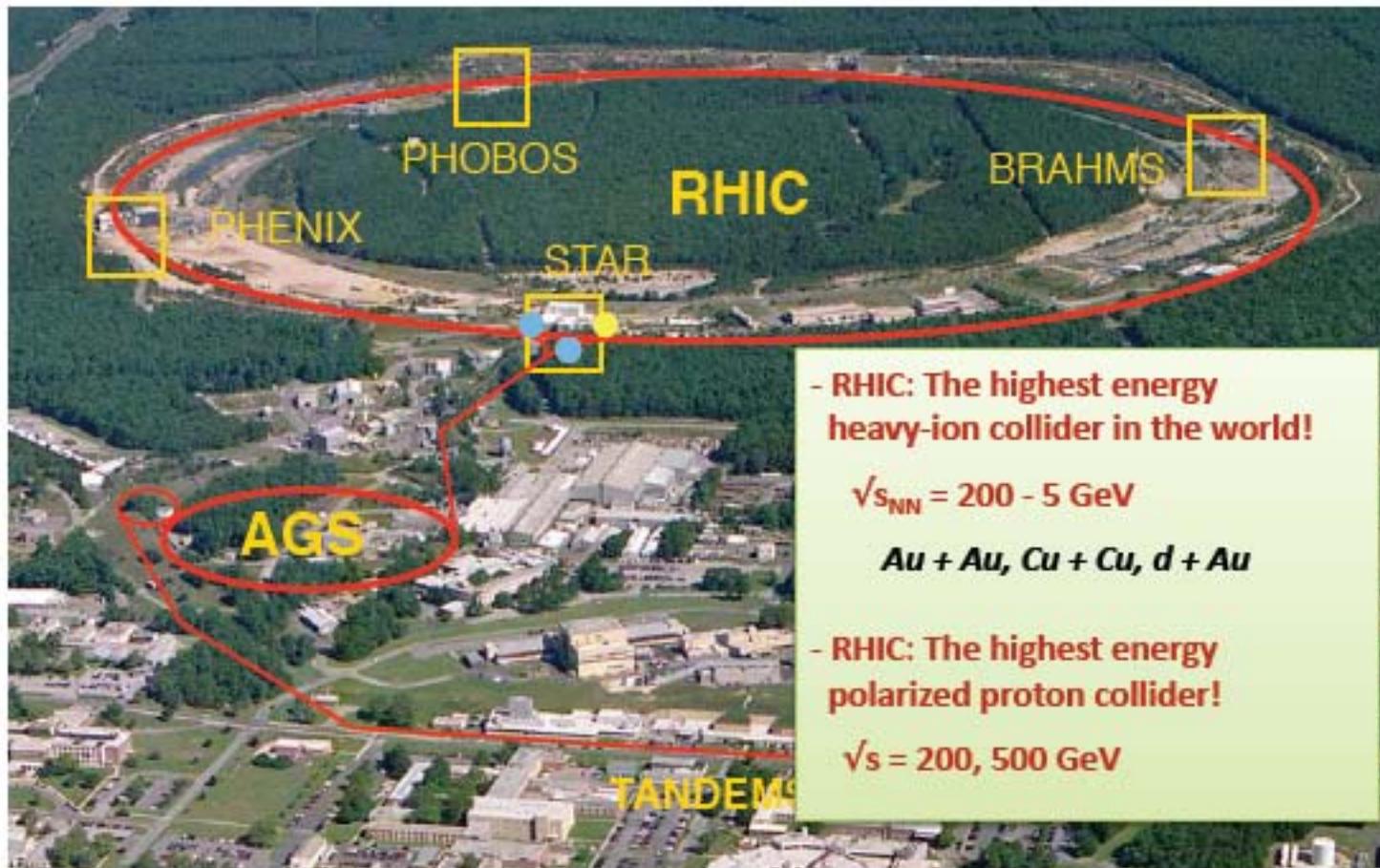
Fig. 1. QCD phase diagram



Relativistic Heavy Ion Collider (RHIC)

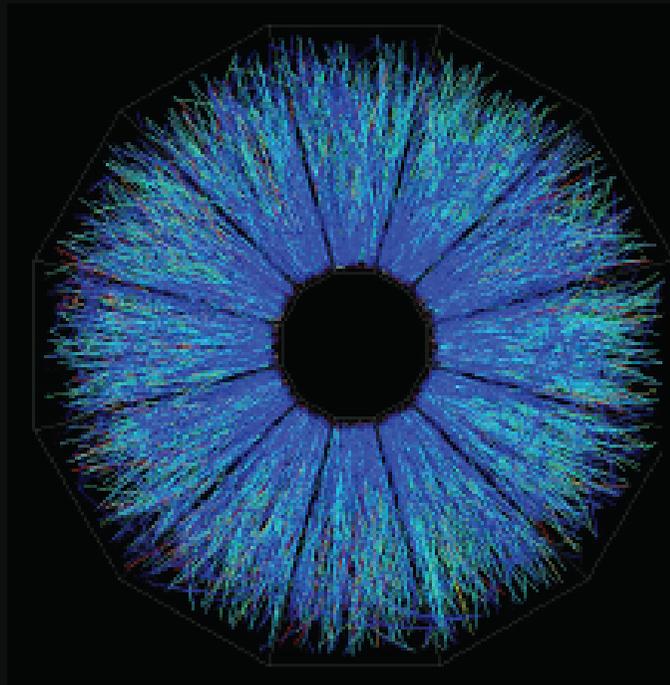


Brookhaven National Laboratory (BNL), Upton, NY

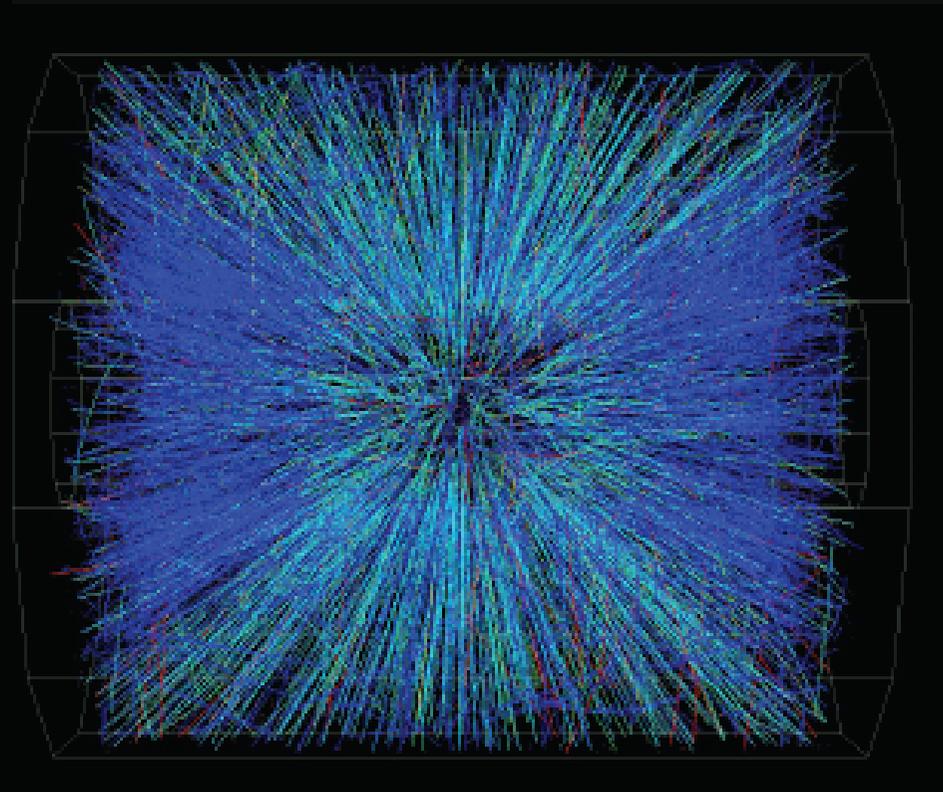


Animation M. Lisa

Au + Au Collisions at RHIC



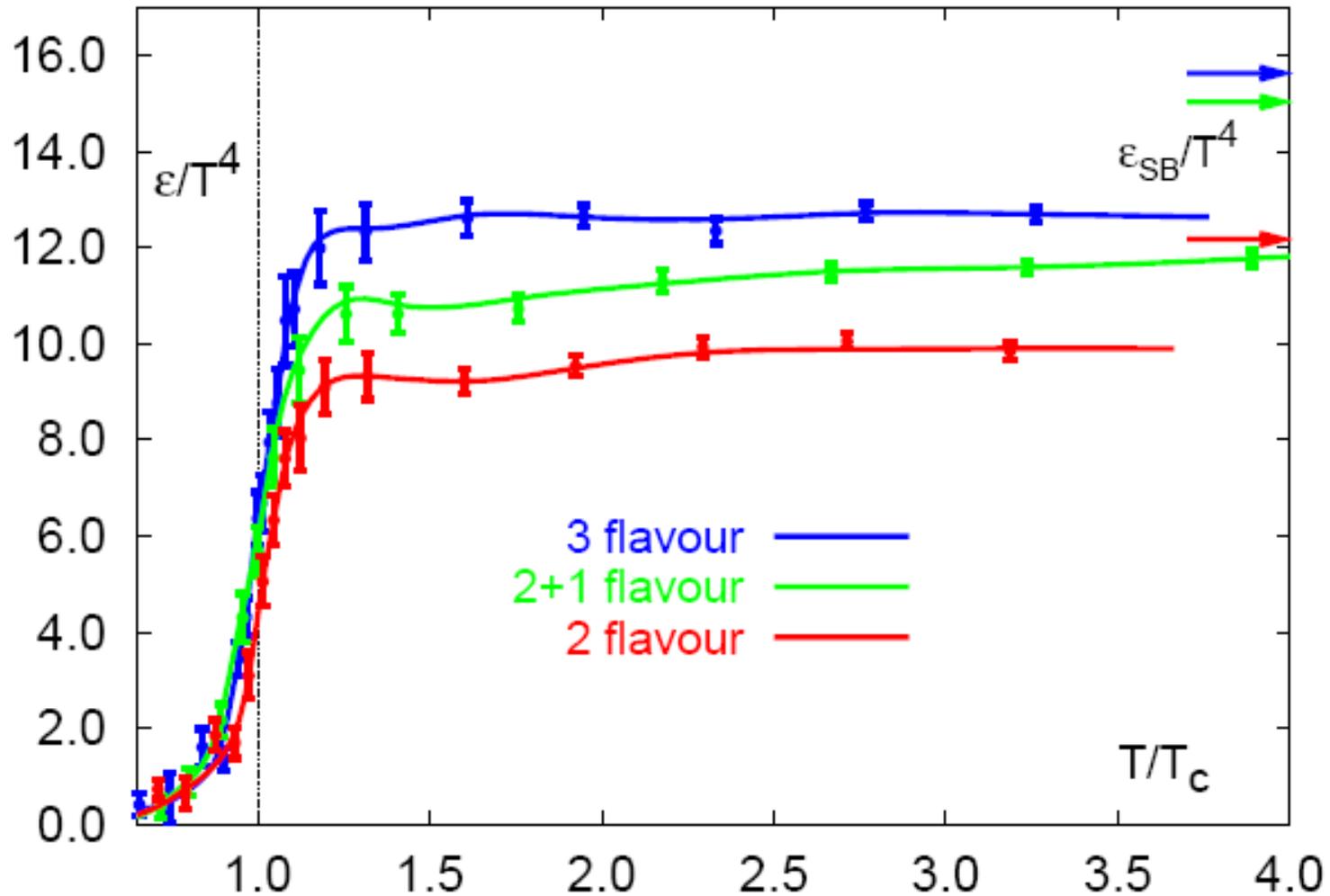
Central Event



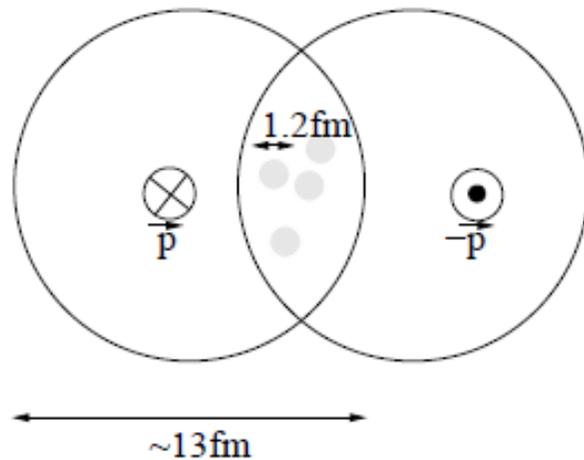
(real-time Level 3)

