

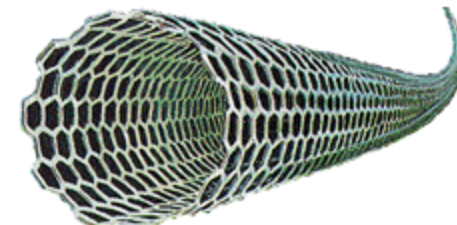
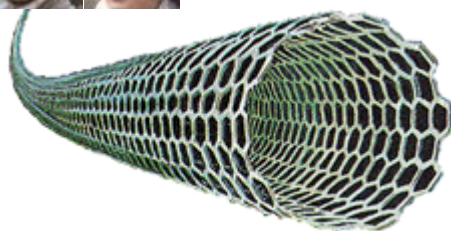


Optical characterization of nanotube and graphene

Riichiro Saito

A. R. T. Nugraha, K. Sato,
L. C. Yin, K. Sasaki, C. Conxiao, Y. Ting,
G. Dresselhaus and M. S. Dresselhaus

Tohoku University, Sendai, Japan
Nanyang Technological University, Singapore
Massachusetts Institute of Technology, MA, USA





東北大学

Tohoku University

Sendai city 350km from Tokyo

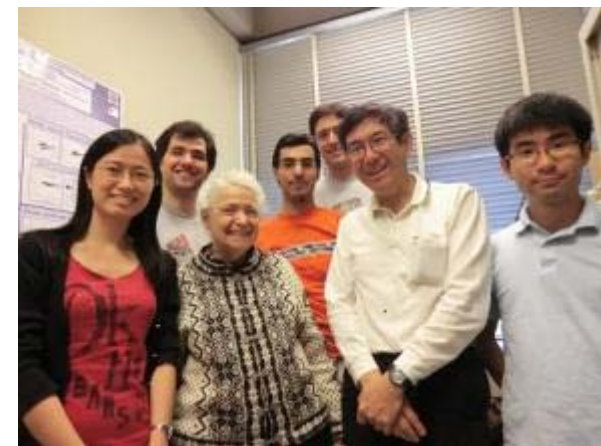
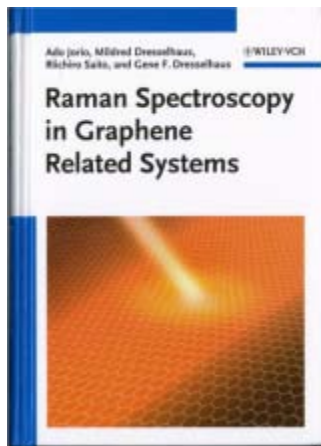
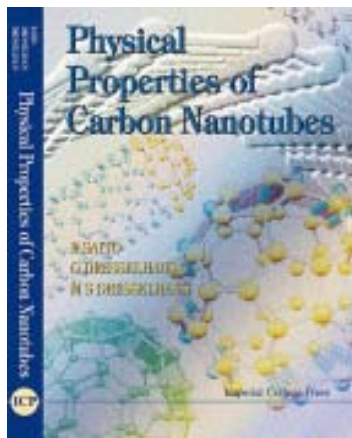
Sendai Pageant of Starlight

Sushi



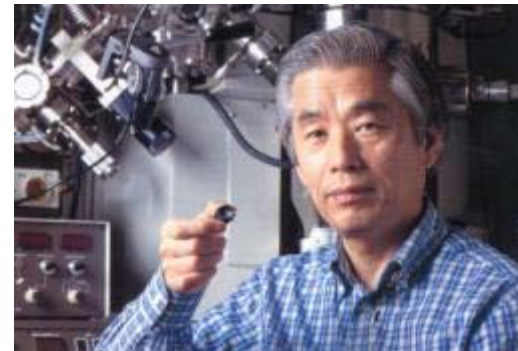
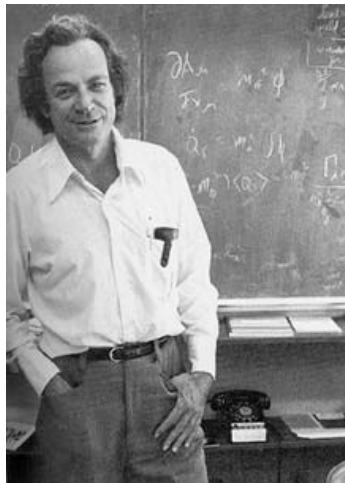
Outline of this 1 hour talk

1. Introduction of Nano Carbon
2. Optical (Raman) characterization
 - Carbon nanotubes
 - Graphene



Introduction of Nano Carbon

Carbon material with 1-10nm size

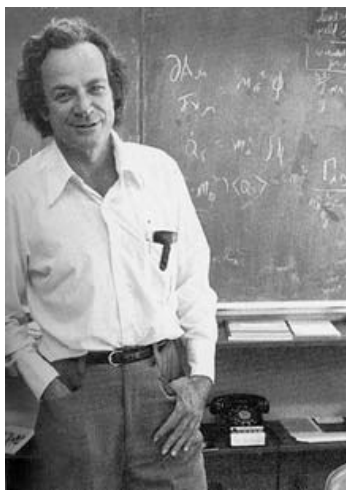


The size of human made objects

(From the American DOE report)

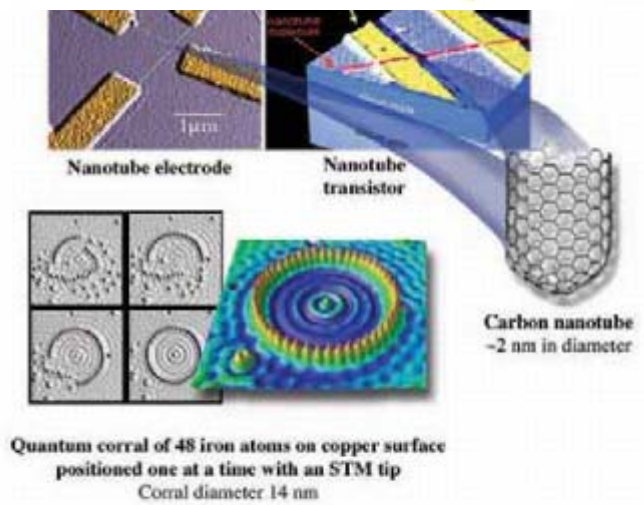
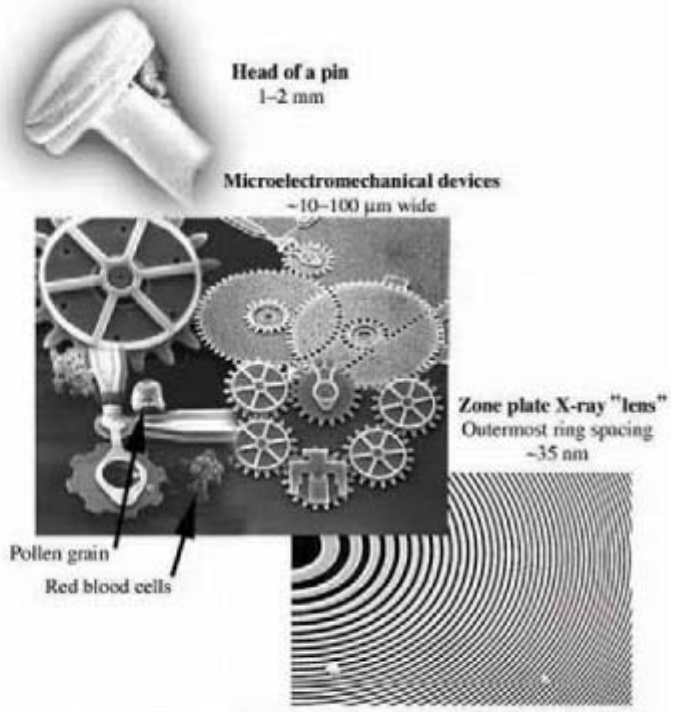
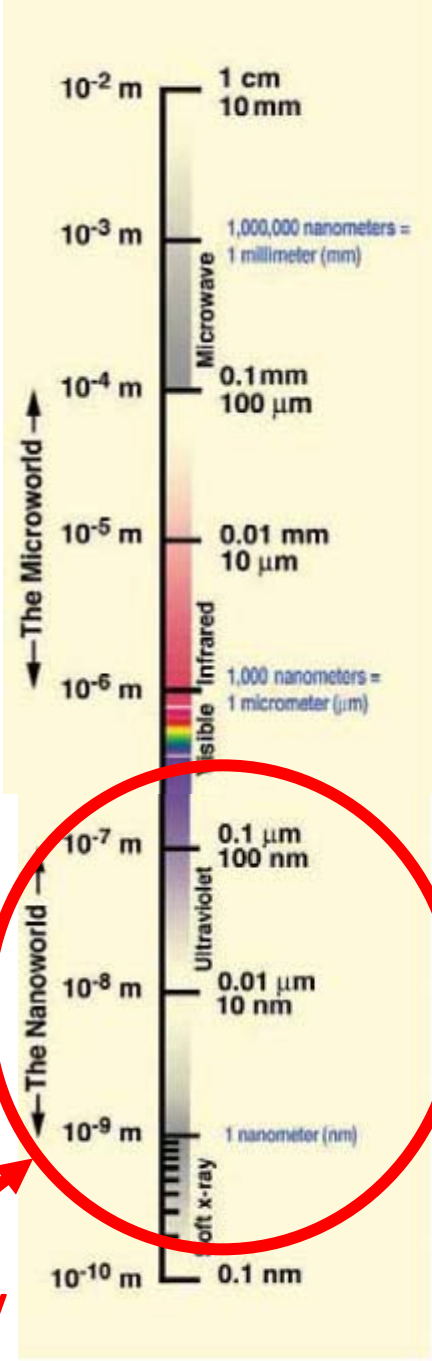
Lower limit of size optical microscope

