

**Double Higgs production in the CP conserving Two Higgs
Doublet Model**

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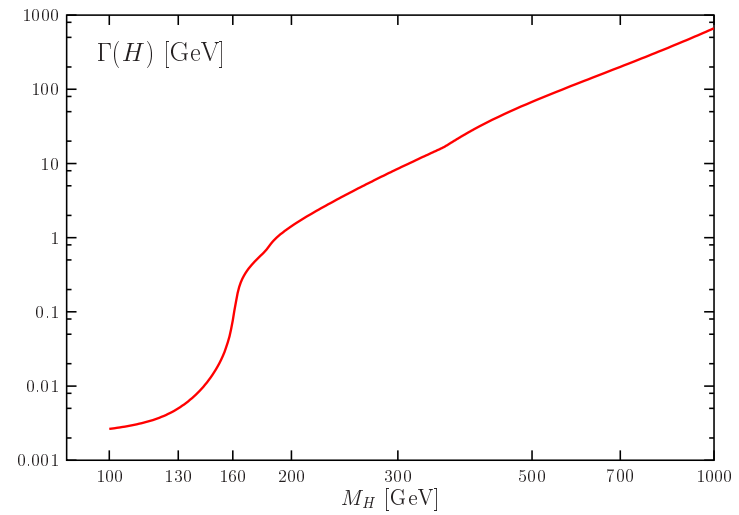
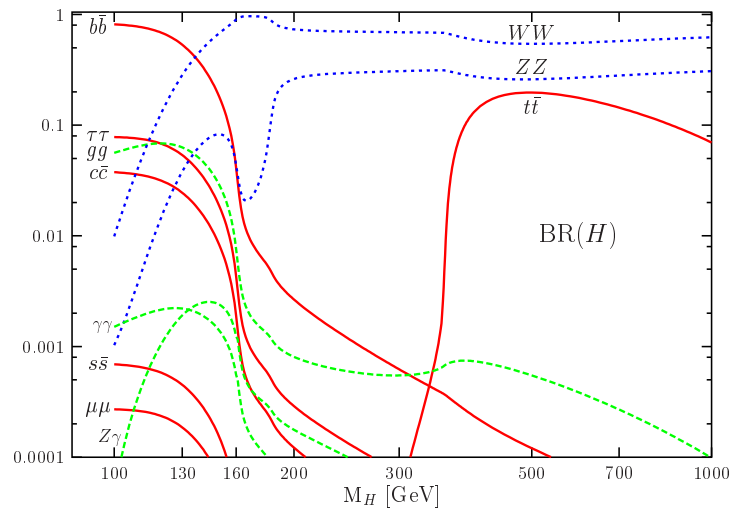
Outline

- Higgs production and decays in SM
- Two Higgs Doublets Models (2HDM) and its Decoupling regime
- Triple Higgs coupling from $h^0 \rightarrow \gamma\gamma$, $h^0 \rightarrow b\bar{b}$
- Triple Higgs couplings from double Higgs production at LHC, ILC and $\gamma\gamma$
- Conclusions

Higgs in SM

- Best fit analysis: $M_H = 84_{-26}^{+34}$ GeV which gives $M_H \lesssim 154$ GeV at 95% CL. (LEP Higgs Working Group).
- LEP II Experiments: $M_H > 114.4$ GeV (LEP),
Tevatron exclude $160 \lesssim M_H \lesssim 170$ GeV from $H \rightarrow WW$ (S. M. Wang Talk).
- Unitarity constraint: $M_H \lesssim 700$ GeV
- Requiring the SM to be extended up to $\Lambda_{GUT} = 10^{16}$ GeV, one can get $130 \lesssim M_H \lesssim 180$ GeV.
- If the $M_H \gtrsim 200$ GeV, then there should be an additional new ingredient that is relevant at the EWSB scale.

Higgs decays



- At hadron colliders (LHC, Tevatron) the relevant processes are:

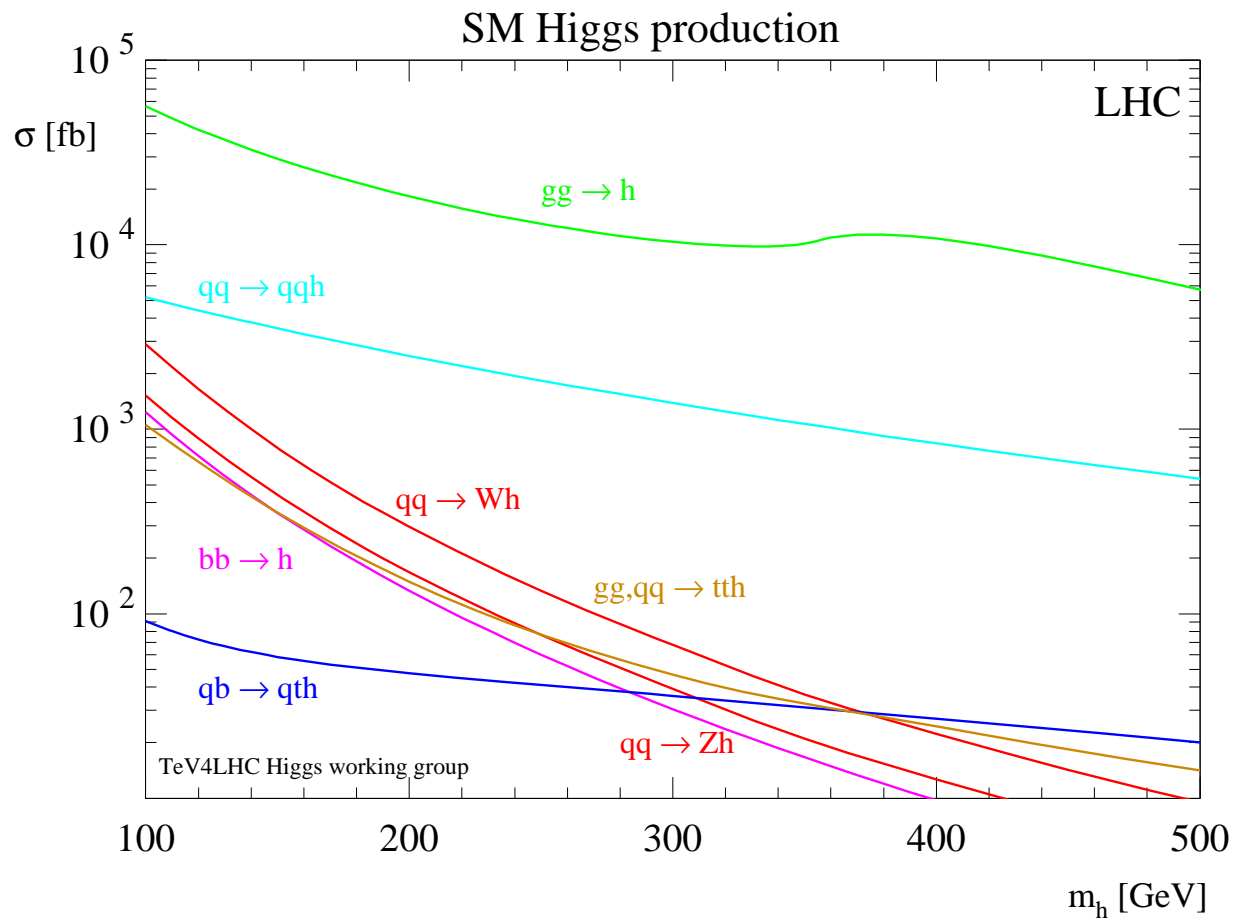
$$gg \rightarrow h_{SM} \rightarrow \gamma\gamma \quad , \quad gg \rightarrow h_{SM} \rightarrow VV^*$$

$$qq \rightarrow qqV^*V^* \rightarrow qqh_{SM} \quad , \quad h_{SM} \rightarrow \gamma\gamma, \tau^+\tau^-, VV^*$$

$$gg, qq \rightarrow t\bar{t}h_{SM} \quad , \quad h_{SM} \rightarrow b\bar{b}, WW^*, WW^*$$