ATHIC 2008, Tsukuba, Japan, Oct. 13 - 15, 2008

QGP EOS (LQCD) ~ an ideal gas

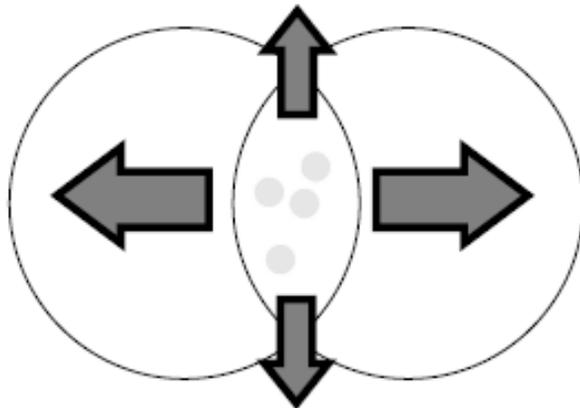


Elliptic Flow: QGP ~ a perfect fluid



$$\frac{\eta}{s} = 0.1 \pm 0.1(\text{th}) \pm 0.08(\text{exp})$$

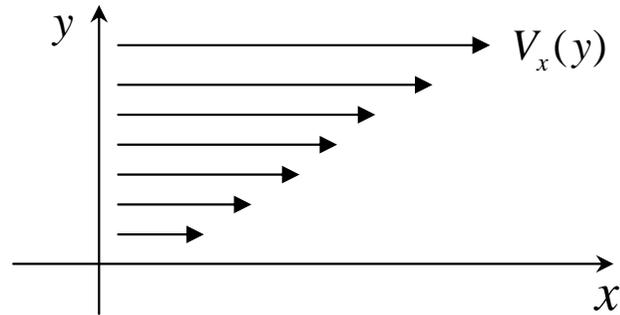
Luzum, Romatschke, 2008



A Paradigm shift!

Figure: H. Meyer

- Shear viscosity



Frictional force

$$T_{ij} = -\eta \left(\frac{\nabla_i V_j(x) + \nabla_j V_i(x)}{2} - \frac{1}{3} \delta_{ij} \nabla \cdot V(x) \right).$$

Shear viscosity measures
how “perfect” a fluid is!

- Kovtun, Son, and Starinets ('05)

Conjecture: Shear viscosity / entropy density

$$\frac{\eta}{s} \geq \frac{1}{4\pi}$$

- Motivated by AdS/CFT

$$\eta = \lim_{\omega \rightarrow 0} \frac{1}{2\omega} \int dt d\mathbf{x} e^{i\omega t} \langle [T_{xy}(t, \mathbf{x}), T_{xy}(0, \mathbf{0})] \rangle$$

$$\eta = \frac{\sigma_{\text{abs}}(0)}{16\pi G}$$

$$\frac{\eta}{s} \geq \frac{1}{4\pi}$$

- “QGP” (quark gluon plasma) almost saturates the bound @ just above T_c (Teaney; Romatschke, Romatschke; Song, Heinz)
- LQCD, gluon plasma (Karsch, Wyld; Nakamura, Sakai; Meyer)
 - ⇒ QGP near T_c , a perfect fluid, **SQGP**
- **PQGP**: Asakawa, Bass, Müller; Xu, Greiner

QCD Phase Diagram

2

M. Stephanov

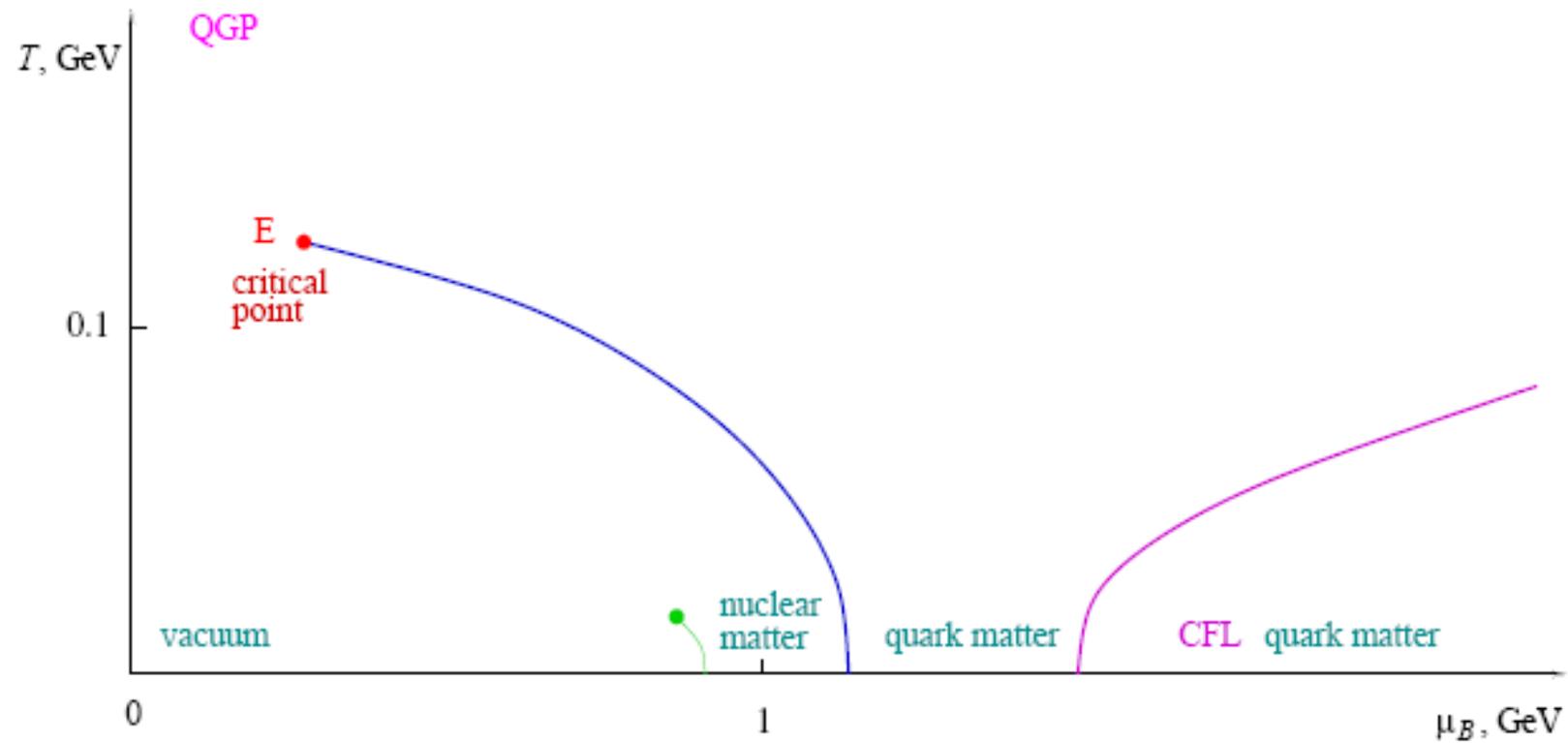


Fig. 1. QCD phase diagram

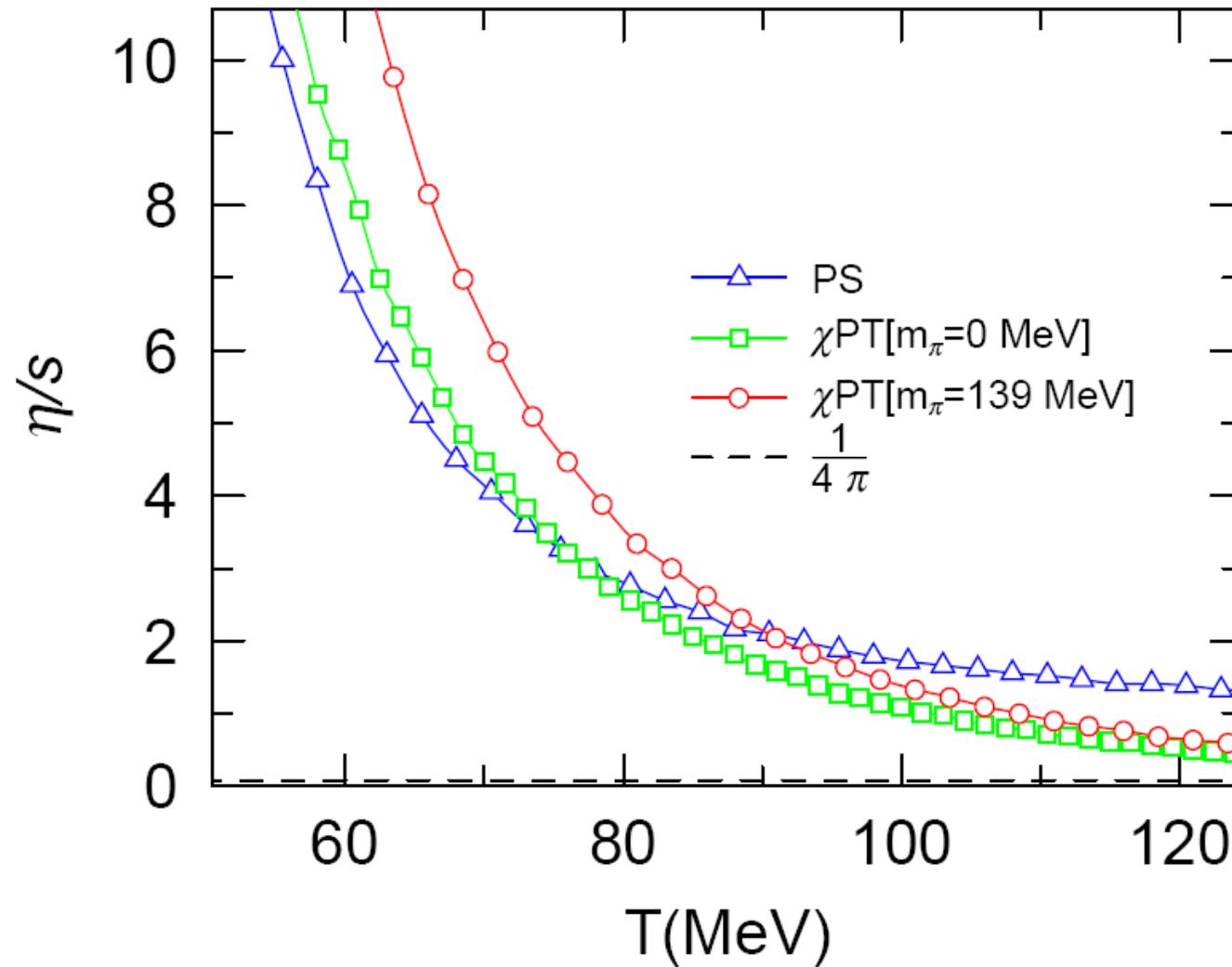
η/s of QCD below T_c

- Pion gas \Rightarrow ChPT (chiral perturbation theory)
- Non-perturbative in coupling
 \Rightarrow Boltzmann equation

Earlier work: [Prakash, Prakash, Venugopalan, Welke;](#)

[Dobado, Llanes-Estrada; Csernai, Kapusta, McLerran](#)