1 Micron = 1 μm



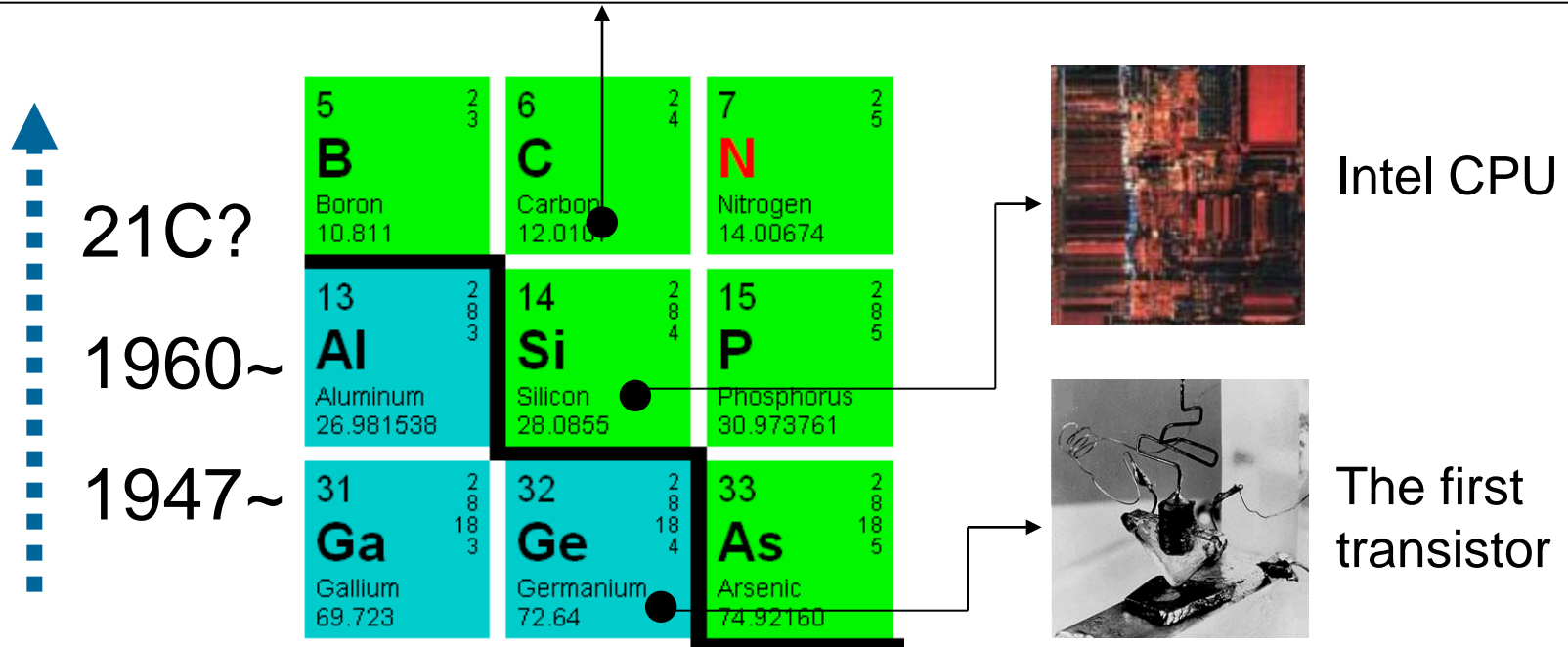
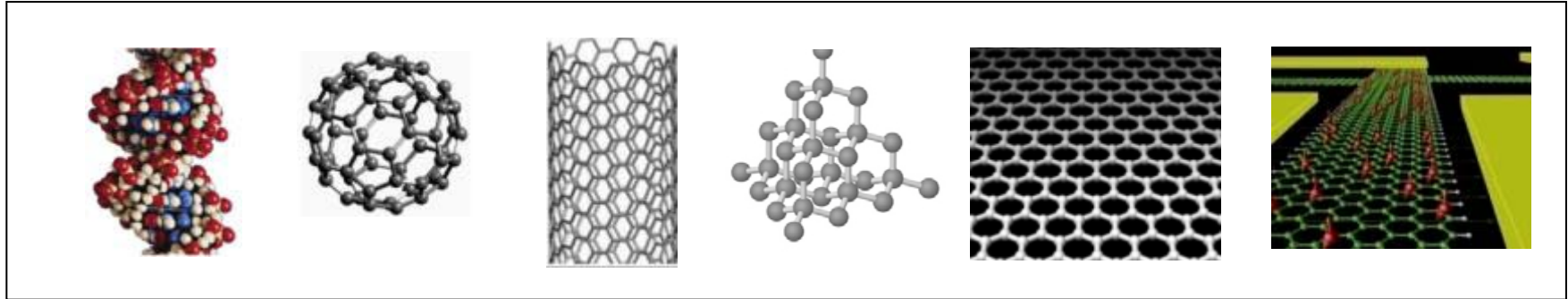
Richard Feynman

Undeveloped Territory in 1950's



Courtesy Office of Basic Energy Sciences, Office of Science, U.S. Department of Energy

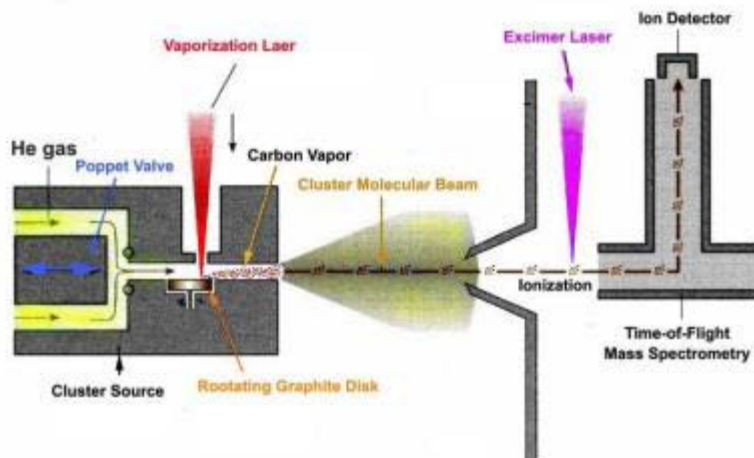
Why nano carbon?



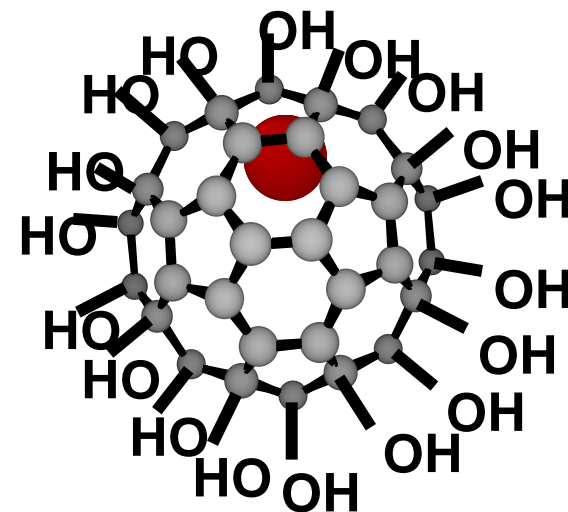
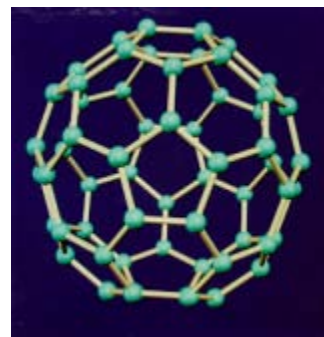
Semiconductor, small size, mobility, melting T

This slides is inspired by T. Ohta at LBNL and Fritz-Haber-Institut.

C₆₀ molecule (1985 Sept. 12th)

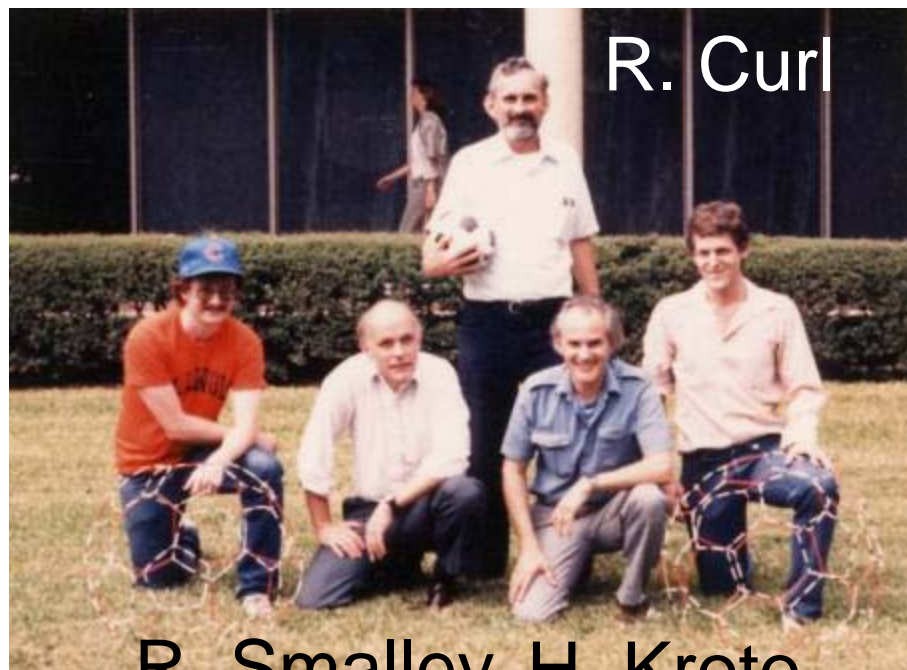


Laser Ablation



C₆₀

Gd@C₈₂(OH)_n



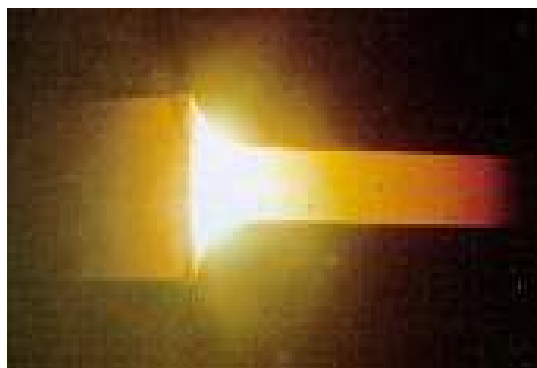
R. Curl

R. Smalley H. Kroto

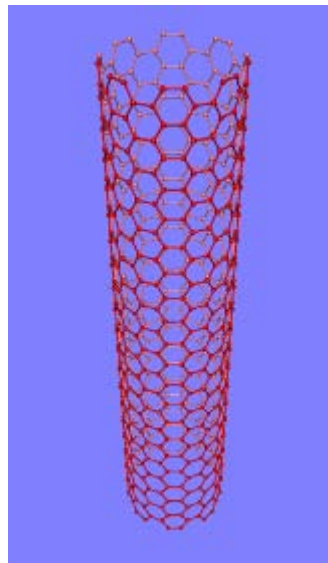


MRI applications

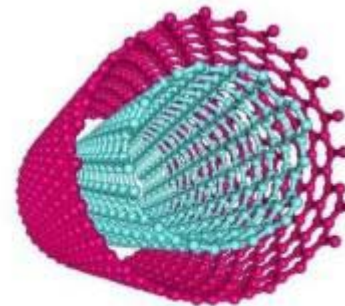
Carbon Nanotubes (1991)