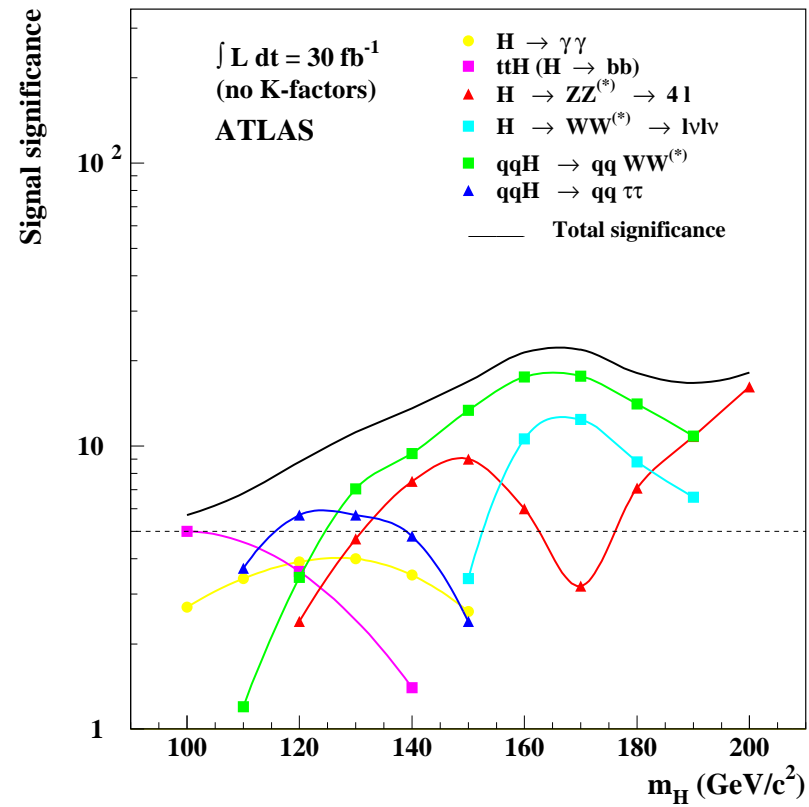
$$qq \rightarrow h_{SM}Z \quad , \quad qq' \rightarrow h_{SM}W \quad , \quad h_{SM} \rightarrow b\bar{b}(\text{Tevatron})$$

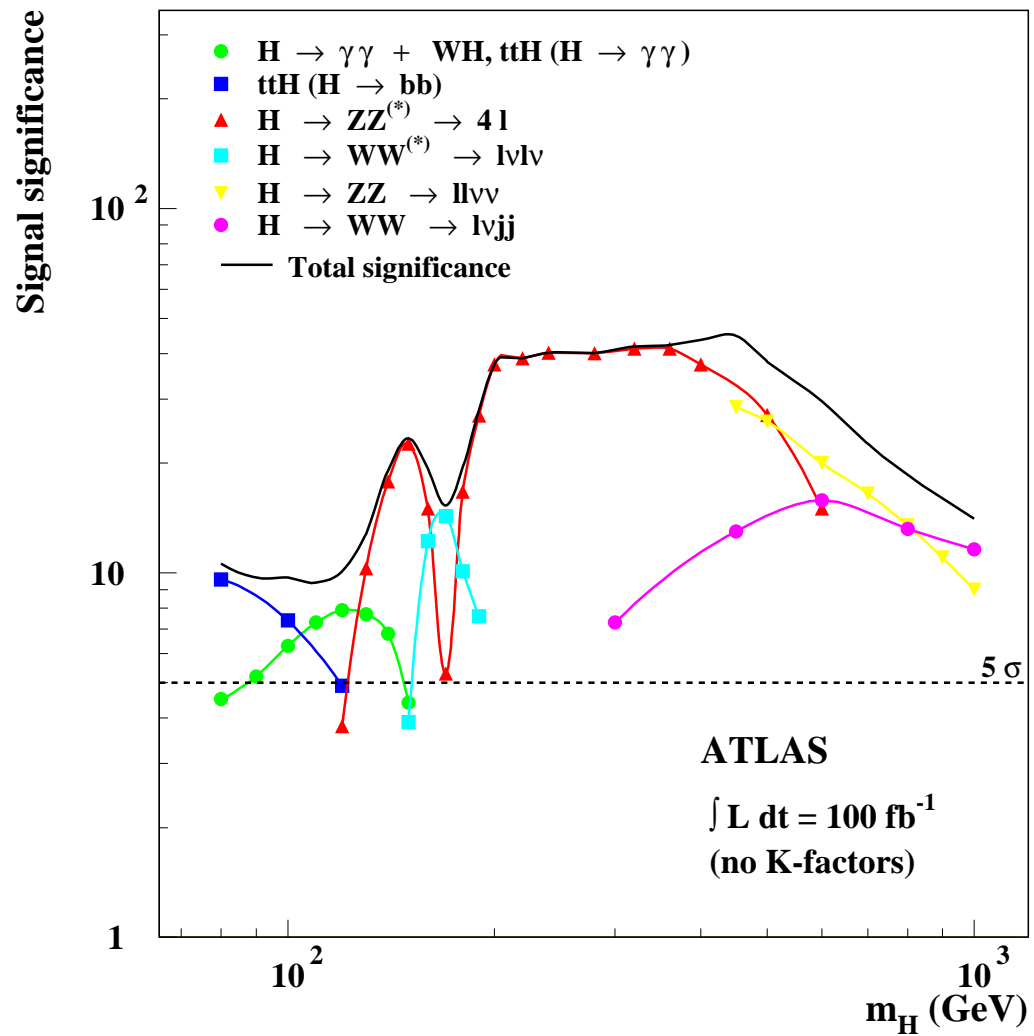
$$gg \rightarrow h_{SM}h_{SM}(\text{double Higgs production})$$



Significance for the experimental detection

Low luminosity





Extended Higgs sector

- With **Extended Higgs sector: 2HDM Φ_1 , Φ_2** , CP can be violated either **explicitly** or **spontaneously** in Higgs sector **T.D.Lee'73**
- Some models of **dynamical electroweak symmetry breaking** yields the 2HDM as their low-energy effective theory. [**H. J. He et al, PRD65, (2002) hep-ph/0108041**].
- Models for phase transition requires 2 Higgs doublets
- Neutrino masses, Dark Matter, BAU
Zee'80, Ma'06, S. Kanemura and C.S Chen talks

Coupling to fermions

- both Φ_1 and Φ_2 couple to fermions: $M_q = Y^u v_1 + Y^d v_2$:
diagonalisation of M_q does not diagonalise simultaneously $Y^{u,d}$:
FCNC at tree level: 2HDM-III
- 2HDM-I One doublet couple to gauge boson and the other one couple to fermion (like in SM).
- To avoid FCNC at tree level, We impose Z_2 symmetry (Weinberg Theorem): $\Phi_2 \rightarrow -\Phi_2$, $d_{iR} \rightarrow -d_{iR}$: 2HDM-II
- 2HDM-X or lepton-specific 2HDM (or Leptophilic Higgs): one doublet generates the masses of the charged leptons and the second one generates the masses of the quarks
Barnet, Senjanovic, Wolfenstein and Wyler'84, S.Su et al, H.Logan et al, M. Aoki et al'09

$$\begin{aligned}
V = & \mu_1^2(\Phi_1^+\Phi_1) + \mu_2^2(\Phi_2^+\Phi_2) + \lambda_1(\Phi_1^+\Phi_1)^2 + \\
& \lambda_2(\Phi_2^+\Phi_2)^2 + \lambda_3(\Phi_1^+\Phi_1)(\Phi_2^+\Phi_2) + \lambda_4|\Phi_1^+\Phi_2|^2 \\
& + \{m_{12}^2(\Phi_1^+\Phi_2) + h.c\} + [\lambda_5(\Phi_1^+\Phi_2)^2 + h.c]
\end{aligned}$$

- One can have: **Explicit CP** if $\Im(m_{12}^4\lambda_5^*) \neq 0$;
- One can have **Spontaneous CP** if: $|\frac{m_{12}^2}{\lambda_5 v_1 v_2}| < 1$; $\langle \Phi_1 \rangle = v_1$,
 $\langle \Phi_2 \rangle = v_2 e^{i\theta}$
- Five physical scalars (8 d.o.f=5+3): **a charged Higgs pair H^\pm , two CP-even h^0, H^0 and one CP-odd A^0**
- $m_A, m_h, m_H, m_{H^\pm}, \alpha, \tan \beta = v_1/v_2$ and m_{12}^2 free parameters.

Theoretical constraints:

- $b \rightarrow s\gamma$: $m_{H^\pm} > 295 \text{ GeV}$, $\forall \tan \beta$ in 2HDM-II. No such bound in 2HDM-I [P.Gambino et al, '01, F.Borzumati et al '98].
In 2HDM-X, light H^\pm is allowed Aoki et al, Logan et al'09
- $\delta\rho \leq 10^{-3}$ [(PDG)]: constrain the splitting M_A and M_{H^\pm}
- Perturbativity on λ_i : $|\lambda_i| \leq 8\pi$
- **Potential bounded from below**: $\lambda_{1,2} > 0$, $\sqrt{\lambda_1\lambda_2} \geq \lambda_3 + \lambda_4 + \lambda_5$
- Unitarity constraints: in 2HDM there is 14 constraints coming from different channel: W^+W^- , ZZ , hh , HH , hH , AA , hA , H^+H^- , hH^+ ... [S. Kanemura et al '98, A.Akeroyd et al '00]

The decoupling limit of 2HDM

- $\cos(\alpha - \beta) \rightarrow 0$ and $m_{\Phi} = m_{H, H^{\pm}, A} \gg m_Z$:
- The effective theory below M_{Φ} is described by one Higgs doublet.
- In this limit:

$$h^0 VV / (h_{SM} VV) = \sin(\beta - \alpha) \rightarrow 1$$

$$h^0 b\bar{b} / h_{SM} b\bar{b} = -\frac{\sin \alpha}{\cos \beta} \rightarrow 1, \quad (h^0 t\bar{t}) / h_{SM} t\bar{t} = \frac{\cos \alpha}{\sin \beta} \rightarrow 1$$

$$H^0 VV \propto \cos(\beta - \alpha) \rightarrow 0, \quad (hhh) / (hhh)_{SM} \rightarrow 1$$

$$h^0 H^+ H^-, h^0 A^0 A^0, h^0 H^0 H^0, H^{\pm} t\bar{b} \dots \neq 0$$

- In the decoupling regime, only one Higgs h may be produced.
In this case, how to disentangle h from SM Higgs?