η/s of QCD below T_c



QCD Phase Diagram

2

M. Stephanov

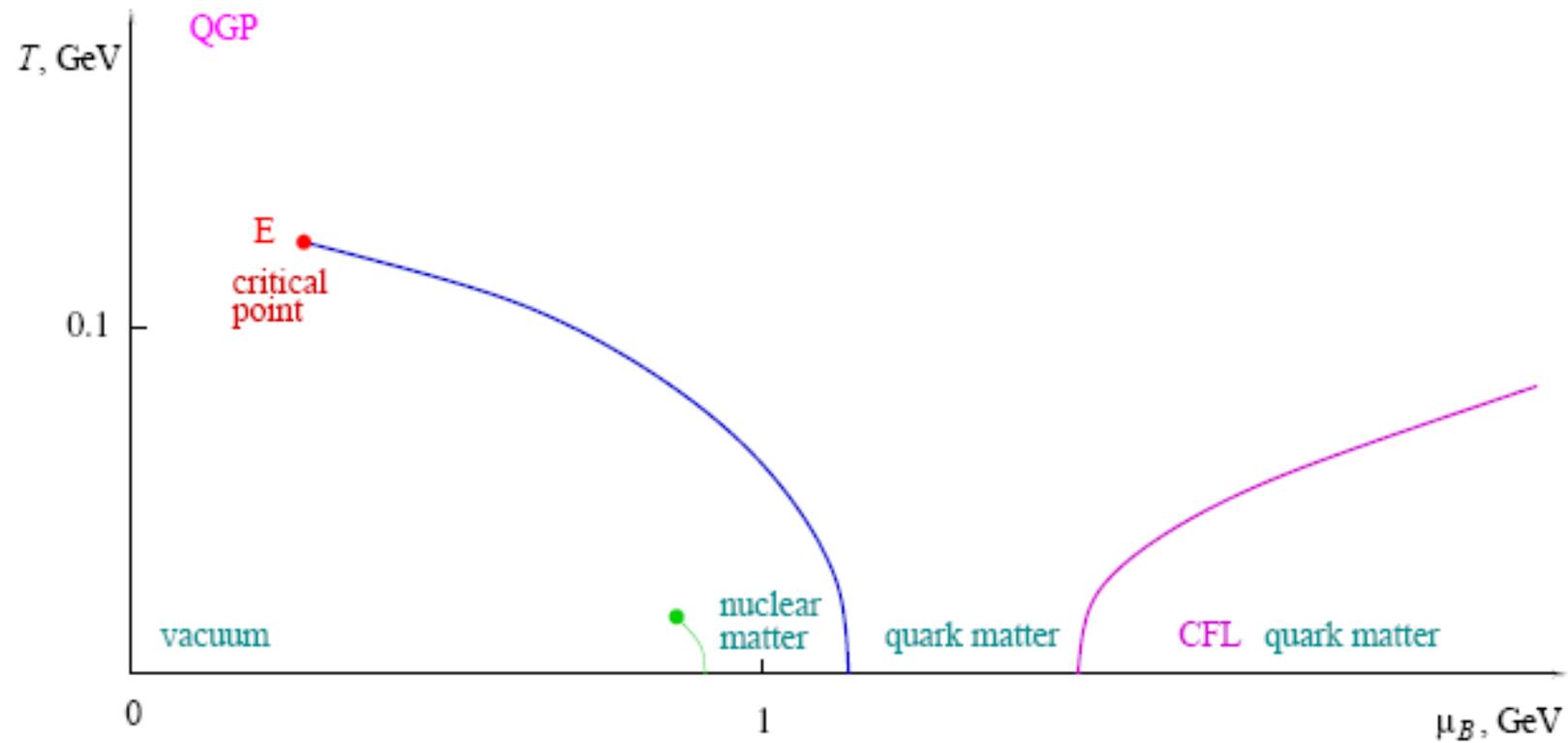
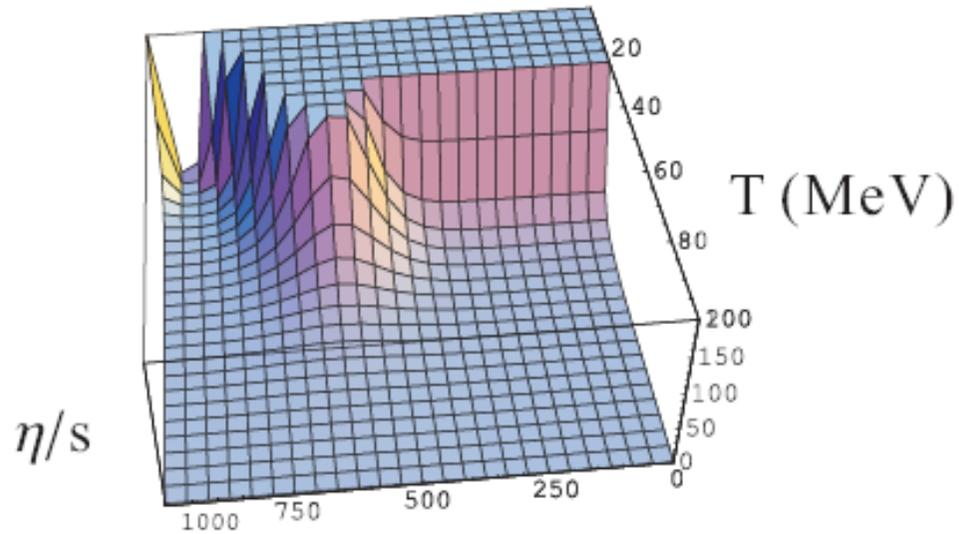
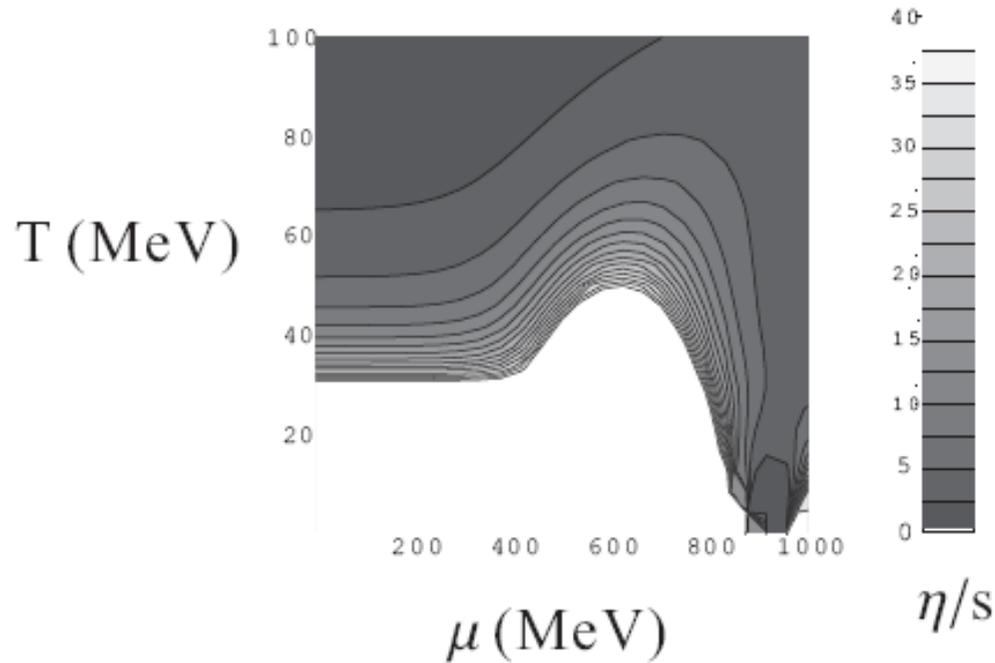


Fig. 1. QCD phase diagram

The η/s “Landscape”