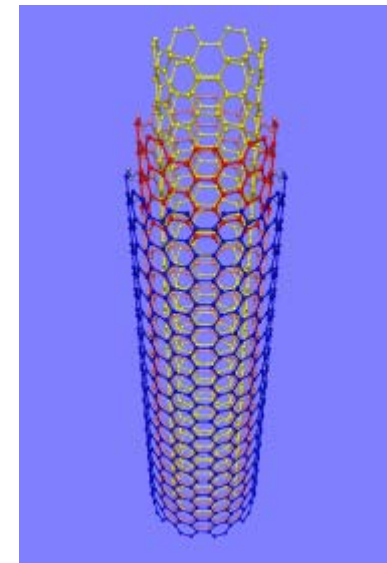
Arc Discharge



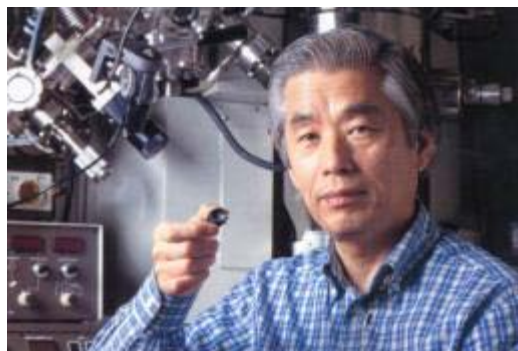
Single-wall nanotube (SWNT) 1993



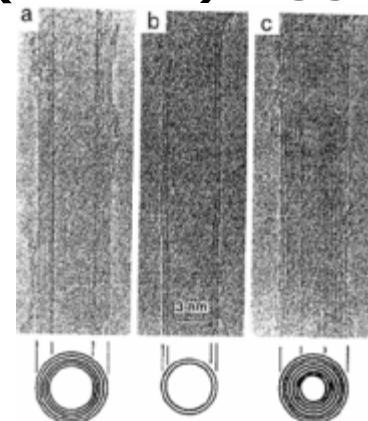
Double-wall nanotube



Multi-wall nanotube (MWNT) 1991

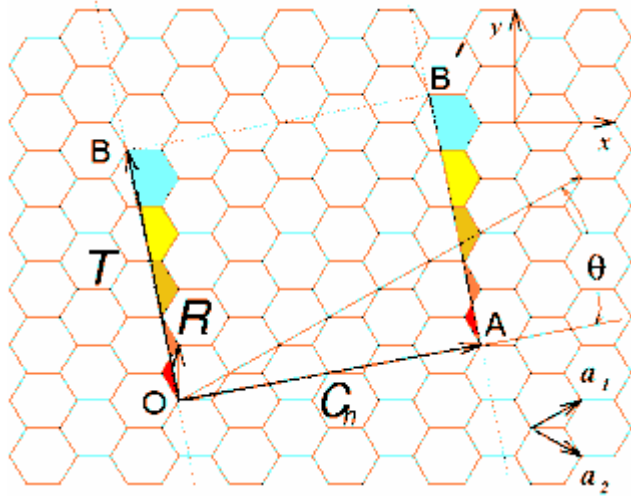


S. Iijima

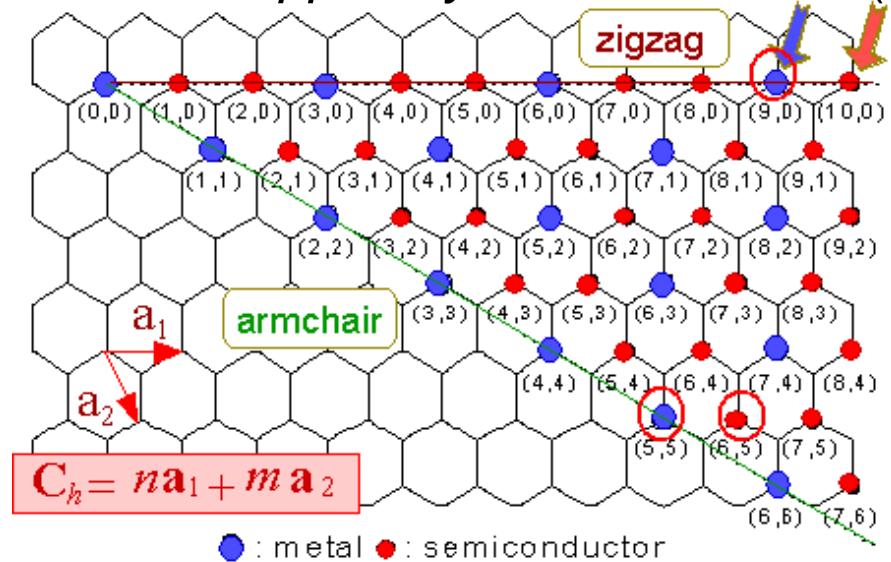


Chirality of Nanotubes (1991)

$$C_h = na_1 + ma_2 \equiv (n, m)$$

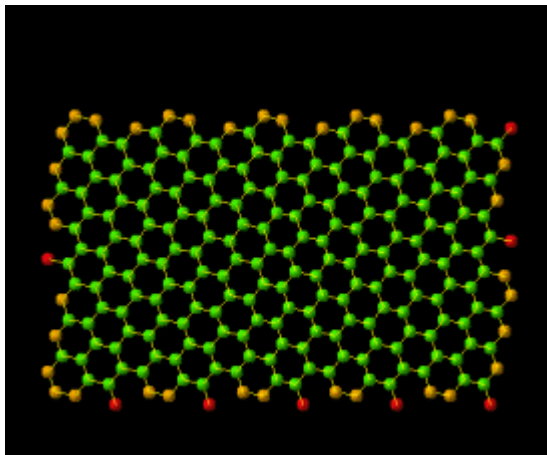


R. Saito *et al.*, *Appl. Phys. Lett.* **60**, 2204 (1992)

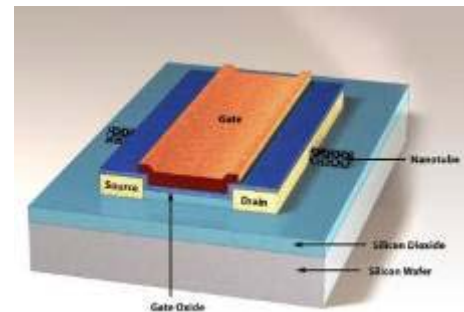


metallic or semiconducting

definition of chirality

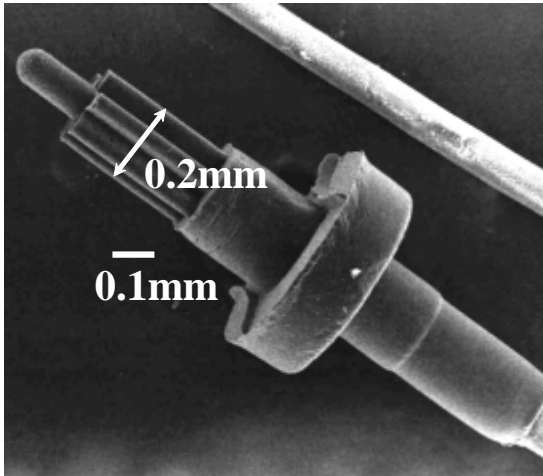


(10,5) nanotube



nanotube FET

Application of fiber-nanotube : Composite Endo



Tiny gear



M. Endo

Hybrid bus
Pb battery





Artificial joint

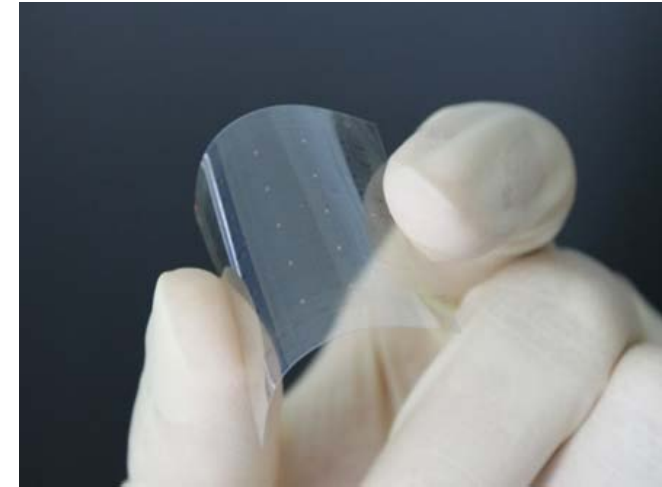


Less friction
Long life

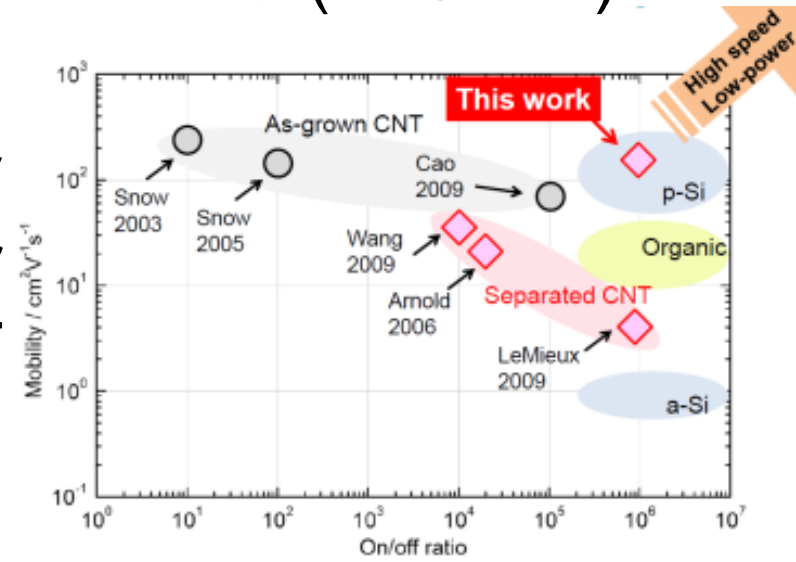


Chirality separation
(H. Kataura)

High mobility
Low power
High T



Nanotube FET
(Y. Ohno)