A program of precision measurements will begin at LHC and will reach maturity at the ILC :

$$\delta(\Gamma_W)/\Gamma_W \approx 5 - 10\% , \quad \delta(\Gamma_\tau)/\Gamma_\tau = \delta(\Gamma_\gamma)/\Gamma_\gamma \approx 18\% \text{ at LHC}$$

At Linear Collider(ILC), the situation is much better:

Relative accuracies (in %) on M_H and couplings at ILC $\sqrt{s} = 500$ GeV and $\int \mathcal{L} = 500 \text{ fb}^{-1}$ [[hep-ph 0106315](#)]

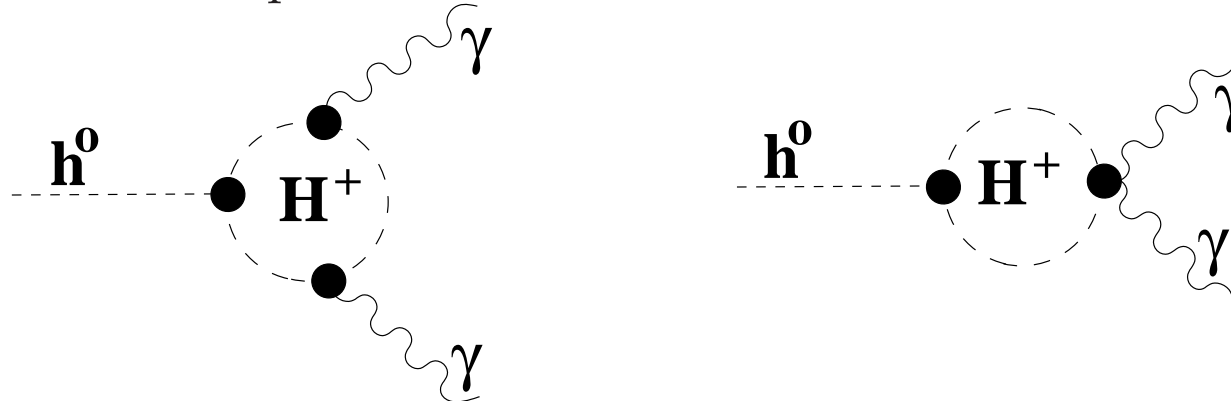
M_H	ΔM_H	g_{HWW}	g_{HZZ}	g_{Htt}	g_{Hbb}	$g_{H\tau\tau}$
120	± 0.033	± 1.2	± 1.2	± 3.0	± 2.2	± 3.3

In $\gamma\gamma$ option of ILC: $\delta\Gamma(H \rightarrow \gamma\gamma)/\Gamma(H \rightarrow \gamma\gamma) \approx 2\%$ can be achieved (from $\gamma\gamma \rightarrow H \rightarrow b\bar{b}$).

Non decoupling effects in Higgs decays

A.A, W.Hollik and S.Penaranda PLB'04

- $h^0 \rightarrow \gamma\gamma$ is loop-mediated processes since the photon does not couple to neutral particles

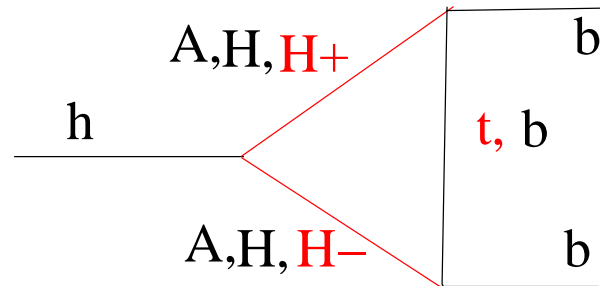


- The only pure **2HDM** contribution comes from charged Higgs loops (if $\alpha = \beta - \pi/2$): $h^0 t\bar{t} \approx \frac{c_\alpha}{s_\beta} \approx 1\dots$

$$g[h^0 H^+ H^-] \approx -\frac{g}{2M_W} \{M_{h^0}^2 + 2(M_{H^\pm}^2 - M_{12}^2)\}$$

The decoupling is achieved when $M_{12} \rightarrow \infty$

- $h_0 \rightarrow b\bar{b}$, already exists at the tree level because of the Higgs- b Yukawa interaction
- Pure **2HDM** one-loop contributions not present in the **SM** case:



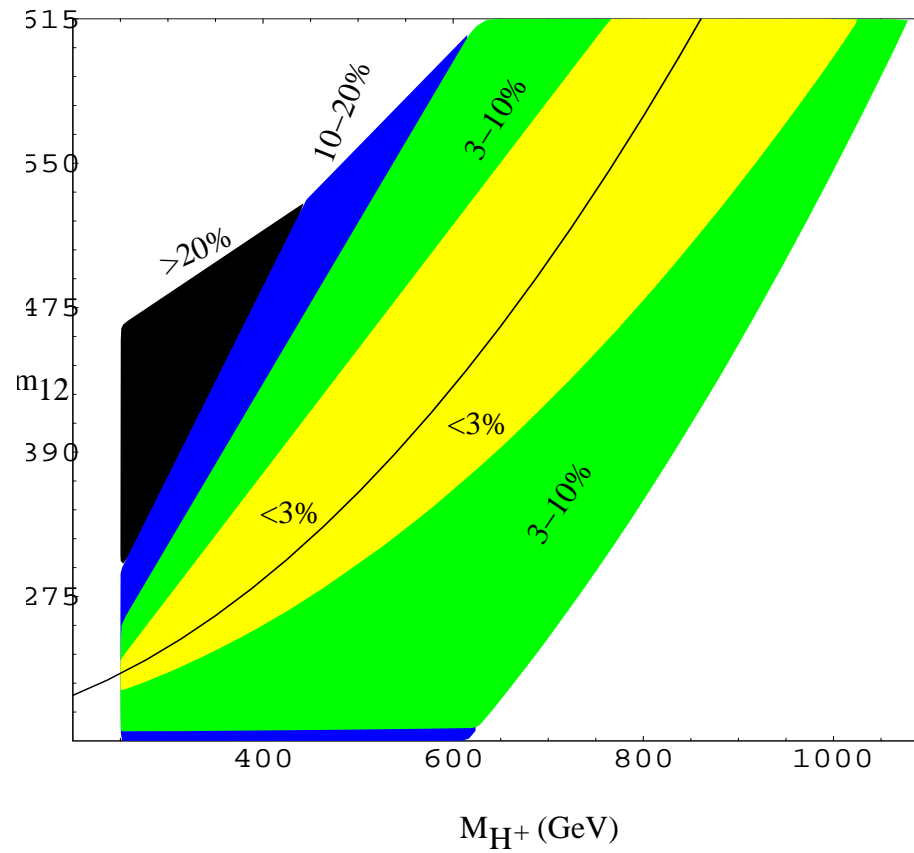
$\alpha \rightarrow \beta - \pi/2 \Rightarrow$ only $h^0 H^+ H^-$, $h^0 H^0 H^0$ and $h^0 A^0 A^0$ don't vanish or reduce to their **SM** values

$$g[h^0 H^+ H^-] \approx -\frac{g}{2M_W} \{M_{h^0}^2 + 2(M_{H^\pm}^2 - M_{12}^2)\}$$