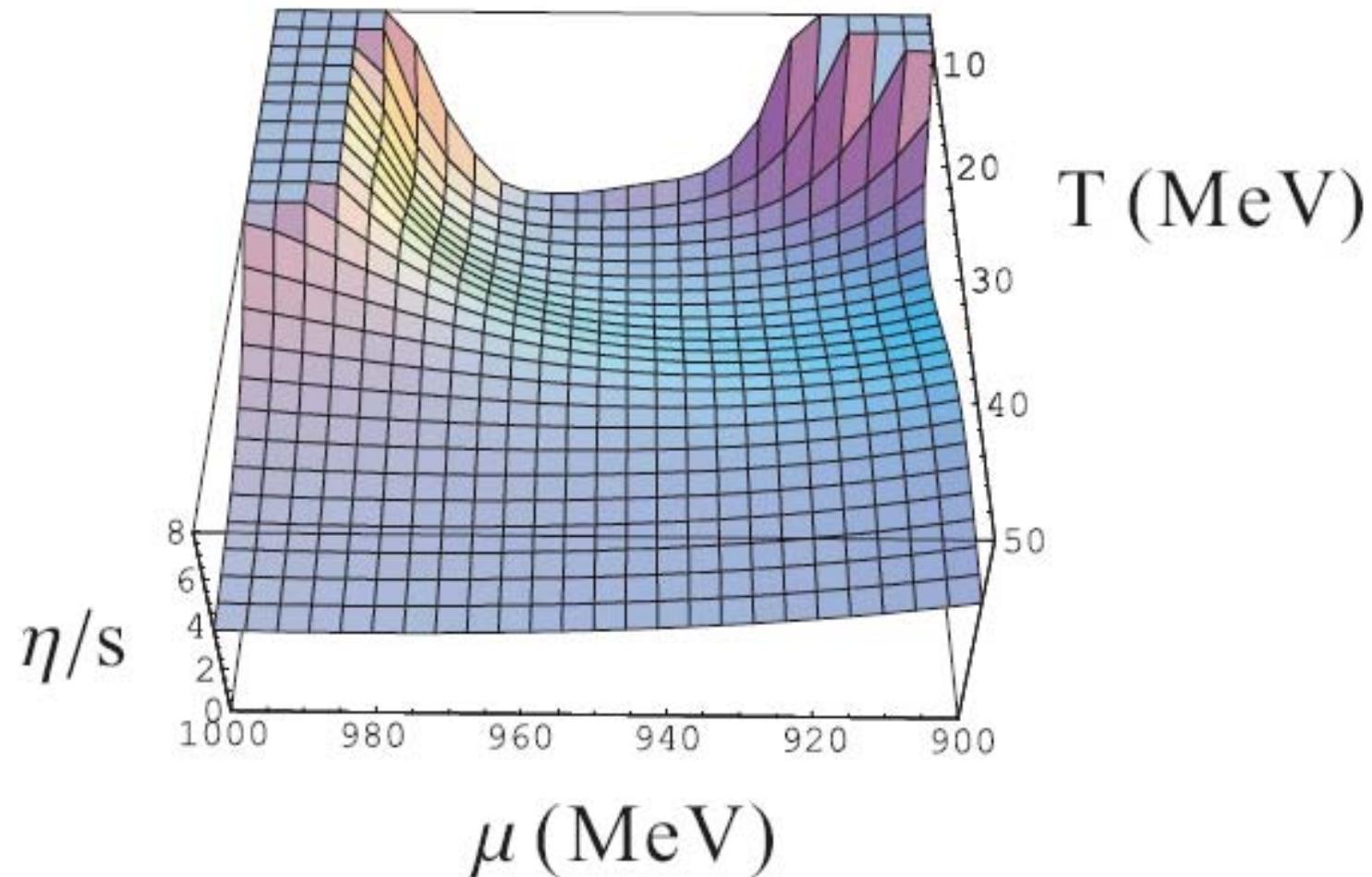


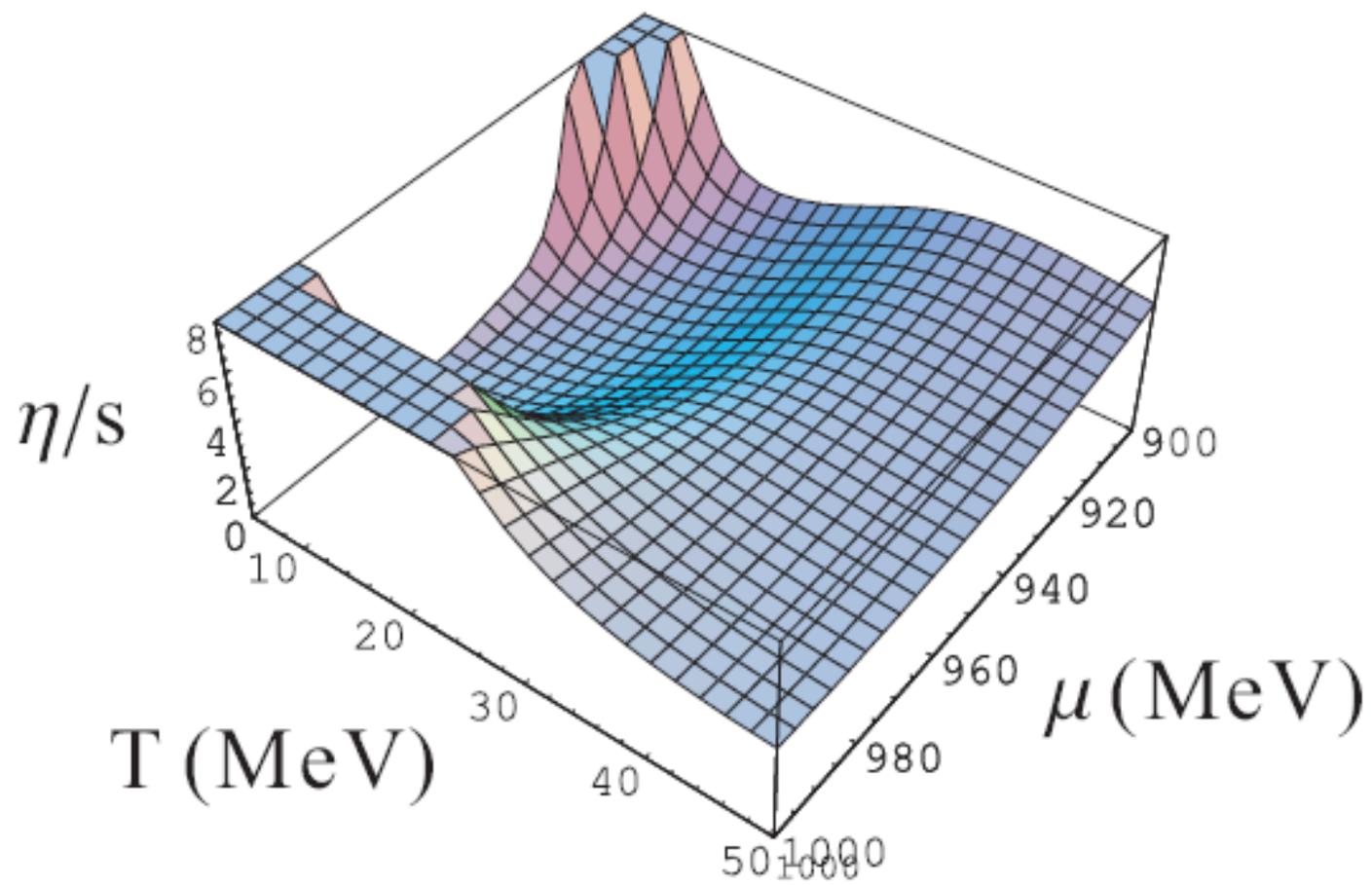
JWC, Li, Liu, Nakano;
Itakura, Morimatsu,
Otomo



The η/s “Landscape”

JWC, Li, Liu, Nakano





QCD Phase Diagram

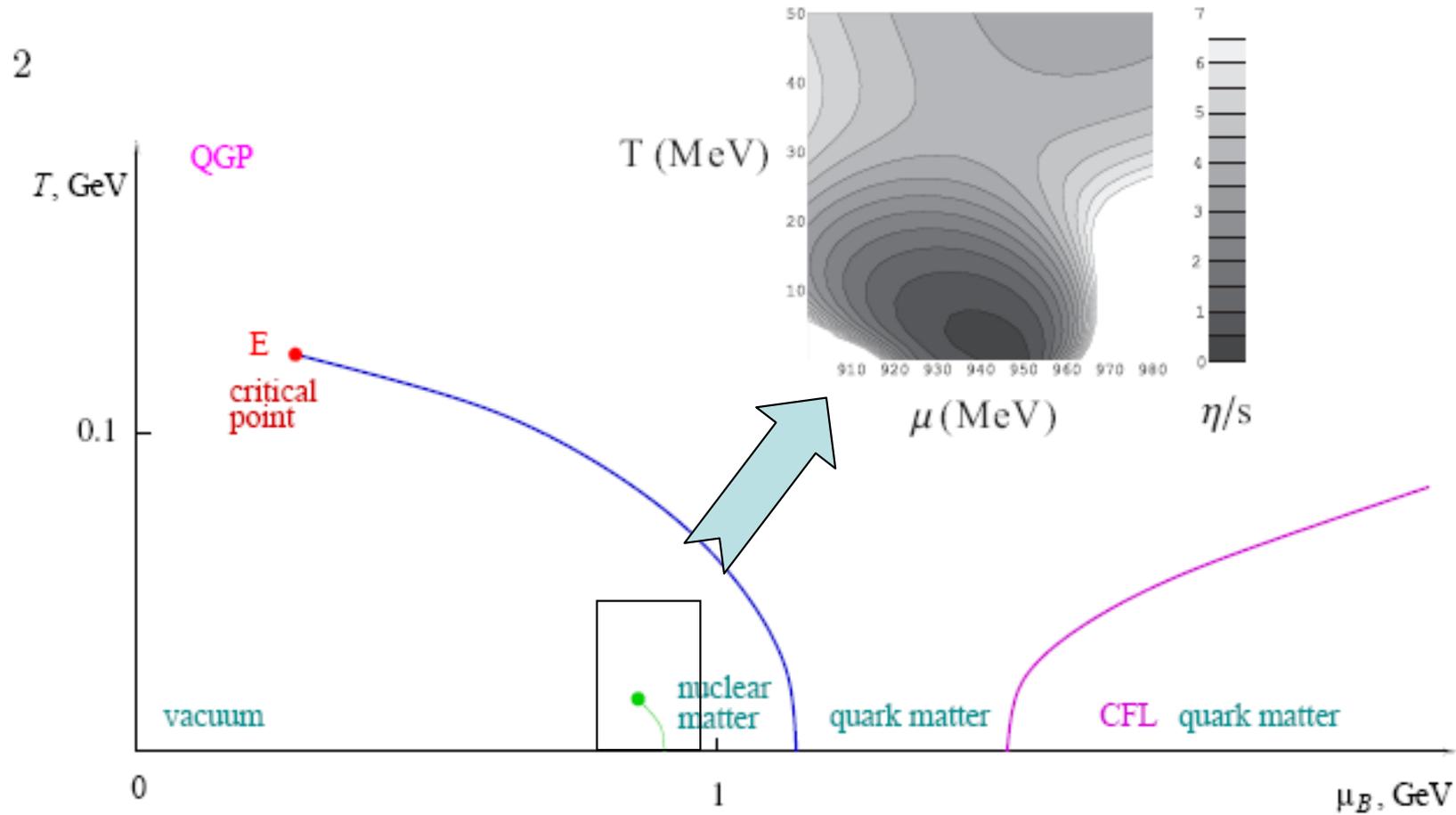
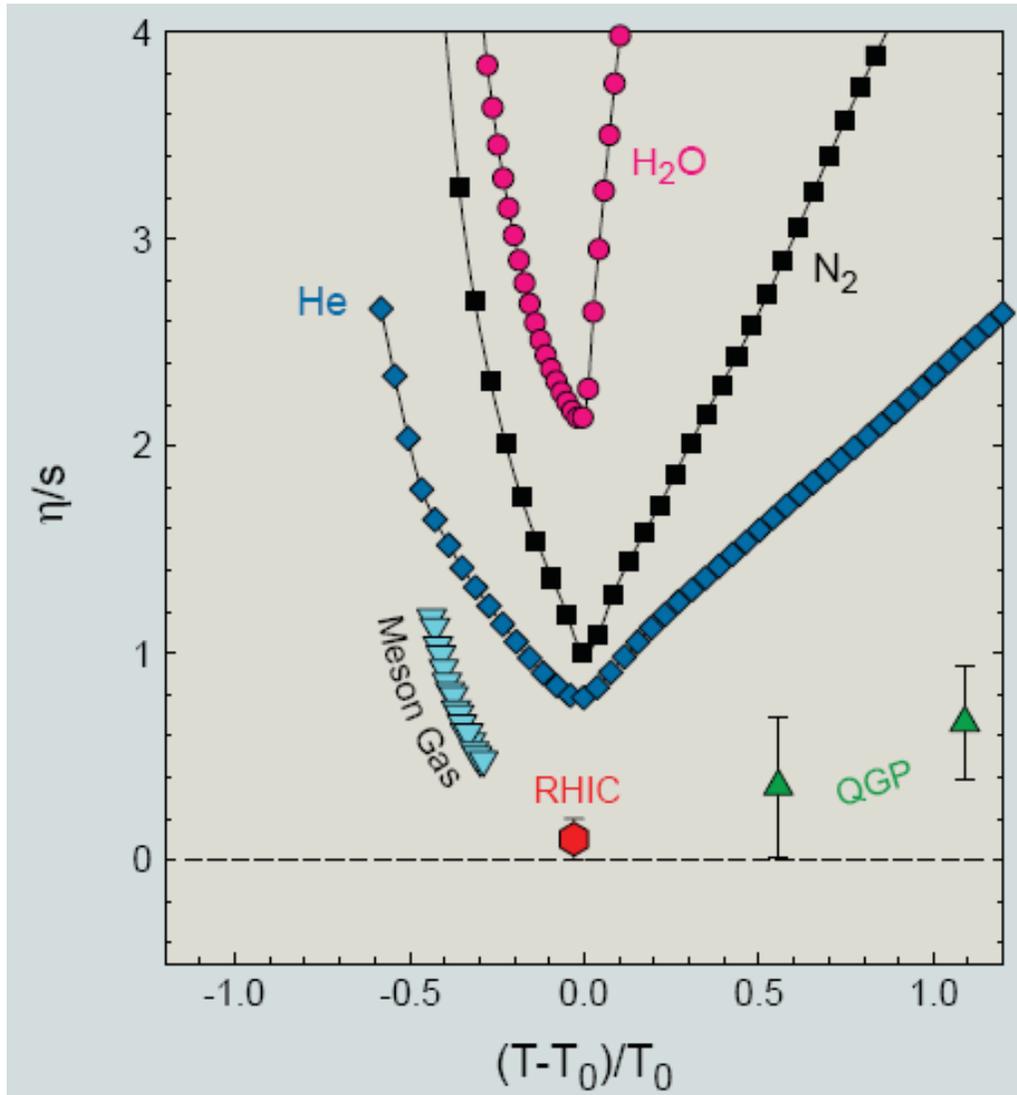
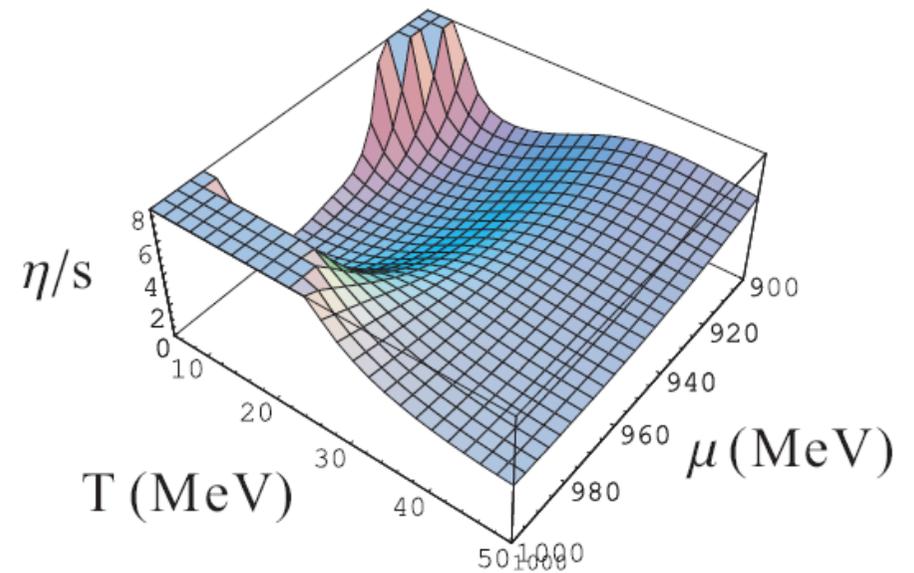
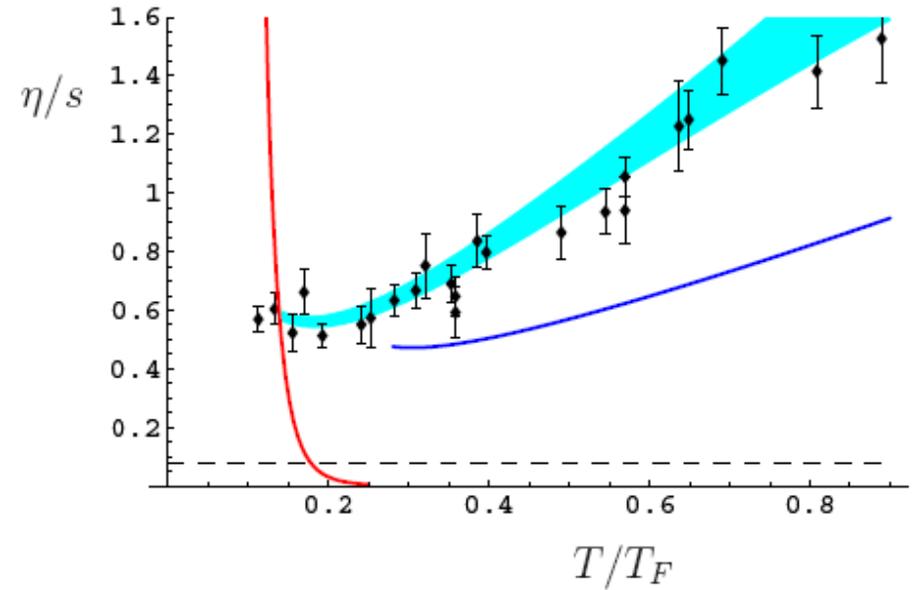