Fullerene factory



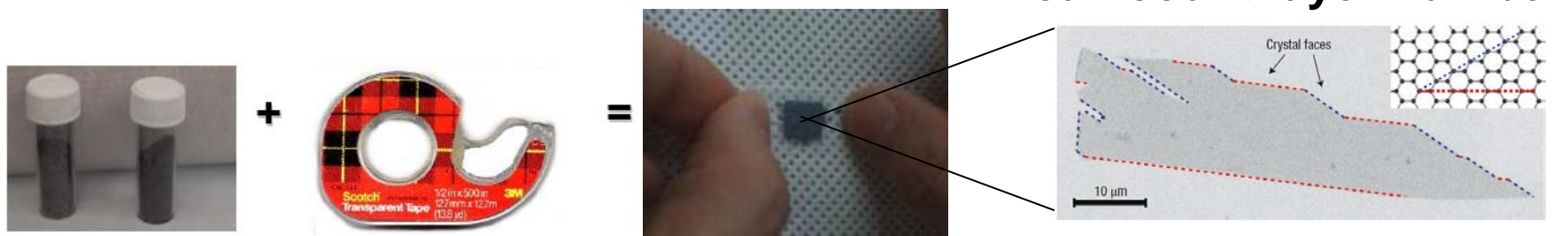
Capacity = 40 tons fullerenes/year (as of May 2008)

Exfoliated Graphene

- Breakthrough



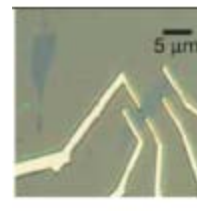
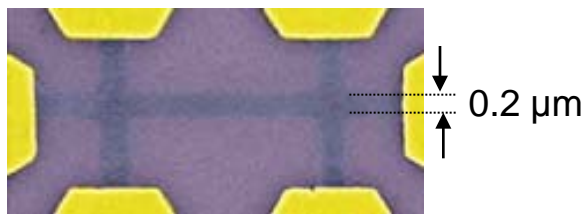
Micromechanical cleavage of graphite via adhesive tapes !
Novoselov *et al*, Science **306**, 666 (2004)



Scotch tape makes one atomic layer

A. K. Geim Group @ Manchester
K. S. Novoselov *et al*, Nature **438**, 197 (2005)

P. Kim Group @ Columbia
Y. Zhang *et al*, Nature **438**, 201 (2005)

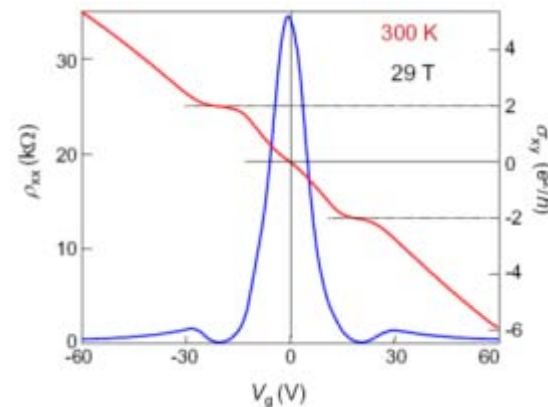
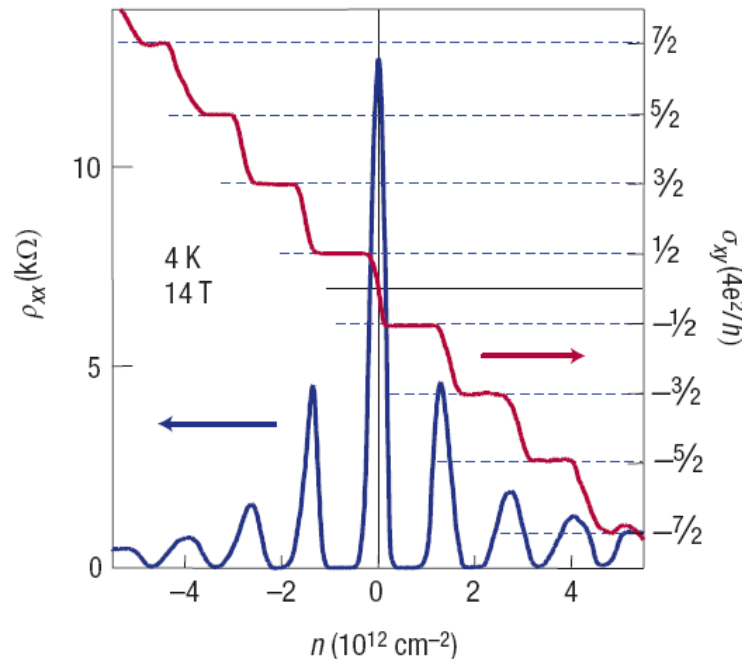


Electronic structure of graphene

- Consequences of chiral massless Dirac fermions

Half-integer Quantum Hall Effect (Room T) !
(Manifestation of Berry's phase of pseudospin)

Half integer QHE at room T



$$R_{xy}^{-1} = \pm g_s \cdot \left(\nu + \frac{1}{2} \right) \cdot \frac{e^2}{h}$$

$$\nu = 1, 2, 3, \dots$$

$$g_s = 2 \times 2 \text{ (spin \& sublattice)}$$

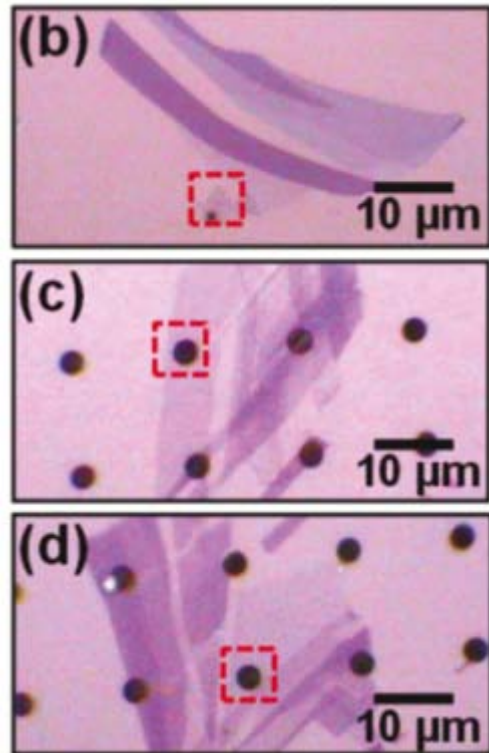
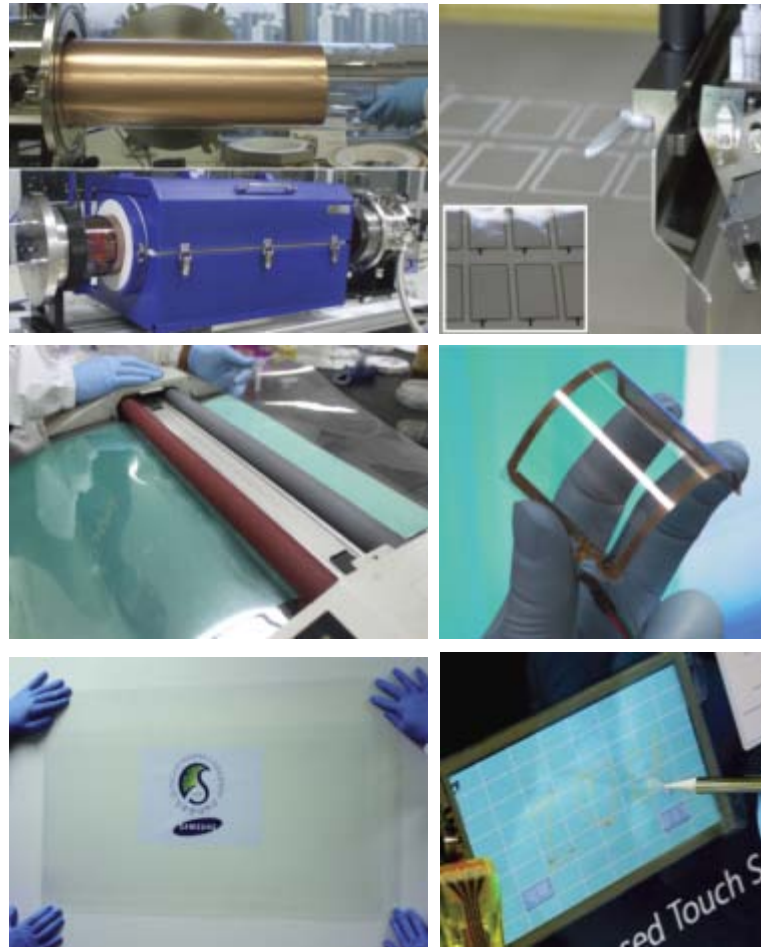
$$\text{Haldane (88), T. Ando (02)}$$

Zhang *et al* (05), Novoselov *et al* (05)

Kim & Geim *et al* (07)

Touch screen application

Single and bi-layer graphene

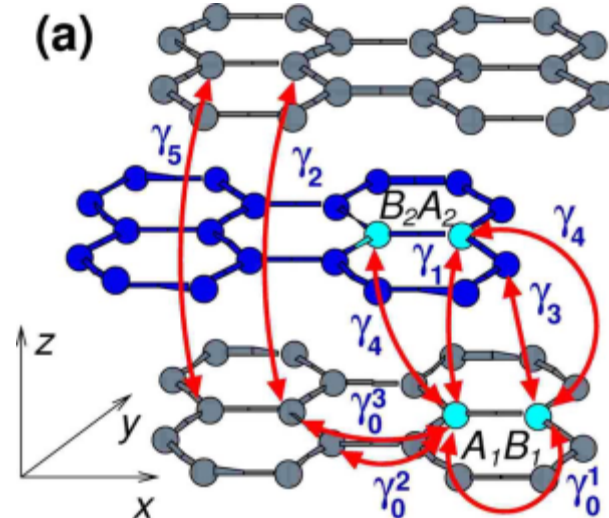


C. Cong et al., ACS Nano 5, 1600 (2011).

S. Bae et al., Nature Nanotechnology 5, 574 (2010).

CVD (Cu foil, gas mixture of CH₄ and H₂)