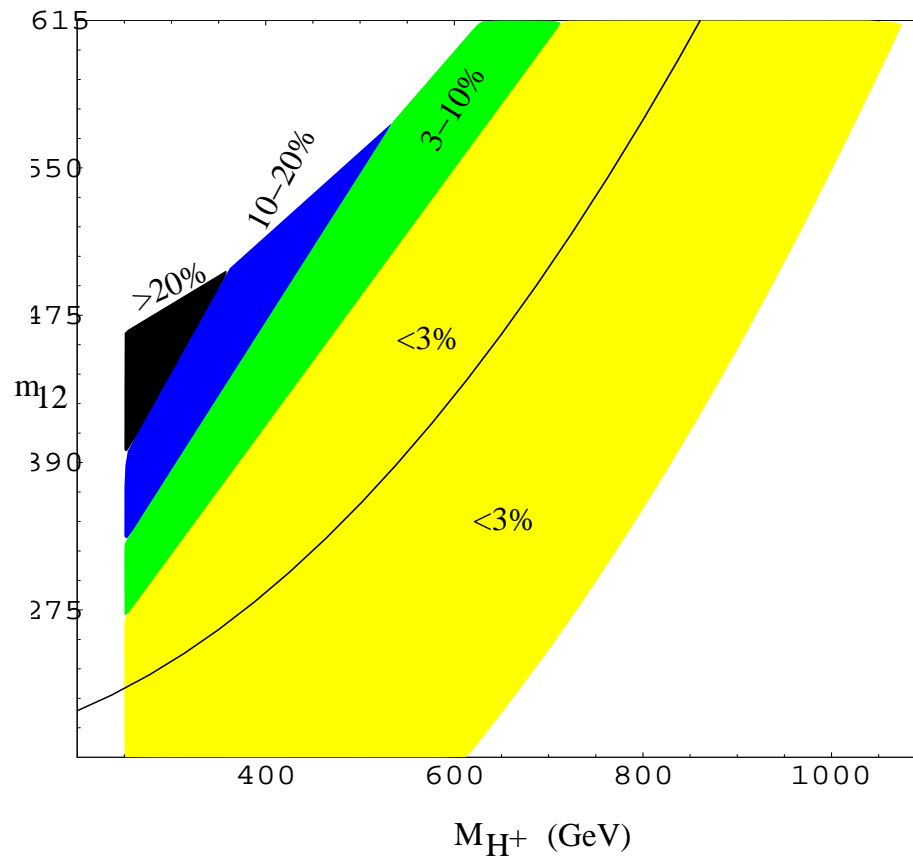
$$g[h^0 H^0 H^0] \approx -\frac{g}{2M_W} \{M_{h^0}^2 + 2(M_{H^0}^2 - M_{12}^2)\}$$

$$g[h^0 A^0 A^0] \approx -\frac{g}{2M_W} \{M_{h^0}^2 + 2(M_{A^0}^2 - M_{12}^2)\}$$

$$h^0 \rightarrow \gamma\gamma: \Delta_{\gamma\gamma} = \left| \frac{\Gamma(h \rightarrow \gamma\gamma)^{2HDM} - \Gamma(h \rightarrow \gamma\gamma)^{SM}}{\Gamma(h \rightarrow \gamma\gamma)^{SM}} \right|$$



$$h \rightarrow b\bar{b}: \Delta_{bb} = \left| \frac{\Gamma(h \rightarrow b\bar{b})^{2HDM} - \Gamma(h \rightarrow b\bar{b})^{SM}}{\Gamma(h \rightarrow b\bar{b})^{SM}} \right|$$

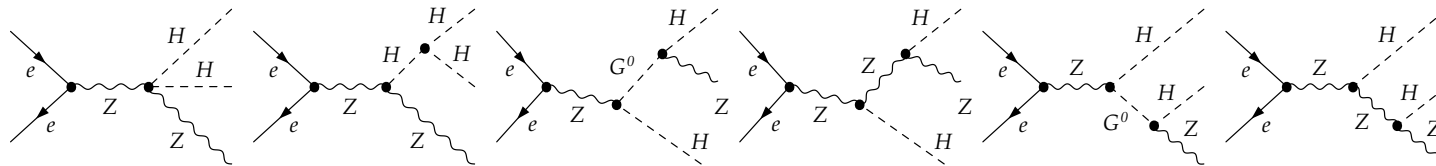


1. Probing triple Higgs couplings in the 2HDM at e^+e^- collider

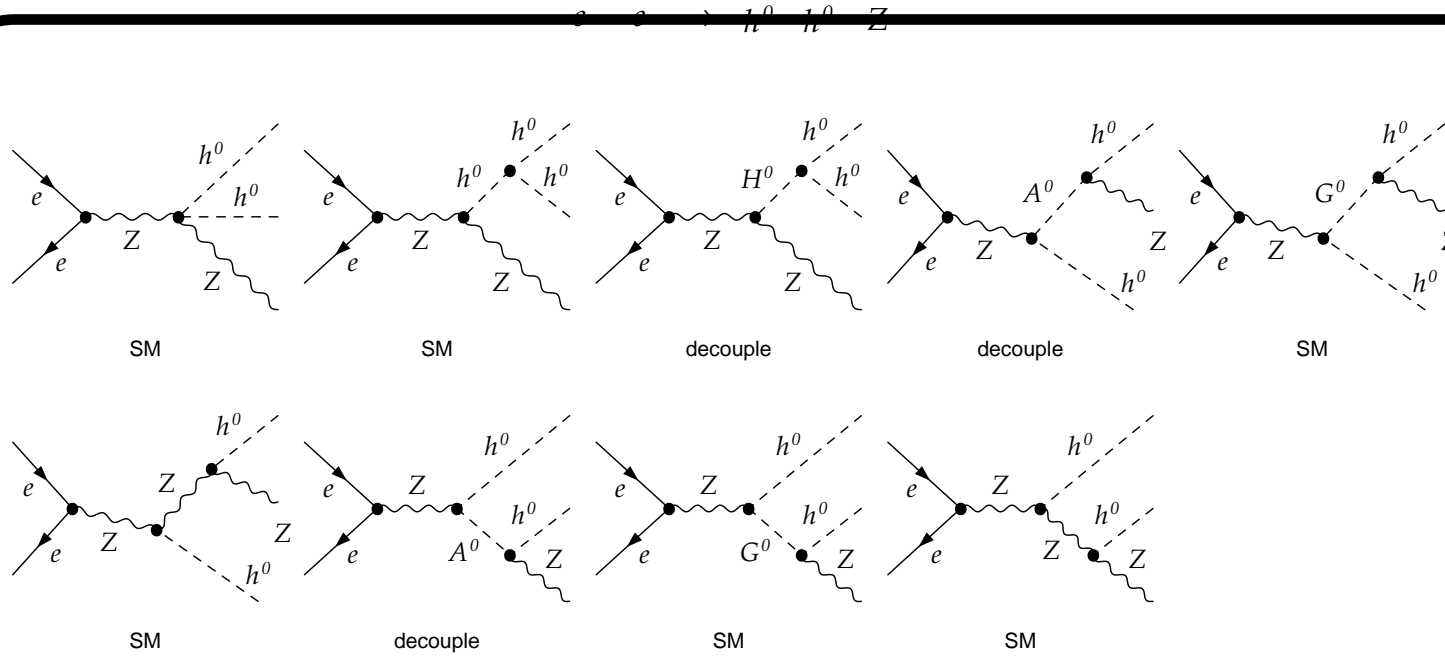
A.A, R.Benbrik and C.W. Chiang'08

- If the Higgs exist, it will be produced either at Tevatron-II or LHC.
- In order to establish the Higgs mechanism, we need to measure the Higgs couplings to fermions, to gauge boson as well as the self-interaction of Higgs bosons.
- Complementarity of LHC/ILC [G. Weiglein et al, “Physics interplay of the LHC and the ILC,” Phys. Rept'06, hep-ph/0410364]
- SM scalar potential can be reconstructed by measuring the triple coupling λ_{hhh} and quartic coupling λ_{hhhh} .
- One can access to λ_{hhh} at ILC from $e^+e^- \rightarrow Zhh$

$e^+e^- \rightarrow Zhh$ in SM



- In SM, $\sigma(e^+e^- \rightarrow Zhh)$ is rather small, for $\sqrt{s}, m_H = 500, 120$ GeV, $\sigma(e^+e^- \rightarrow Zhh) = 0.2$ fb
- possible to extract a signal from EW and QCD background $e^+e^- \rightarrow Zbb\bar{b}\bar{b}$ by simple kinematics cuts: e.g, invariant masses...
Much more events are possible if: [[D.Miller et al hep-ph/9906395](#)]
 - Very high luminosity
 - Excellent b tagging
 - Beam polarization.