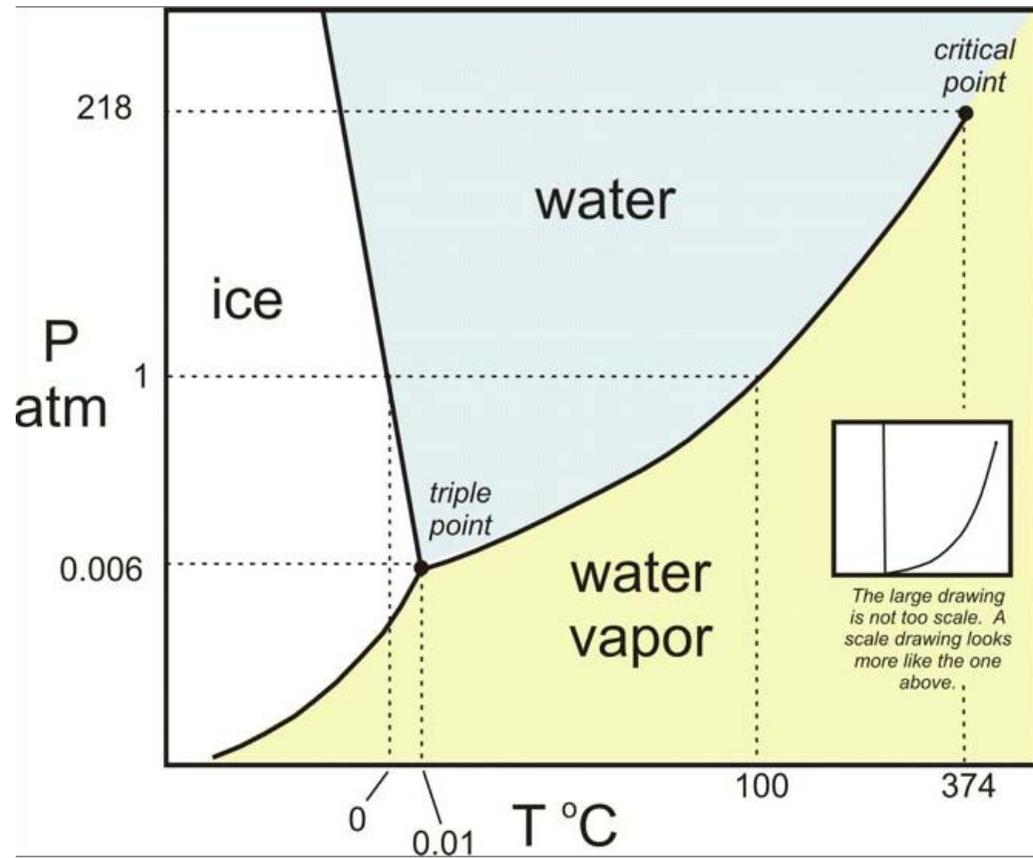
Fig. 1. QCD phase diagram

Cold Unitary Atoms
Rupak & Schafer 2007

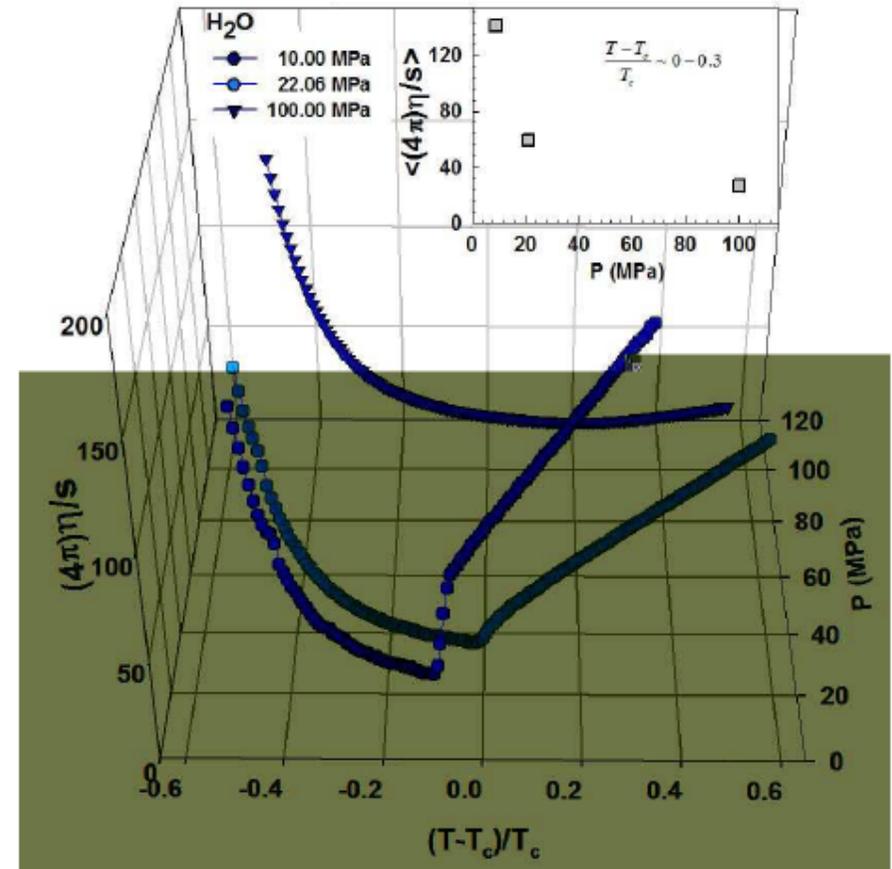


Lacey et al., PRL 98:092301,2007;
2007 US Nuclear Science Long
Range Plan

Water P-T Phase Diagram



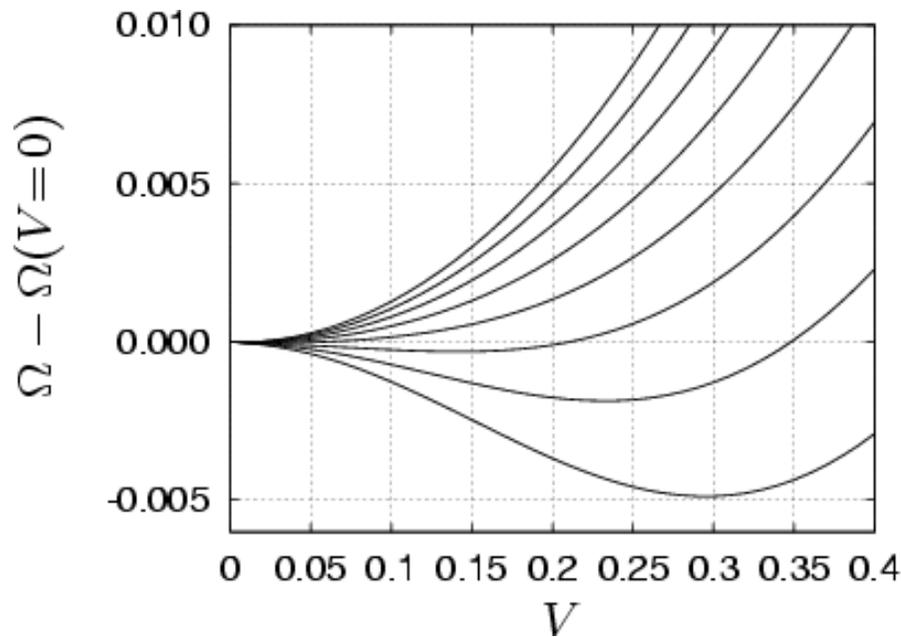
η/s of Water



(Lacey et al.)

$$\mathcal{L} = \frac{1}{2}(\partial_\mu \phi)^2 - \frac{1}{2}a\phi^2 - \frac{1}{4}b\phi^4 - \frac{1}{6}c\phi^6$$

(JWC, M. Huang, Y.H. Li, E. Nakana, D.L. Yang)

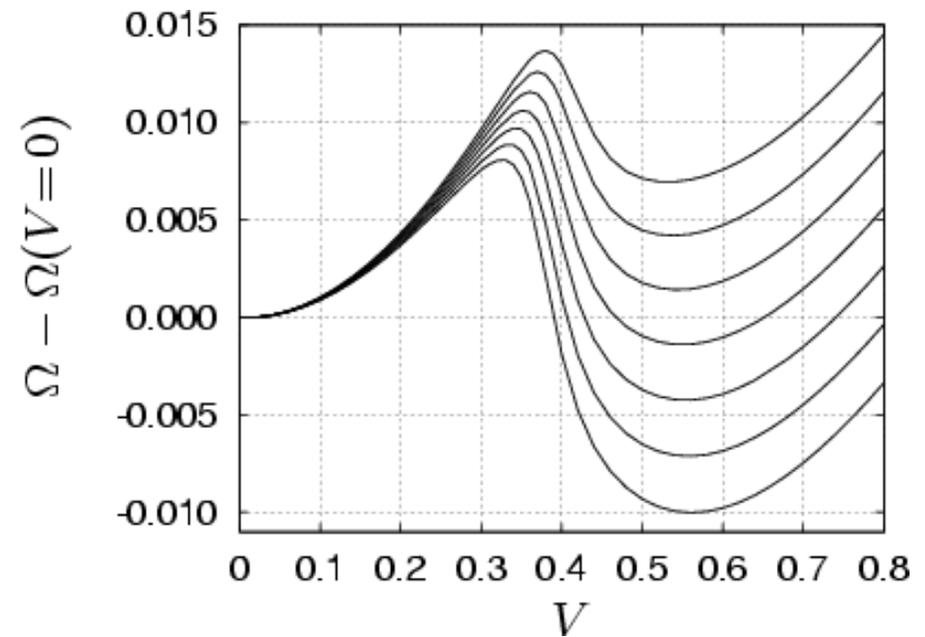


2nd-order p.t.:

$$a < 0, b > 0, c = 0$$

$$\text{crossover: } + \delta\mathcal{L} = H\phi$$

$$\text{No p.t.: } a > 0, b > 0, c = 0$$

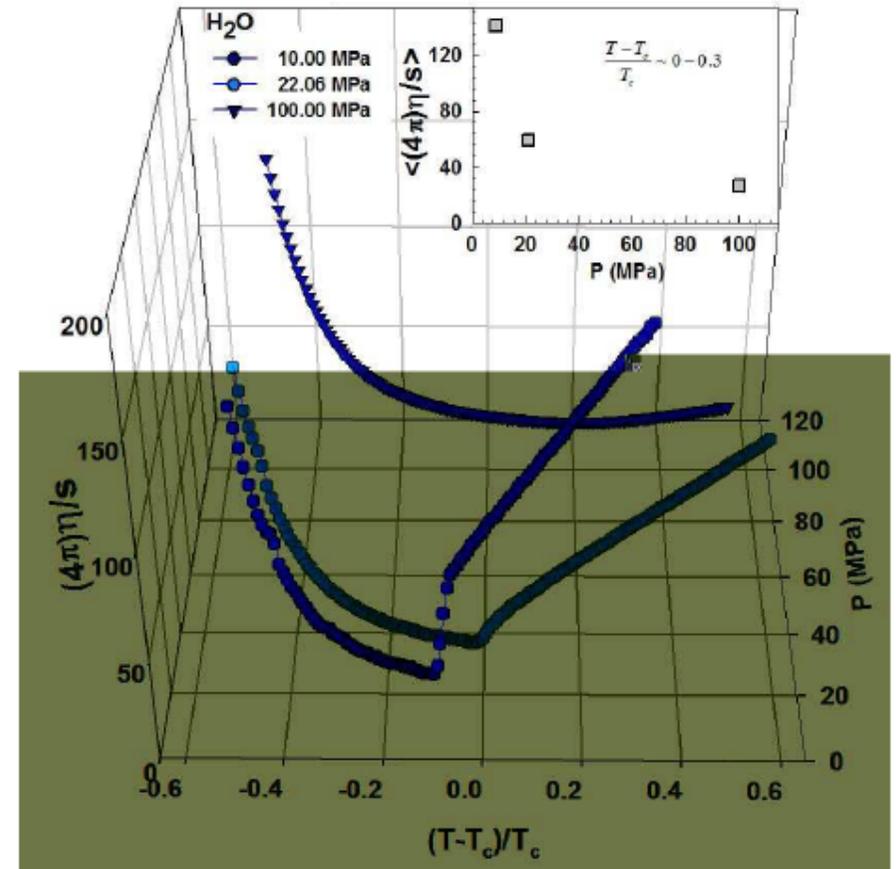
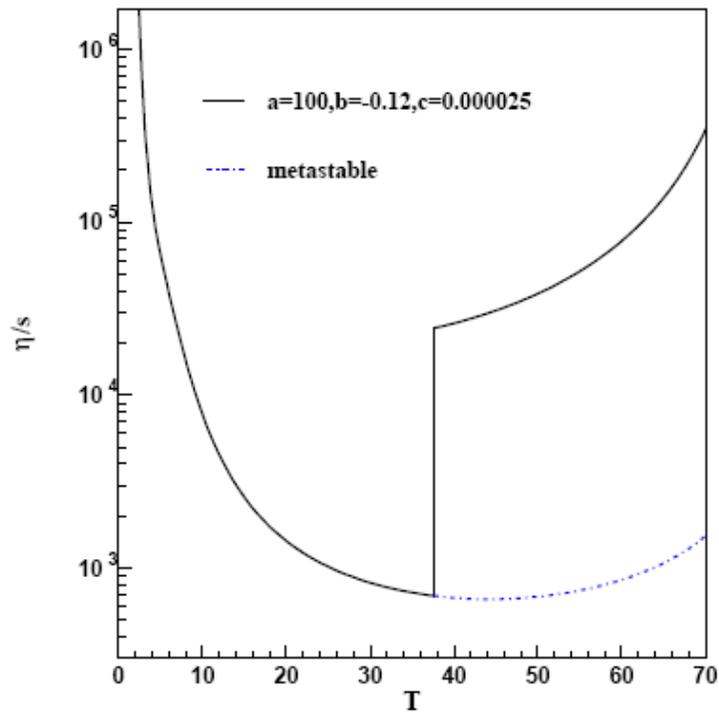
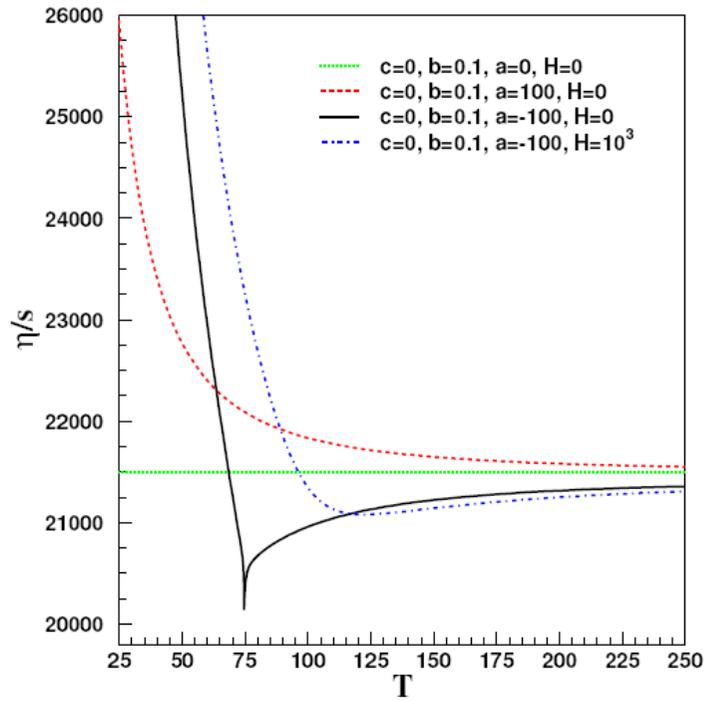


1st-order phase transition

$$a > 0, b < 0, c > 0$$

- Weak coupling, Boltzmann eq.
- Mean field calculation
- CJT formalism (Cornwall, Jackiw, Tomboulis)

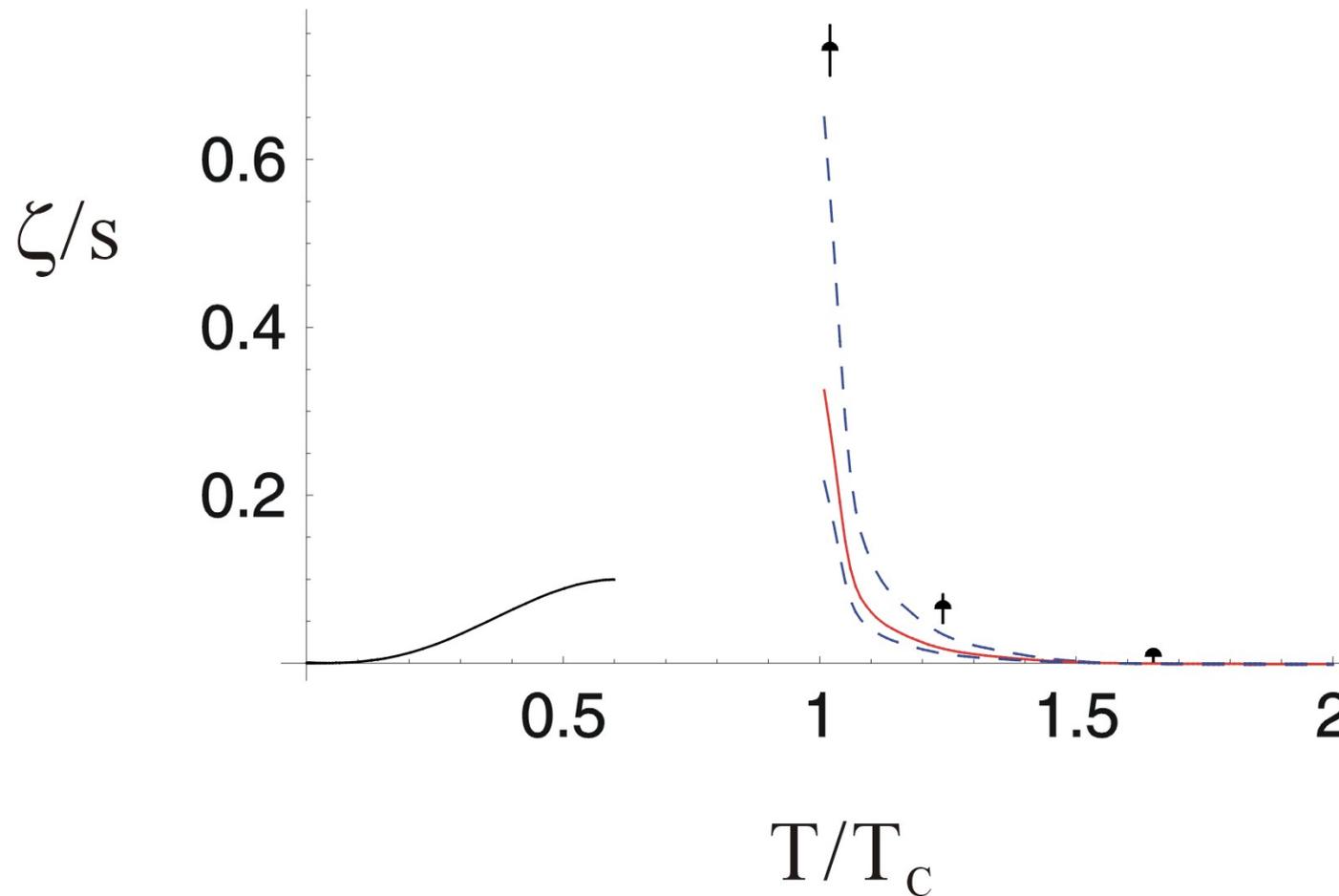
η/s of Water



(Lacey et al.)

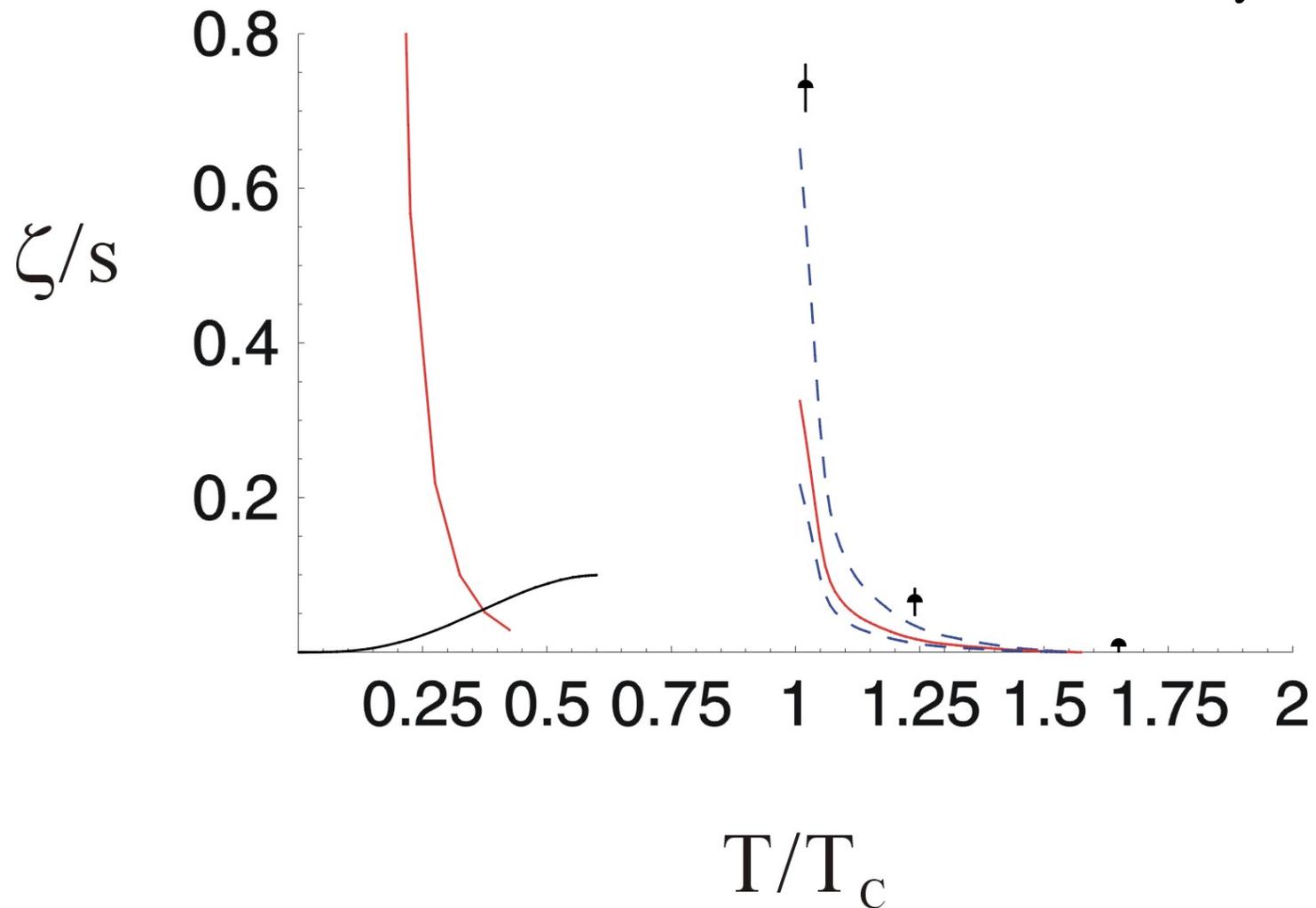
QCD Bulk Viscosity (Chiral Limit)