AB stacking graphene

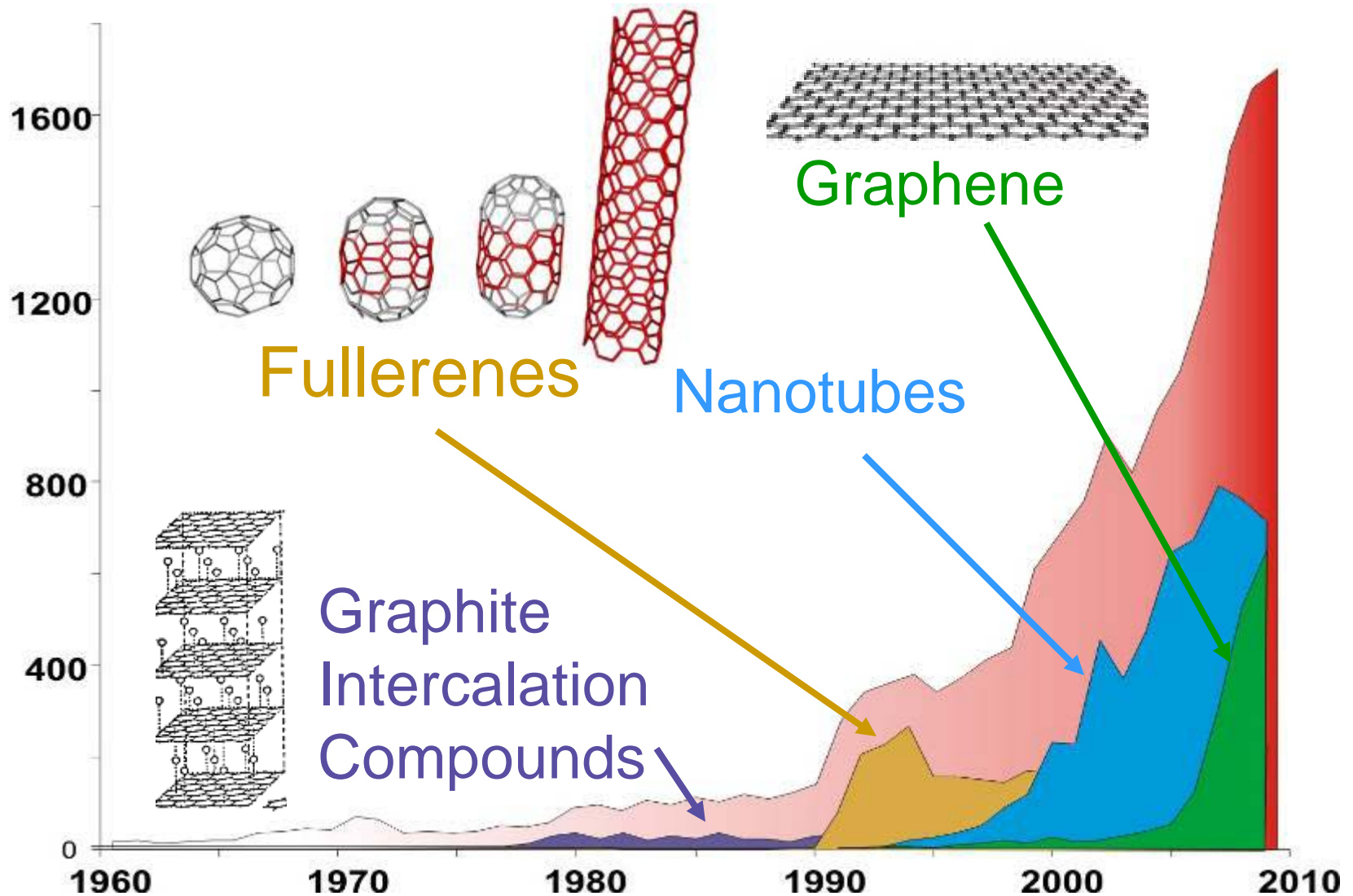


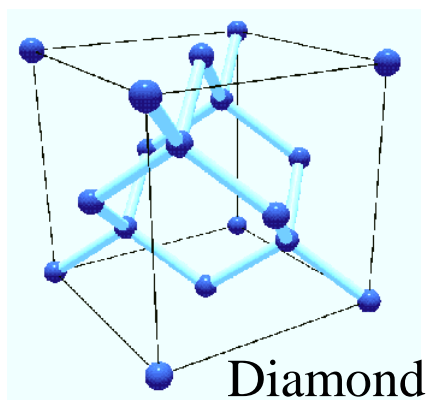
A. Gruneis et al., Phys. Rev. B 78, 205425 (2008).

Stacking order

Development of the field of nano-carbon research

Number of physics-related publications on Carbon

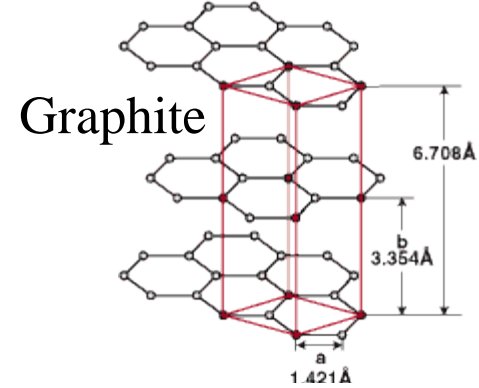




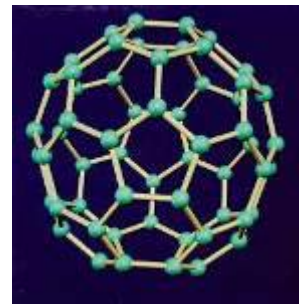
Family of nano-carbon

hybridization and geometry

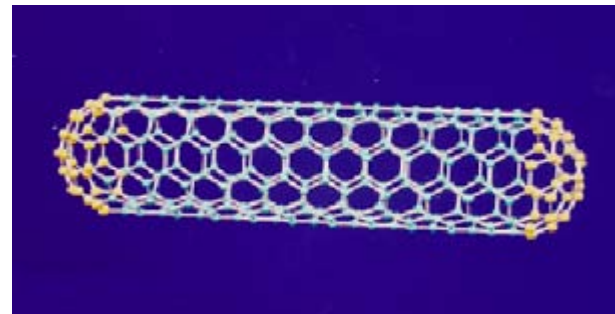
R. Saito, in "Carbon Alloy" Elsevier (2003)



Fullerene

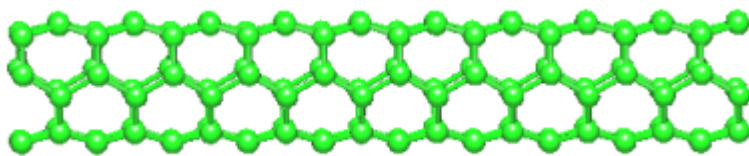
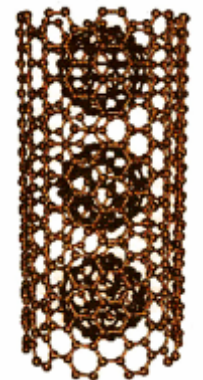
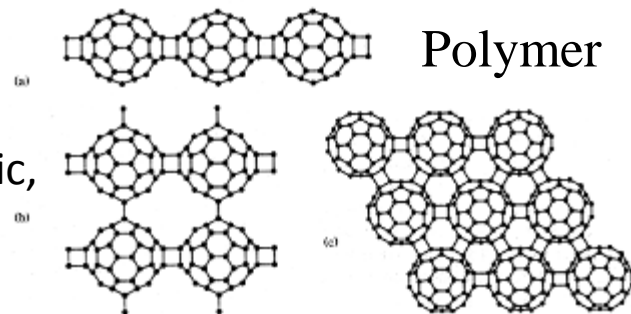


- sp^3 : Diamond (3D)
- sp^2 : Graphene Graphite (2D)
- Fullerene (0D)
- Fullerene Polymer(1-3D)
- Nanotube (1D)
- Peapod (0D+1D)

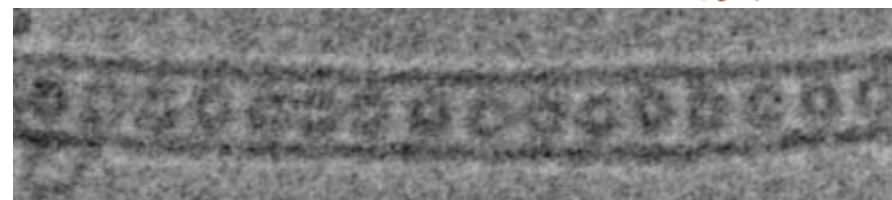


sp : Carbyne (1D)

Not crystal: HOPG, VGCF, glassy, whisker, fiber, nanohorn, turbostratic, nanographite

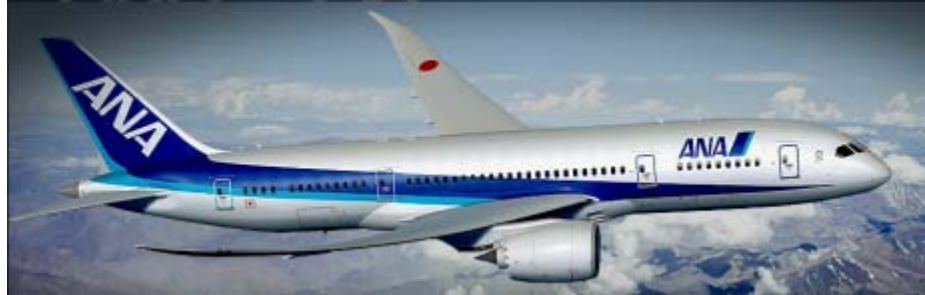


nanographite



Peapod & Nanobud

Competition between nanotube and graphene



B787

Requirement from society

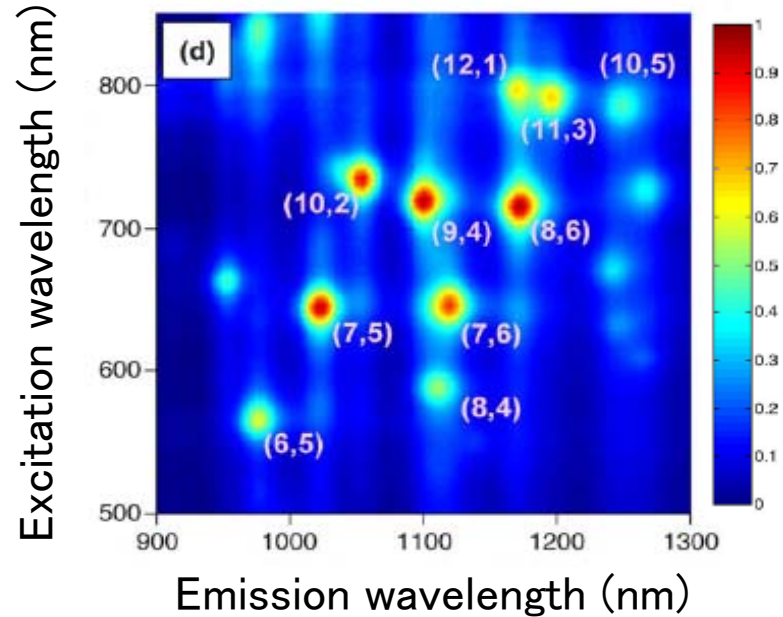
Synthesis technique

Quality of material

Quantity and price

Physical properties

Optical properties of nanotubes

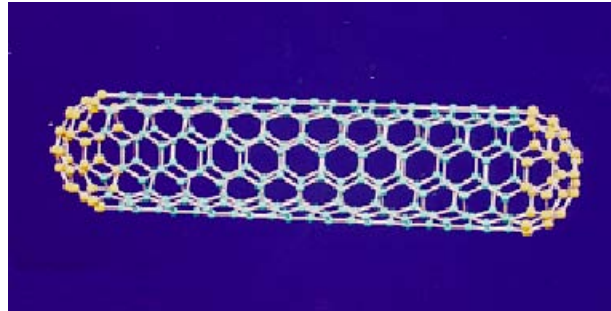
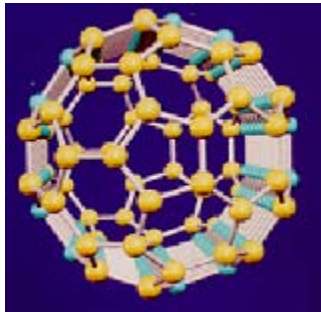