In 2HDM we are sensitive to:

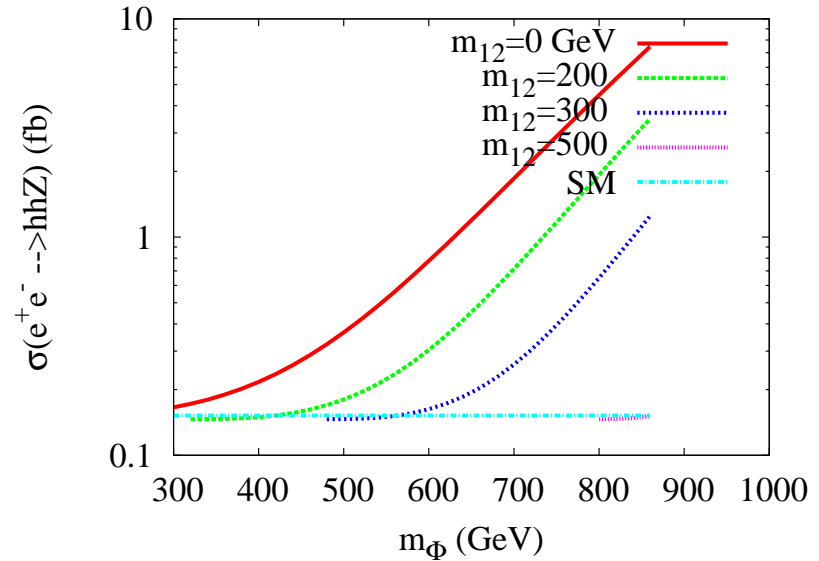
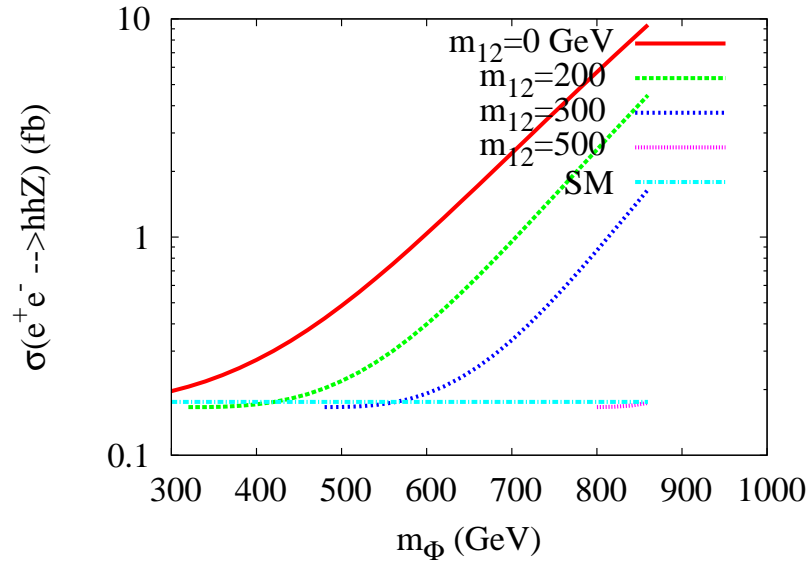
$$hhh = \frac{-3e}{m_W s_W s_{2\beta}^2} \left[(c_\beta c_\alpha^3 - s_\beta s_\alpha^3) s_{2\beta} m_{h^0}^2 - c_{\beta-\alpha}^2 c_{\beta+\alpha} m_{12}^2 \right]$$

$$Hhh = -\frac{1}{2} \frac{e c_{\beta-\alpha}}{m_W s_W s_{2\beta}^2} \left[(2m_{h^0}^2 + m_{H^0}^2) s_{2\alpha} s_{2\beta} - (3s_{2\alpha} - s_{2\beta}) m_{12}^2 \right]$$

$e^+e^- \rightarrow Zhh$ in the decoupling limit: $m_\Phi = m_H = m_A = m_{H\pm}$

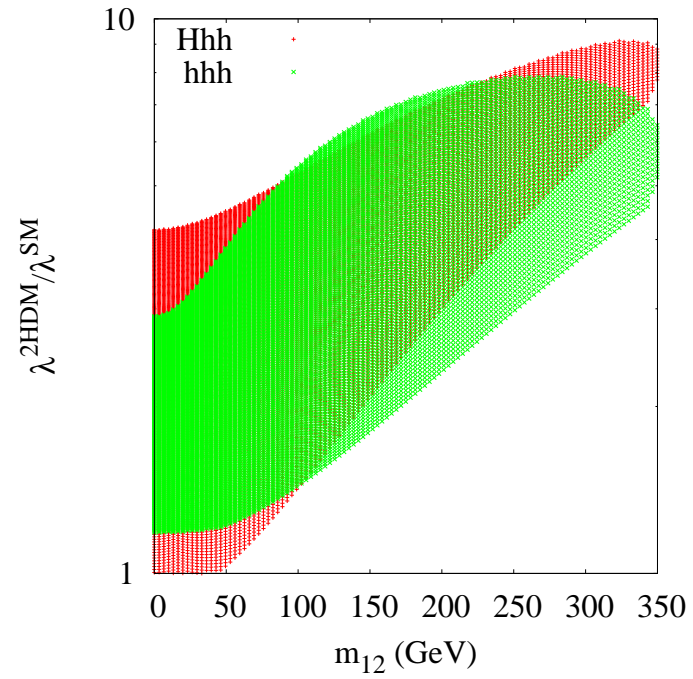
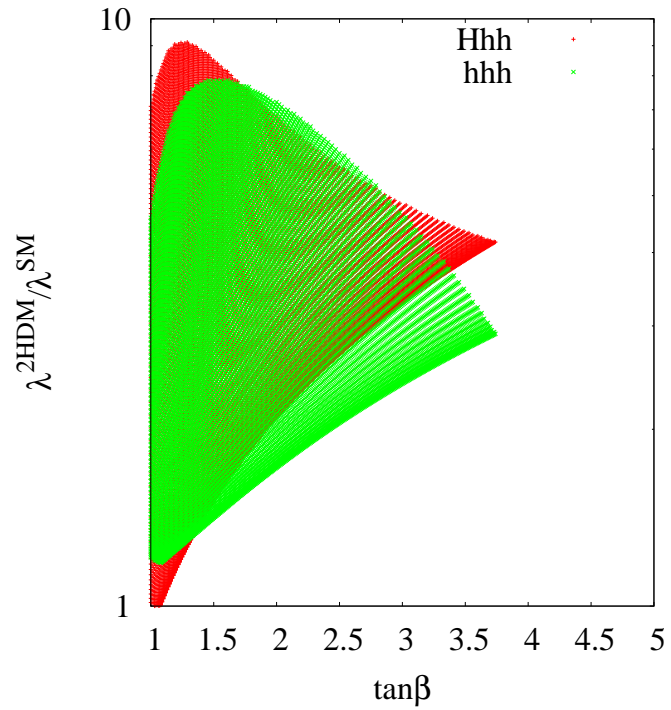
$$hhh_{eff} = \frac{3M_h^2}{v} \left\{ 1 + \frac{m_\Phi^4}{3\pi^2 m_h^2 v^2} \left(1 - \frac{m_{12}^2}{\sin^2 \beta \cos^2 \beta m_\Phi^2} \right)^3 - \frac{N_{ct} m_t^4}{3\pi^2 m_h^2 v^2} \right\},$$

S.Kanemura, E.Senaha, Y.Okada, C.P.Yuan PLB'02



$m_h = 120$ GeV, $\sqrt{s} = 500$ GeV (left) and $\sqrt{s} = 800$ GeV (right).

Away from decoupling limit one can reach 100 fb for $Z\Phi_i\Phi_j$.



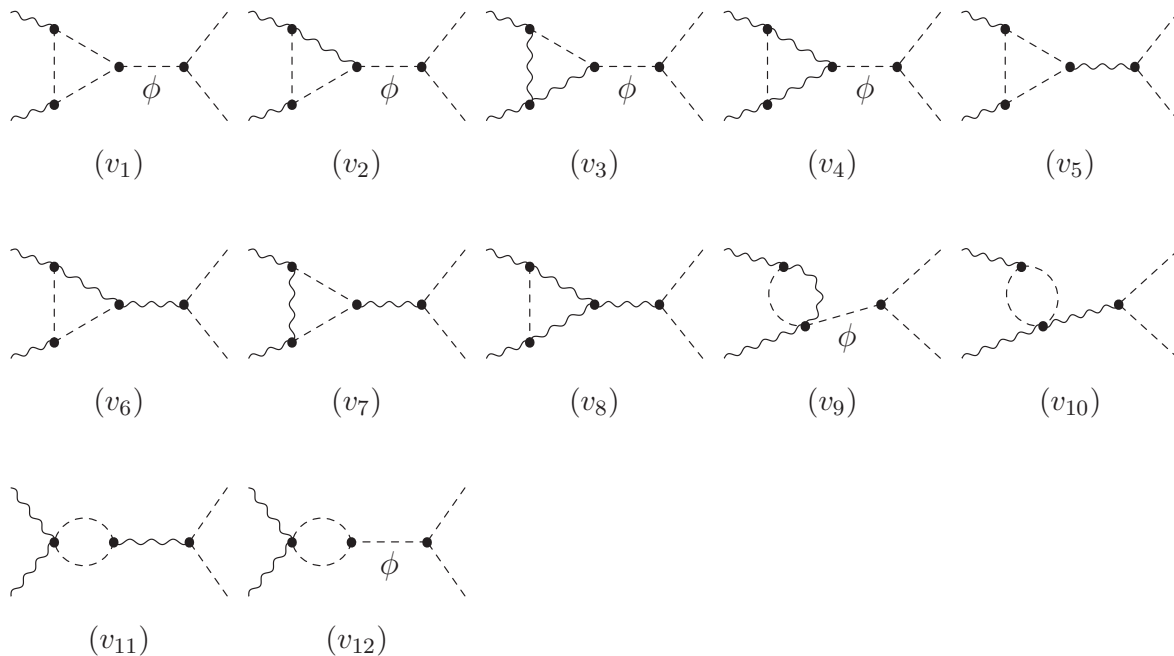
$m_h, M_H, M_A, M_{H\pm} = 120, 300, 350, 300$ GeV, $\sin\alpha = -0.9$,
 $1 \lesssim \tan\beta \lesssim 10$, $m_{12} \in [0, 600]$ GeV