Karsch, Kharzeev, Tuchin;
Meyer; JWC, Wang

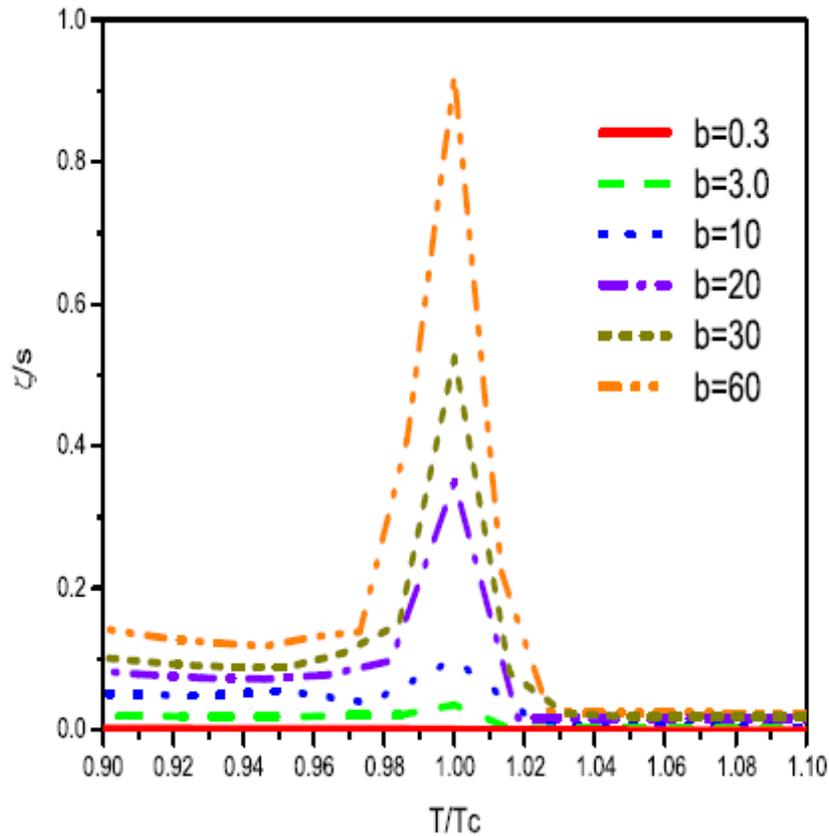


QCD Bulk Viscosity

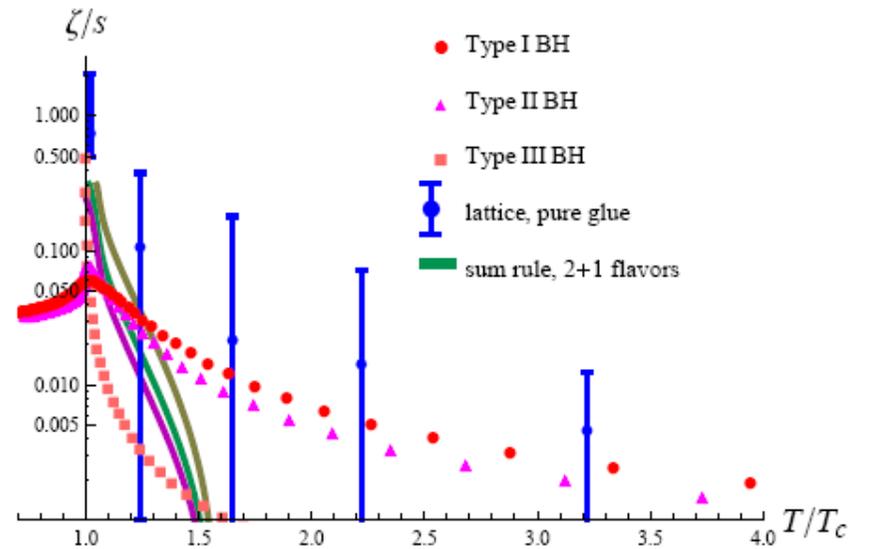
Karsch, Kharzeev, Tuchin;
Meyer; JWC, Wang



Bulk Viscosity



Li, Huang



Gubser, Nellore, Pufu, Rocha

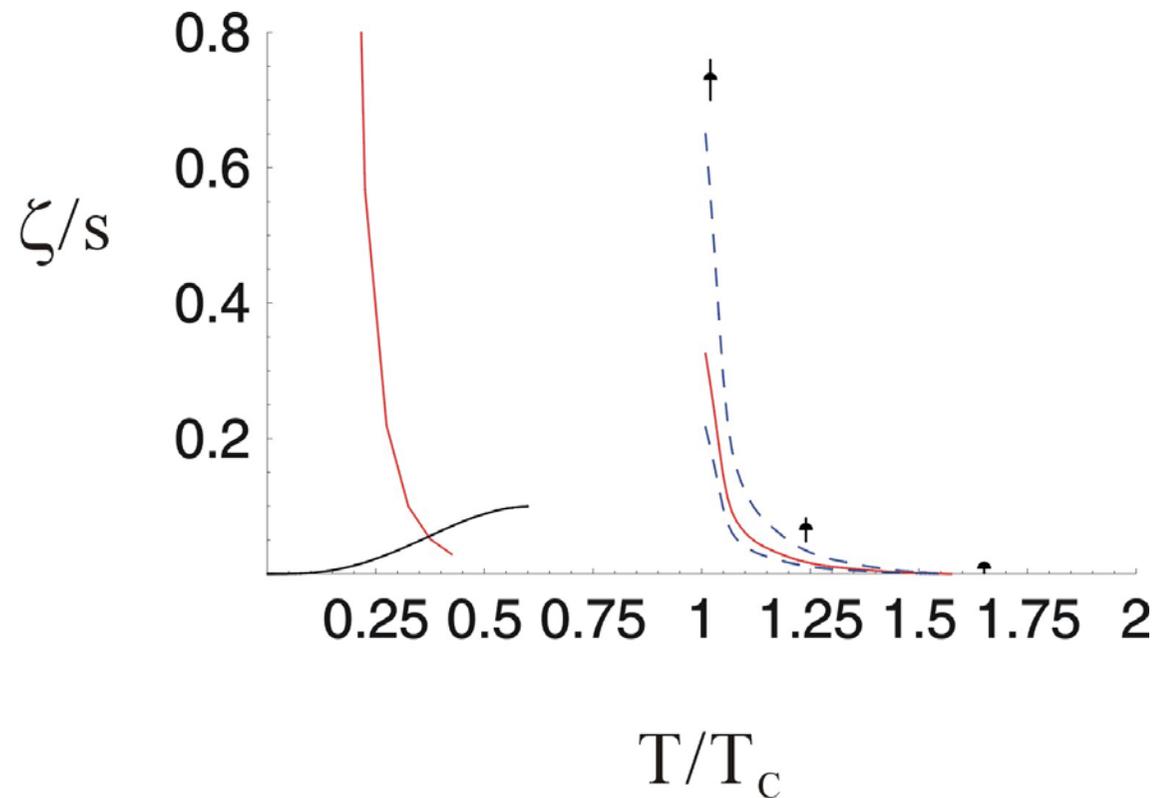
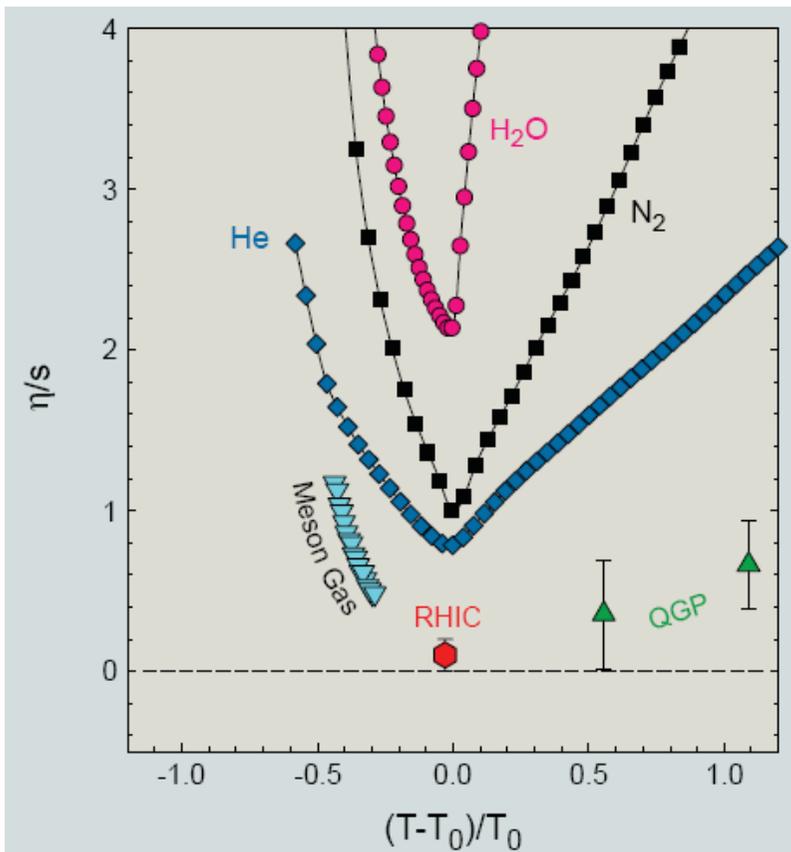
$$\frac{\eta}{s} = \frac{1}{4\pi}$$

Outlook I: Universality?

Universal η/s and ζ/s behaviors?

(η/s reaches local minimum near p.t.

ζ/s reaches local maximum near p.t.)



Mapping QCD phase diagram by η/s ?