Nanotubes Structure

S. Iijima, (1991), M. S. Dresselhaus *et al.* (1991)
J. Mintmire *et al.*, R. Saito *et al.*, N. Hamada *et al.*, K. Tanaka *et al.*

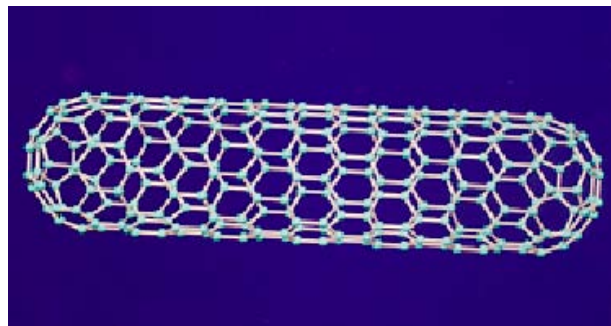
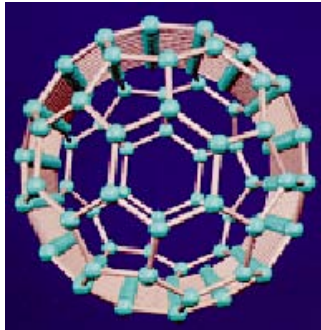
Arc Method:(by Y. Saito)

Laser Ablation:(by H. Kataura)



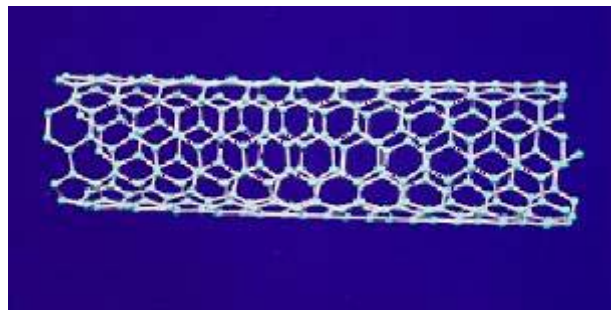
(5, 5)

Armchair



(9, 0)

Zigzag



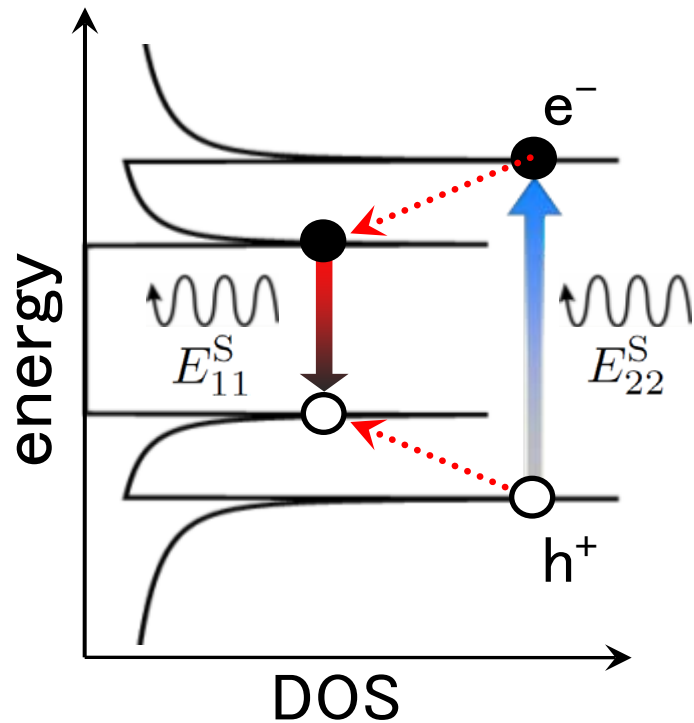
(6, 5)

Chiral



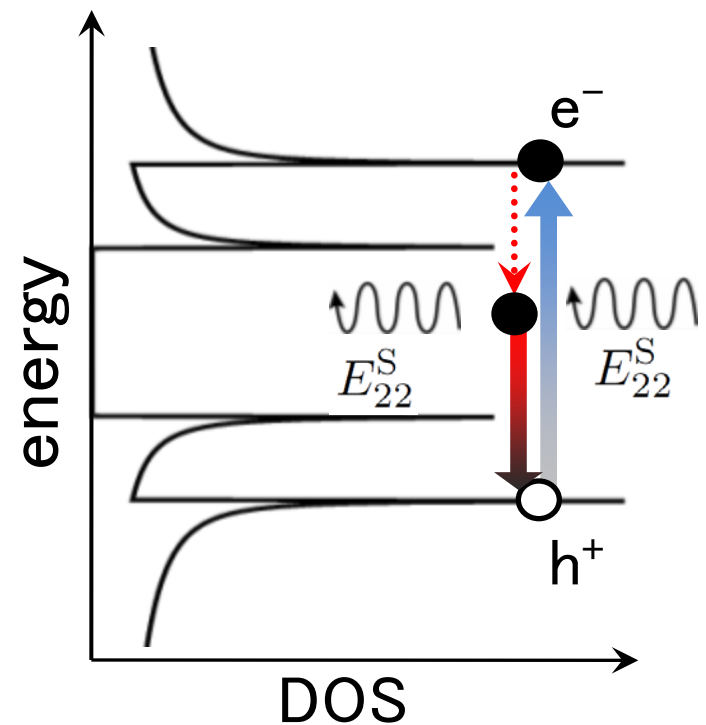
Photoluminescence and Raman

Photoluminescence



Spontaneous emission
of light 1ns

Resonance Raman

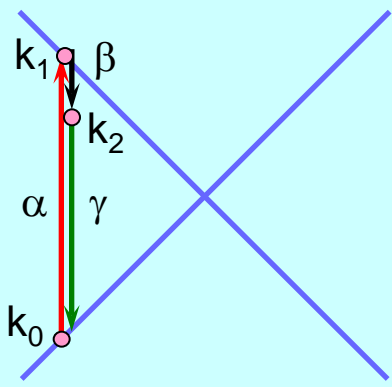
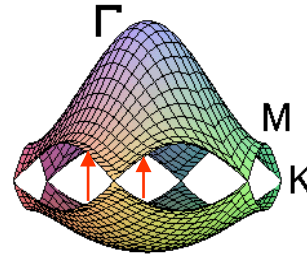


Inelastic scattering
of light 1ps

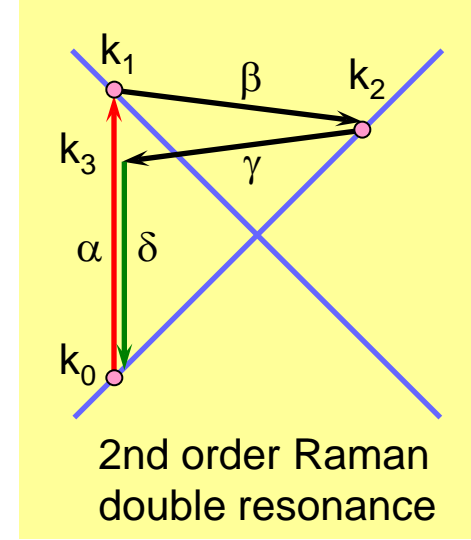
1st and 2nd order resonance Raman processes

M. S. Dresselhaus et al. Phys. Rep. 409, 47 (2005).

Electron phonon interaction



1st order Raman



2nd order Raman double resonance

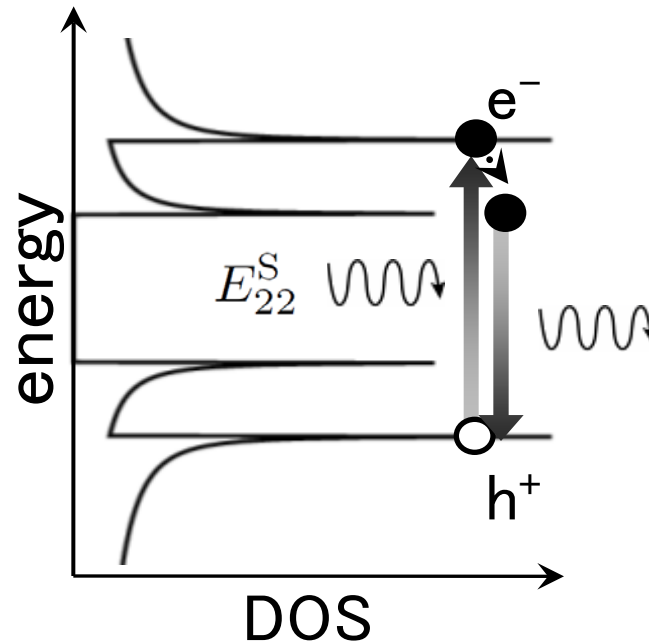
- Raman intensity formula(1st)

$$M = \sum_{a,b,c} \frac{M_{op}^{ab} M_{el-p}^{bc} M_{op}^{ca}}{(E_{las} - E_{ab} + i\gamma)(E_{las} - E_{phon} - E_{ac} + i\gamma)}$$