Probing triple Higgs couplings in the 2HDM at $\gamma\gamma$ collider

A.A, R.Benbrik and C.H.Chen and R.Santos'09

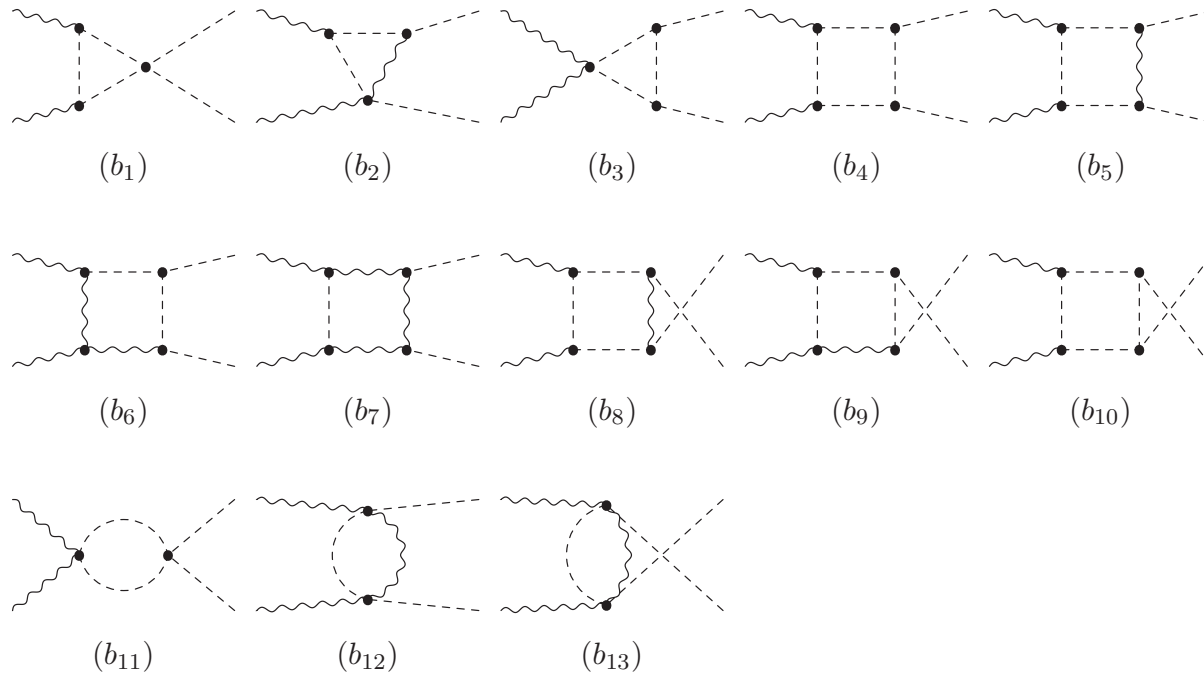
F.Cornet et al PLB'08, E. Asakawa et al PLB'08

- $\gamma\gamma \rightarrow hh$ is loop mediated, then very sensitive to new physics.
- $\gamma\gamma \rightarrow hh$ has more phase space than $e^+e^- \rightarrow Zh h$



Just charged Higgs contribution are shown

In 2HDM, scalar loops dominate

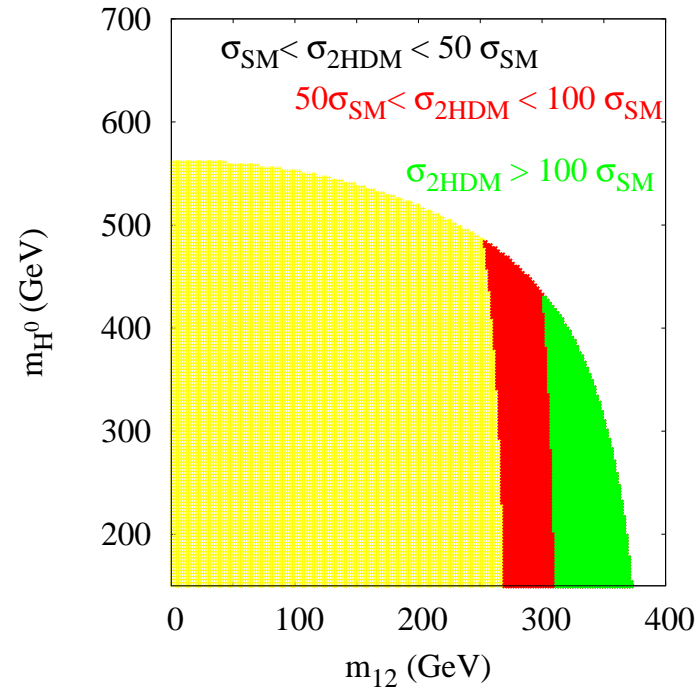
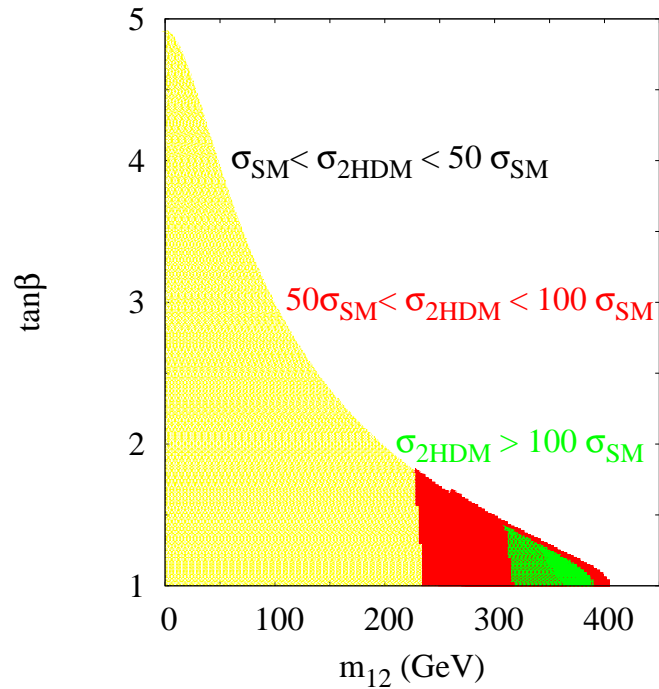


www.FeynArts.de , FormCalc , LoopTools, (T.Hahn)