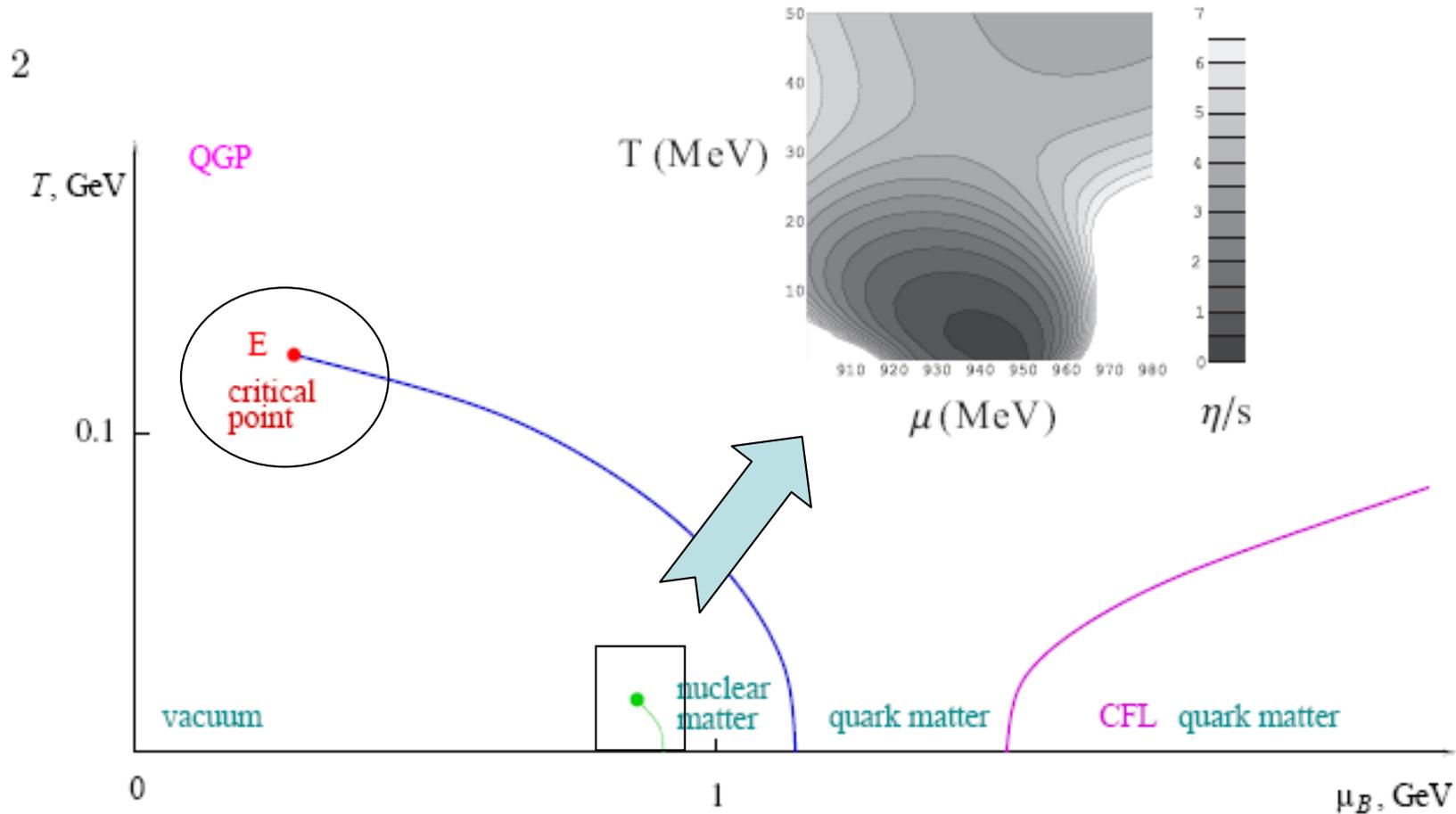


Fig. 1. QCD phase diagram

Locating critical end point (Lacey)

Outlook II: Invading the Bound

Go metastable (T. Cohen)

$$Q\bar{q} \quad N_Q = N, \quad N_{\bar{q}} = 1$$
$$m_Q \propto N, \quad N_c \propto N$$

$$\eta/s \propto 1/\ln N$$

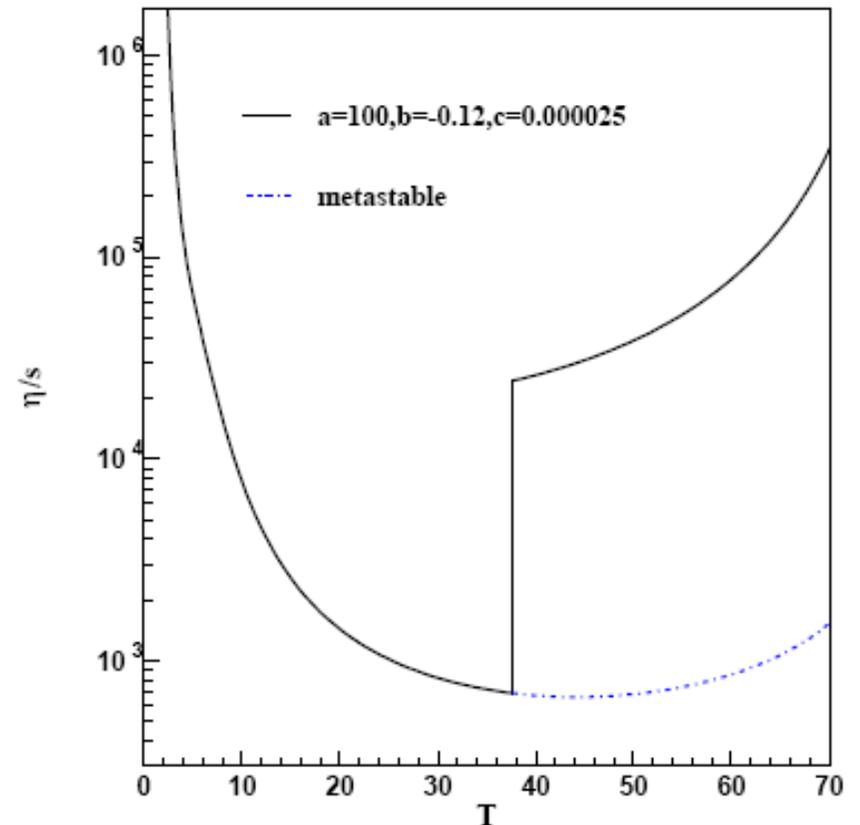
UV complete but metastable

Outlook

Invading the bound

$$Q\bar{q} \quad N_Q$$
$$m_Q$$

$$\eta/s \propto 1/\ln N$$



UV complete but metastable

Go Finite N

- $O(1/N)$ effect, Higher derivative gravity,
(Brigante, Liu, Myers, Shenker, Yaida; Kats, Petrov)

$$\frac{\eta}{s} \geq \frac{16}{25} \left(\frac{1}{4\pi} \right)$$

Outlook III: Cold Atoms

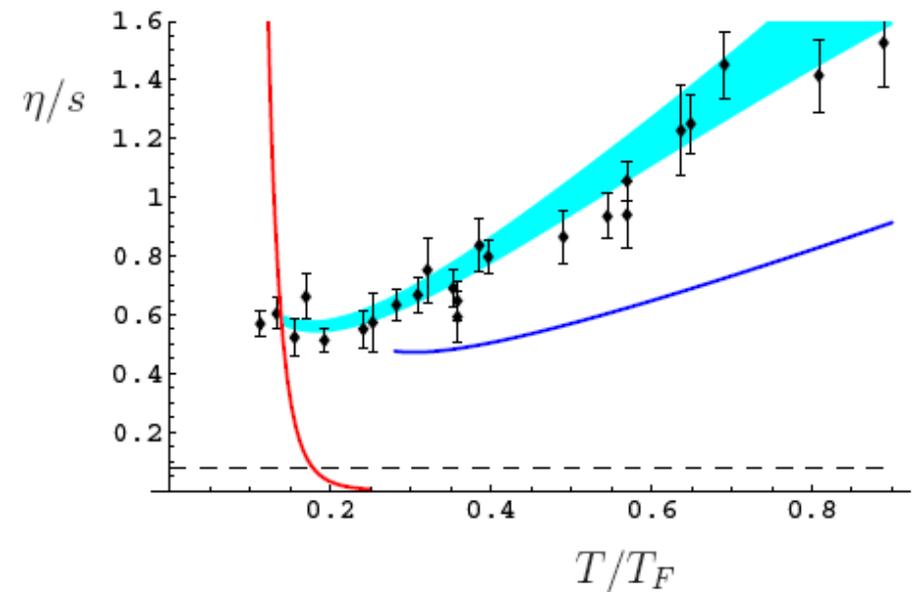
- NR AdS/CFT

Adams, Balasubramanian, McGreevy;
Maldacena, Martelli, Tachikawa;
Herzog, Rangamani, Ross, 2008

$$d = 2 + 1$$

$$\frac{\eta}{s} = \frac{1}{4\pi}$$

Cold Unitary Atoms



Outlook III: Cold Atoms

- NR AdS/CFT

Adams, Balasubramanian, McGreevy;
Maldacena, Martelli, Tachikawa;
Herzog, Rangamani, Ross, 2008

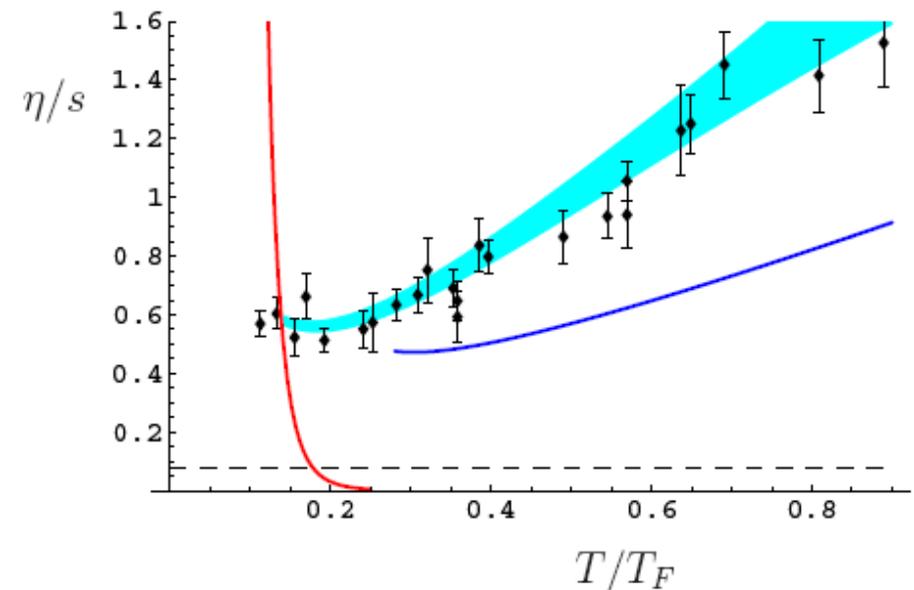
$$d = 2 + 1$$

$$\frac{\eta}{s} = \frac{1}{4\pi}$$

Not for cold atoms at 2+1 d,

where unitary fermi gas is a free gas JWC, Wen, 08

Cold Unitary Atoms



- QCD shear viscosity in the hadronic phase:
 - (a) zero density (w/ Eiji Nakano)
 - (b) nuclear L-G phase transition
(w/ Yen-Fu Liu, Yen-Han Li, Eiji Nakano)
- Scalar field theory (w/ Mei Huang, Yen-Han Li, Eiji Nakano, Di-Lun Yang)
- Bulk Viscosity (w/ Juven Wang)
- Gluon Plasma (w/ Kazuaki Ohnishi, Hui Dong, Qun Wang) Anion (w/ Shu-Ping Lee)

How do we distinguish different phases?

- thermodynamics: different equations of state
 - but often qualitatively different phases have numerically close equations of state. Examples:
 - strongly coupled and weakly coupled $\mathcal{N} = 4$ SYM:
 $s_{\lambda=\infty}/s_{\lambda=0} = 3/4$ (AdS/CFT methods)
 - large baryon density: nuclear matter and quark matter can have similar EoS
- transport coefficients: perturb the system slightly, let it relax to equilibrium
 - viscosity, heat conductivity, diffusion constants
 - in $\mathcal{N} = 4$ SYM, $(\eta/s)_{\lambda=\infty} = 1/4\pi$ vs. $(\eta/s)_{\lambda=0} = \infty$
 - $(\eta/s)_{CFL} \ll (\eta/s)_{nucl. matt.}$