Light emission

Light absorption

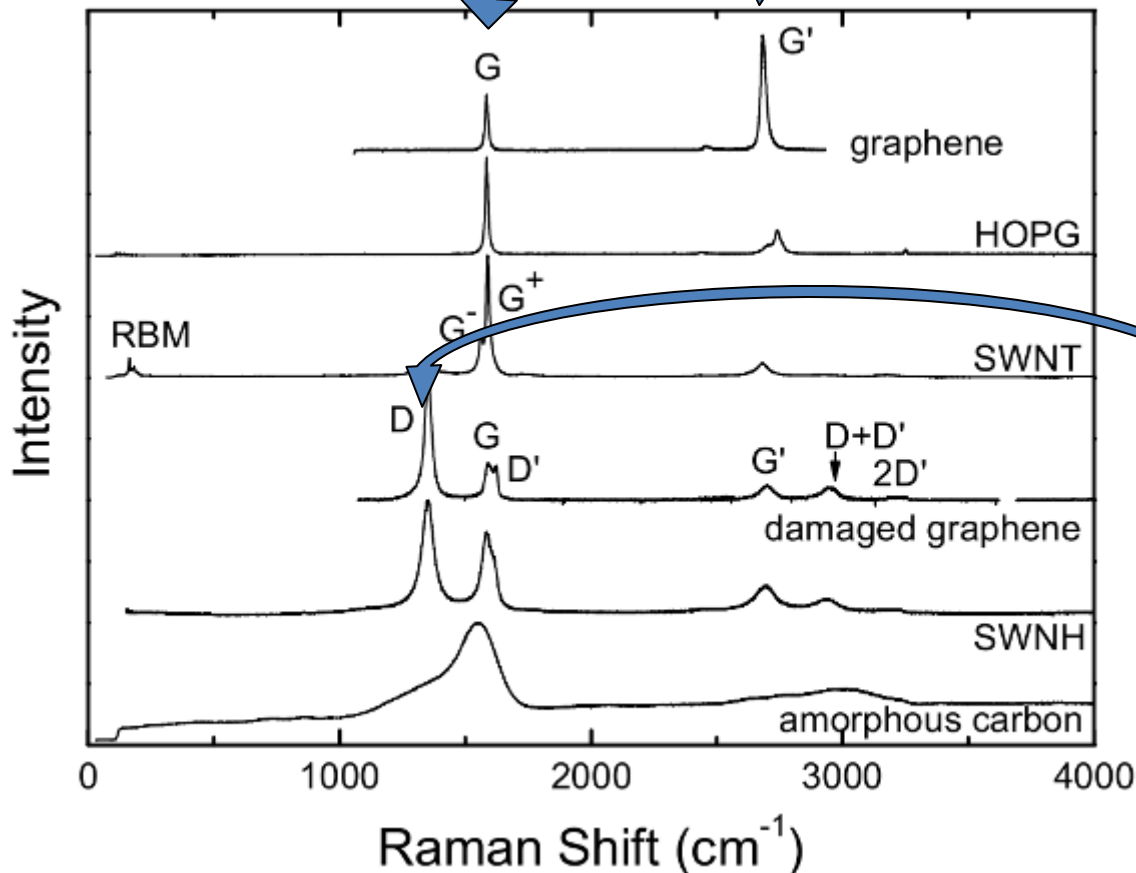
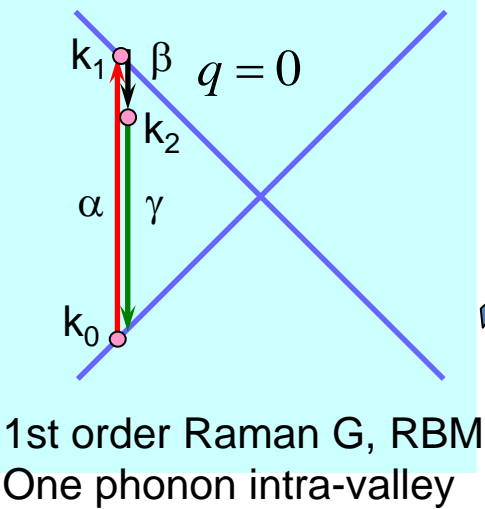
Intensity is enhanced
When optical absorption
occues.
Resonant Raman effect



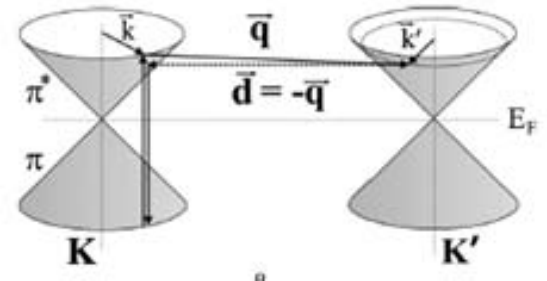
$h\omega_q$ Raman shift

Raman spectral of nano carbon

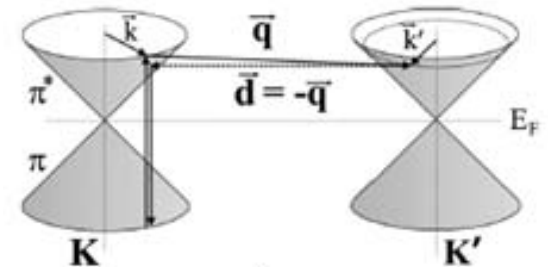
Spectral shape, Relative intensity,
Defect oriented Raman signals



G' : inter-valley DR
Two phonon scattering

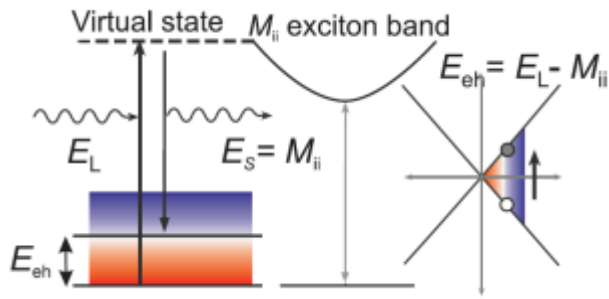
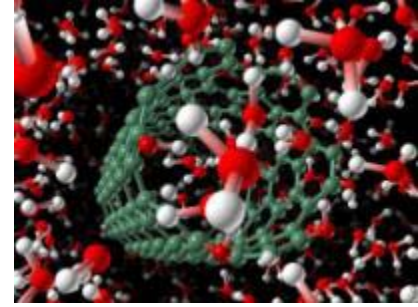


D: inter-valley DR
one phonon scattering
one elastic scattering

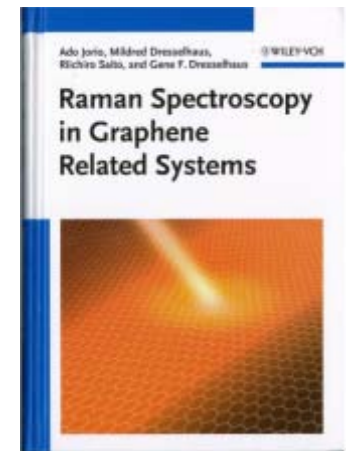
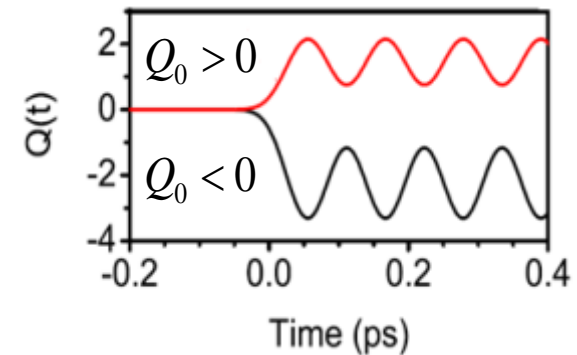


Defect is needed

Recent our works



- Nanotube Raman spectroscopy
 - Exciton Environmental Effect
 - Electronic Raman spectra
 - Coherent phonon spectra
- Graphene Raman spectroscopy
 - ABA stacking order
 - Kohn anomaly effect



A. Jorio, R. Saito, G. Dresselhaus, M. S. Dresselhaus
"Raman Spectroscopy of graphene related systems" Wiley-VCH (2011),

Exciton Kataura Plots

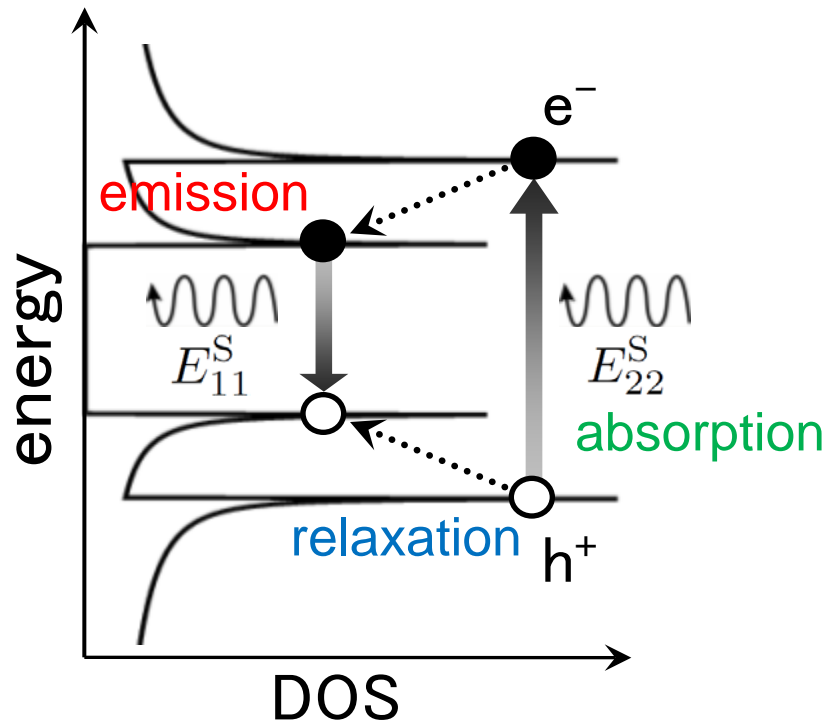
How to assign (n,m) for different surrounding materials?