$\gamma\gamma \rightarrow HH$ in SM

Jikia'92, Belusevic'04 and Takahashi'08

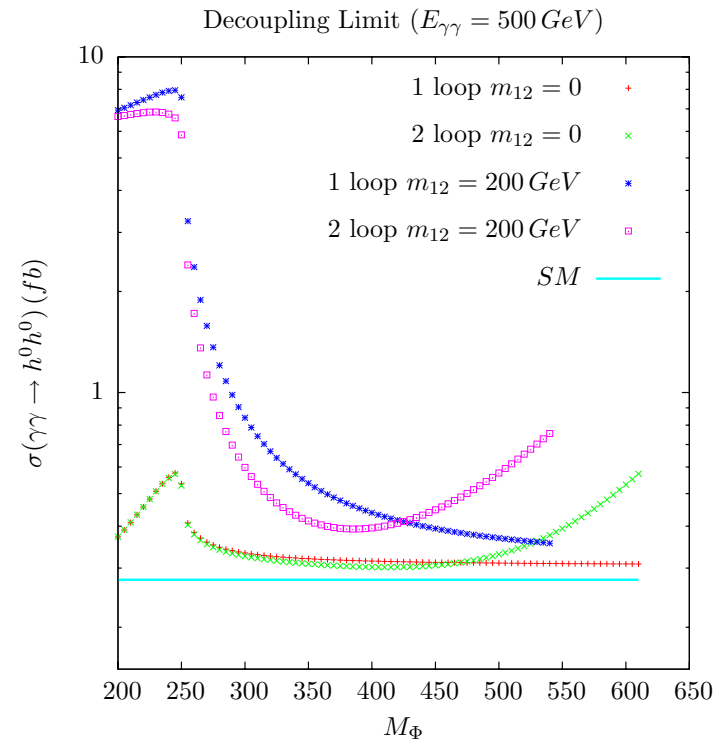
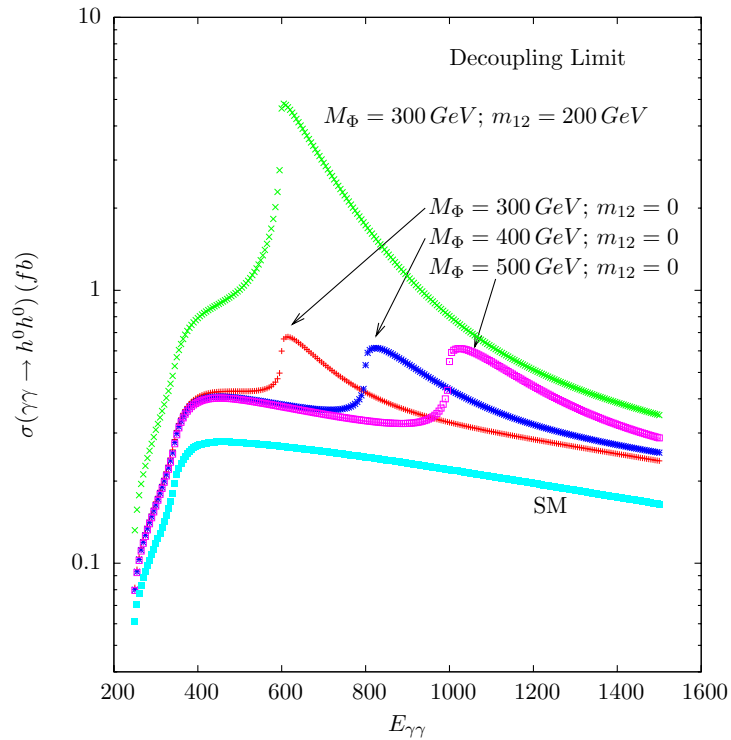
- look for $\gamma\gamma \rightarrow HH \rightarrow 4b$
- Main background from W^+W^- and from non-resonant four jet final state.
- Select 2 jet and reconstruct Higgs mass, $M(q\bar{q}) - MH < 5$ GeV
- **Conclusion:** For a center of mass energy of 350 GeV and $m_H = 120$ GeV an integrated luminosity of 450 fb^{-1} would be needed to exclude a zero Higgs boson self-coupling at the 5σ level.



$m_{h^0} = 115 \text{ GeV}$, $m_{A^0} = 270 \text{ GeV}$, $m_{H^\pm} = 350 \text{ GeV}$.

Left $m_{H^0} = 2m_{h^0}$, $E_{\gamma\gamma} = 500 \text{ GeV}$, $-1 \leq \sin\alpha \leq 1$, $1 \lesssim \tan\beta \lesssim 10$
 and right $\tan\beta = 1$, $\sin\alpha = -0.9$, $E_{\gamma\gamma} = 800 \text{ GeV}$

Decoupling limit, $m_h = 120$ GeV

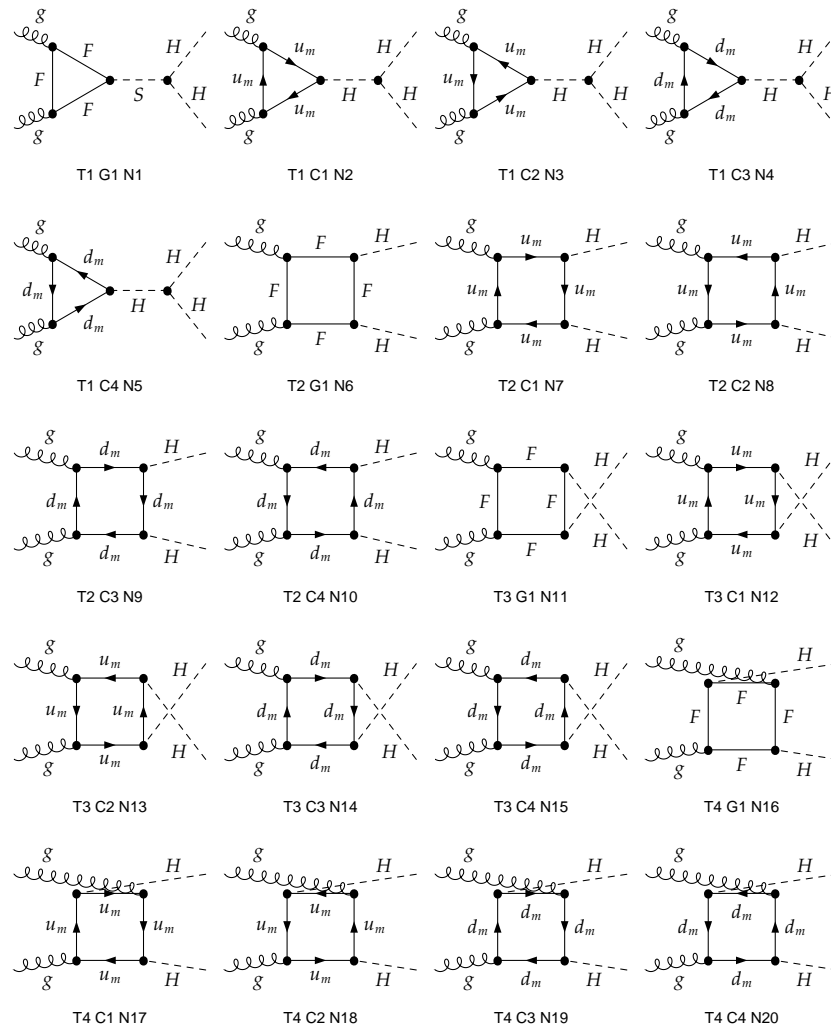


(Left) $\gamma\gamma \rightarrow hh$ at LO,

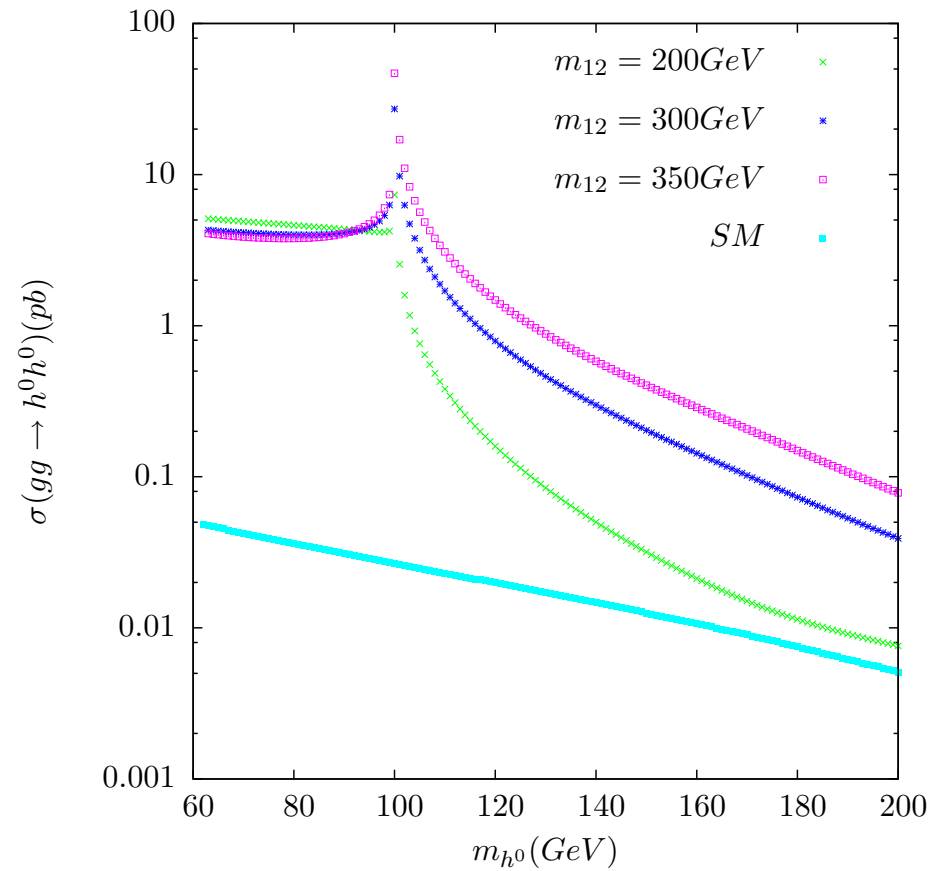
(Right) $\gamma\gamma \rightarrow hh$ at LO and LO + High order corrections to hhh

3. Probing triple Higgs couplings in the 2HDM at LHC

(A.A, R.Benbrik, C.H. Chen, R. Guedes and R.Santos'09)

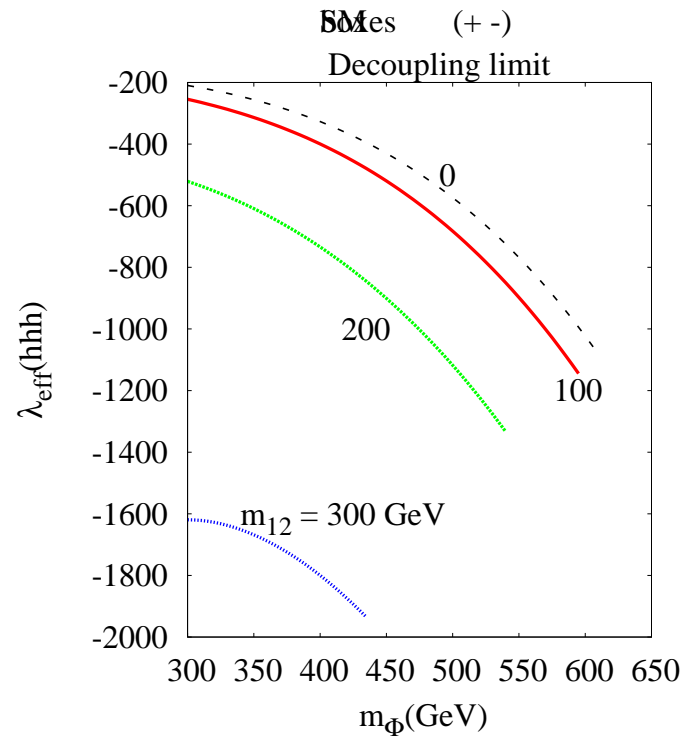
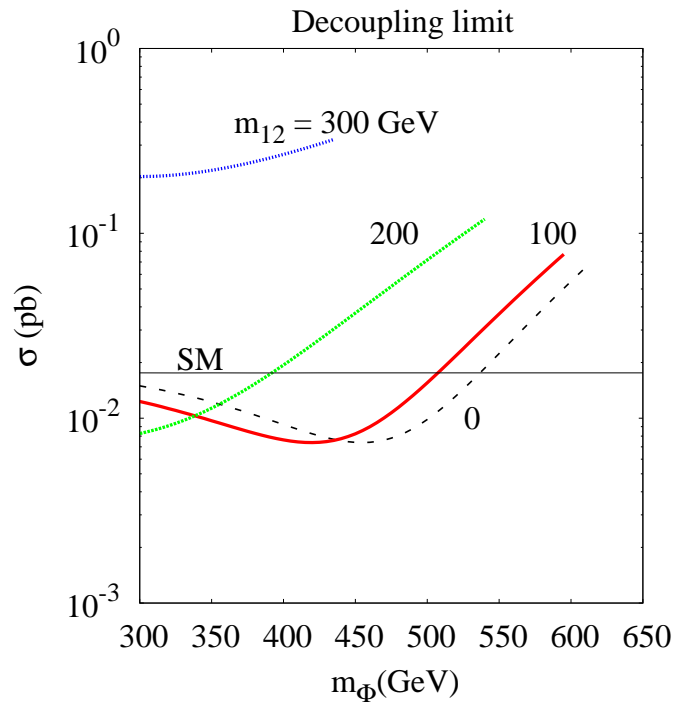


- In SM, the cross section is small $1 \lesssim \sigma(gg \rightarrow HH) \lesssim 3$ fb for $120 \lesssim M_H \lesssim 190$ GeV.
- $150 \lesssim M_H \lesssim 200$ GeV, from $gg \rightarrow HH \rightarrow W^+W^-W^+W^- \rightarrow 2l4j$ or $3l2j$, the non vanishing of the triple Higgs coupling of the SM can be established at 95% CL (with 300 fb^{-1}).
- One need VLHC to measure the triple Higgs coupling of the SM with an accuracy of 8-25% at 95% CL. (U. Baur et al '03)
- $M_H \lesssim 140$ GeV, $gg \rightarrow HH \rightarrow b\bar{b}\gamma\gamma$, look promissing. With 600 fb^{-1} or more, we could make a rough first measurement for $M_H = 120$ GeV (with 6 signal events). (U. Baur et al '04)



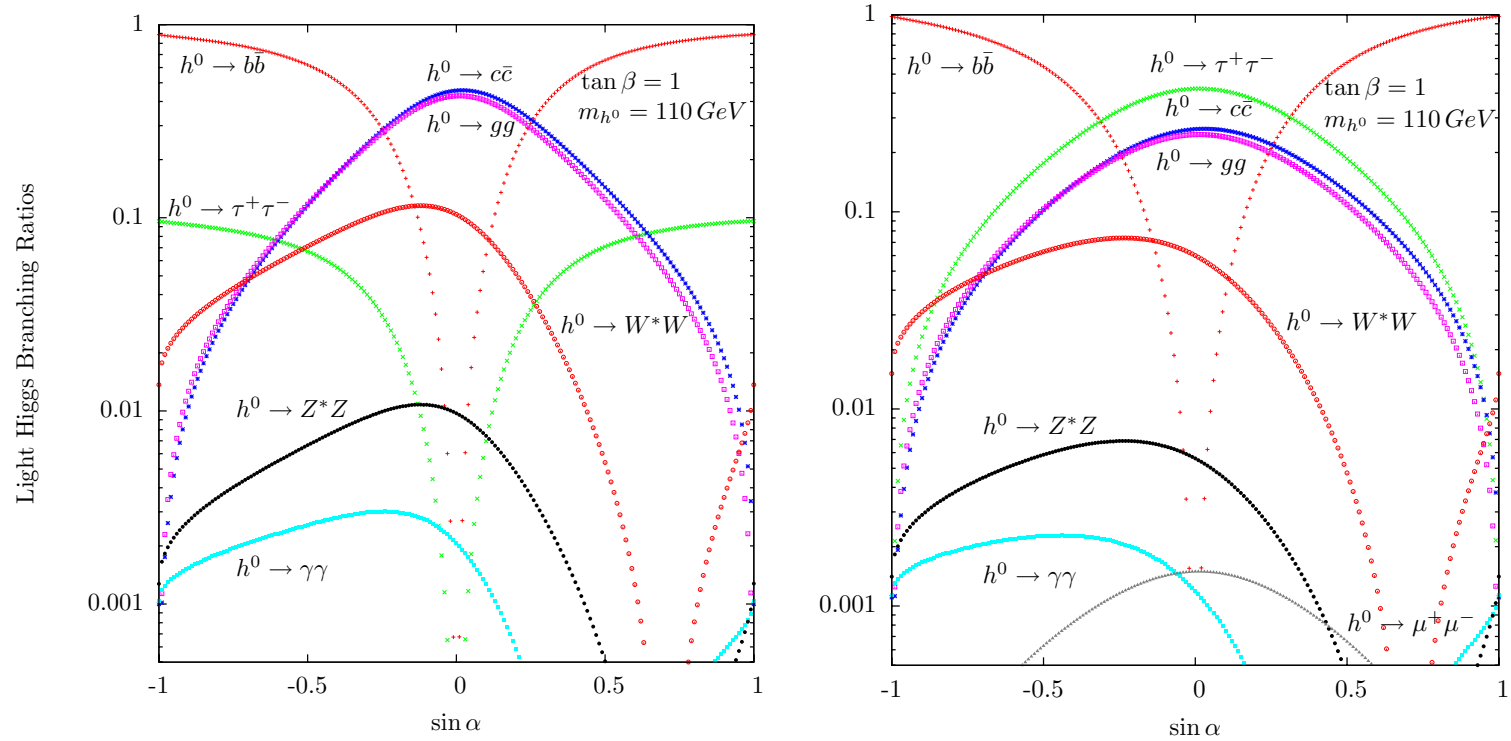
$m_{H^0} = 200\text{GeV}$, $m_A = 200\text{GeV}$, $m_{H^\pm} = 300\text{GeV}$, $\sin \alpha = 0.631$ and $\tan \beta = 1$. ($\sin(\beta - \alpha) = 0.1$)

Decoupling limit



(+ +)

Higgs signatures



Left: 2HDM-II , Right 2HDM-X (leptophilic Higgs)

Conclusions

- LHC will be capable to discover the Higgs bosons and measure its coupling to top quark, τ lepton, W and Z with 10–30% accuracy ($\mathcal{L} = 300 fb^{-1}$).
- At LC, the precision of the measurement is about 1–2%, such precision is needed to distinguish between models.
- In 2HDM, non decoupling effects could be large to be measured both at LHC and ILC and its $\gamma\gamma$ option.
- If 2HDM Higgs masses are not too heavy, their triple self couplings can be accessible at LHC and ILC