(n,m) assignment from Photo-Luminescence (PL)

2D PL map of SWNTs

Optical Process of PL

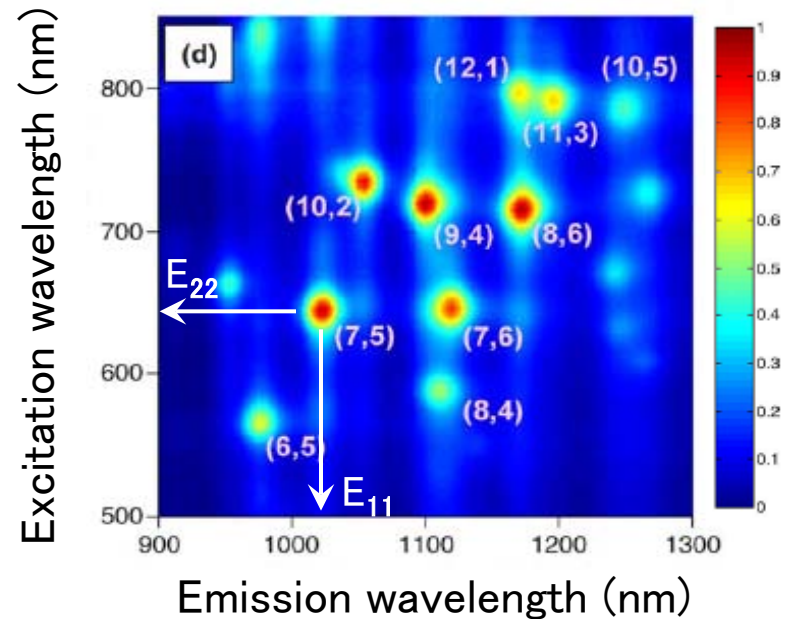


+ Intensity information

(type dependence, chiral angle dependence)

Y. Oyma et al. Carbon 44, 873-879 (2006).

- M. J. O'Connell *et al.*, Science **297**, 593 (2002)
- S. M. Bachilo *et al.*, Science **298**, 2361 (2002)
- Y. Miyauchi *et al.*, Chem. Phys. Lett. **387**, 198 (2004)



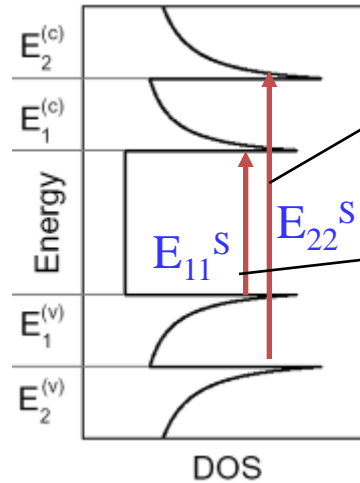
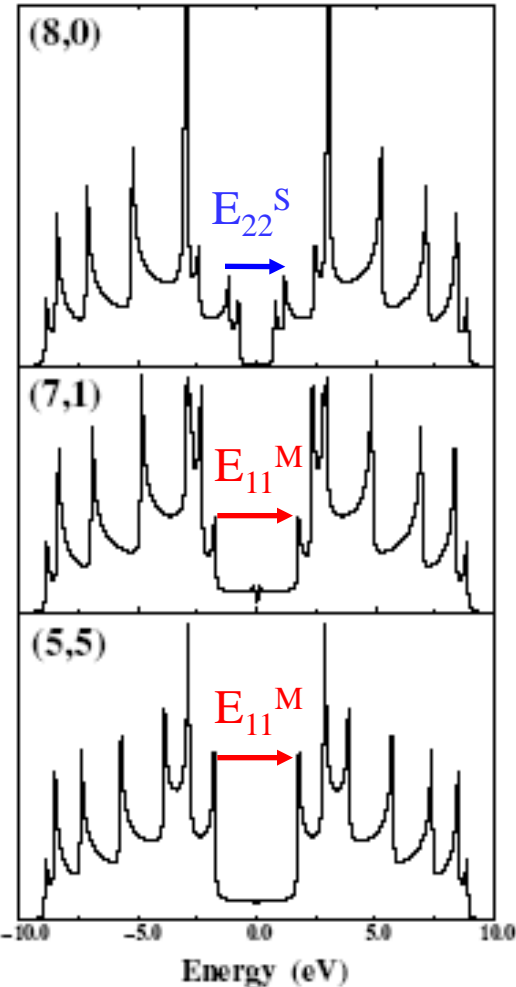
$(E_{22}, E_{11}) \rightarrow (n,m)$

Raman Spectroscopy: the Kataura plot

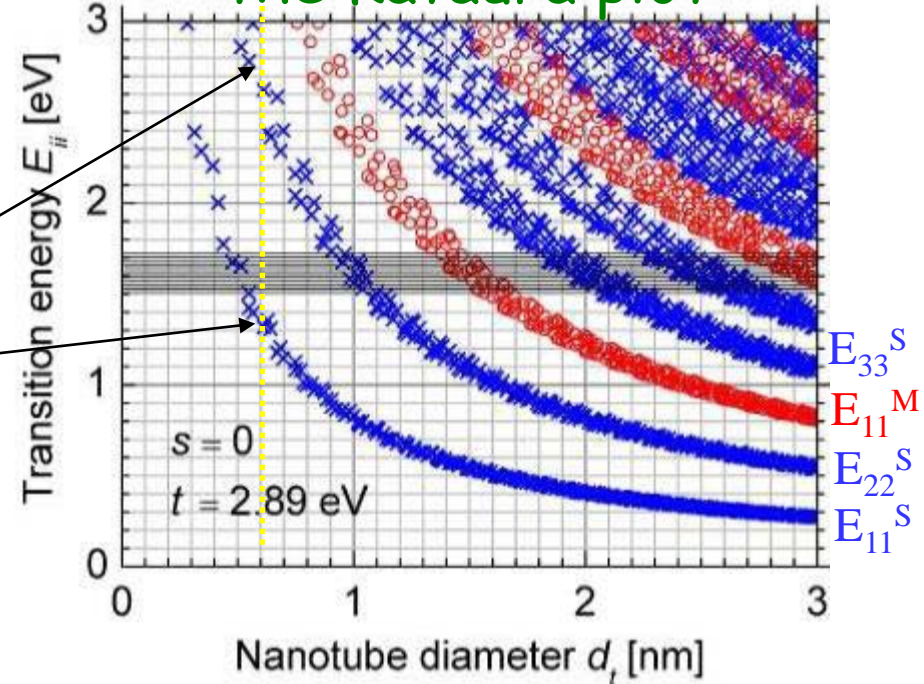
R. Saito et al., Phys. Rev. B 61, 2981 (2000)



vHS in the density of states (DOS)
Responsible for strong optical effects!



the Kataura plot



Raman Spectroscopy:
Excitation profile $\rightarrow E_{ii}$
RBM frequencies $\rightarrow d_t, \theta$

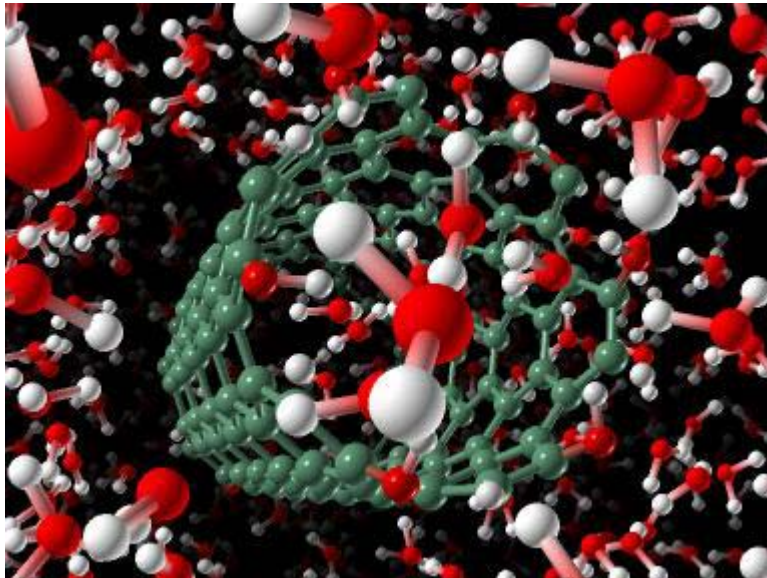
$$(E_{ii}, \omega_{ph}, Int.) \rightarrow (n, m)$$



Environmental Effect of SWNTs

$$\Delta E_{ii} (0-80\text{meV})$$

depending on surrounding materials



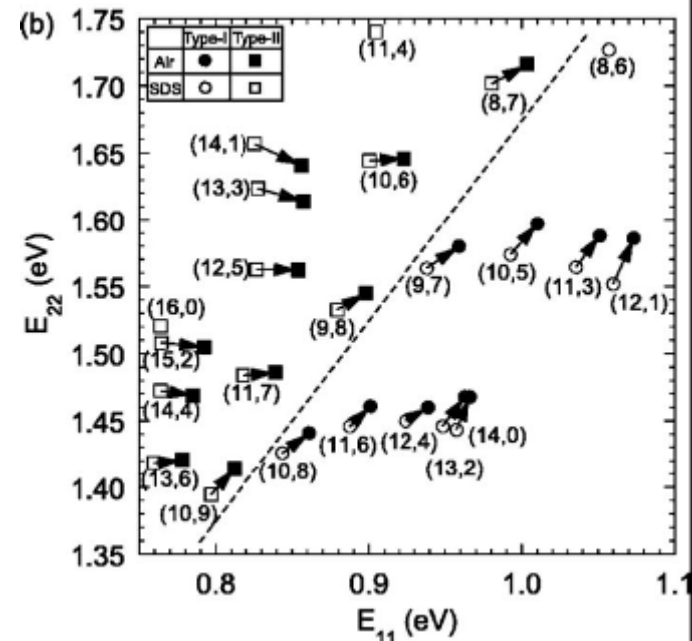
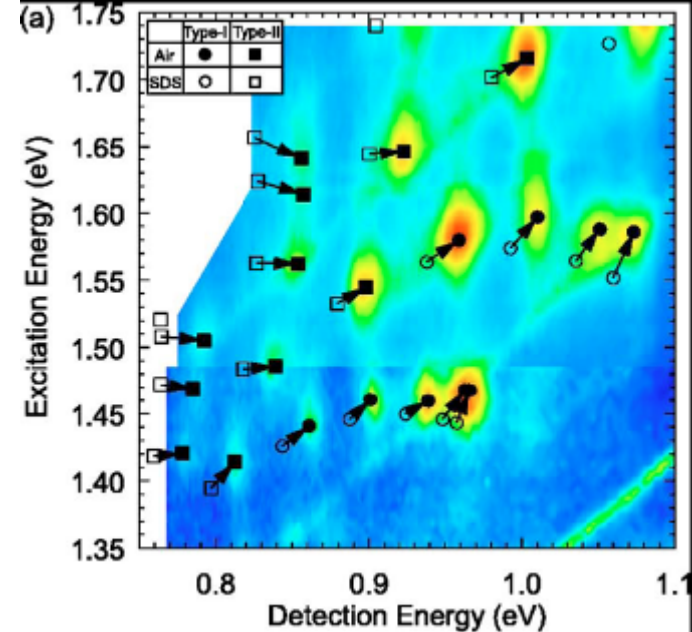
Dielectric screening of exciton.

Chirality dependent, type dependent

Effective mass



Y. Ohno et al., Phys. Rev. B 73, 235427 (2006)





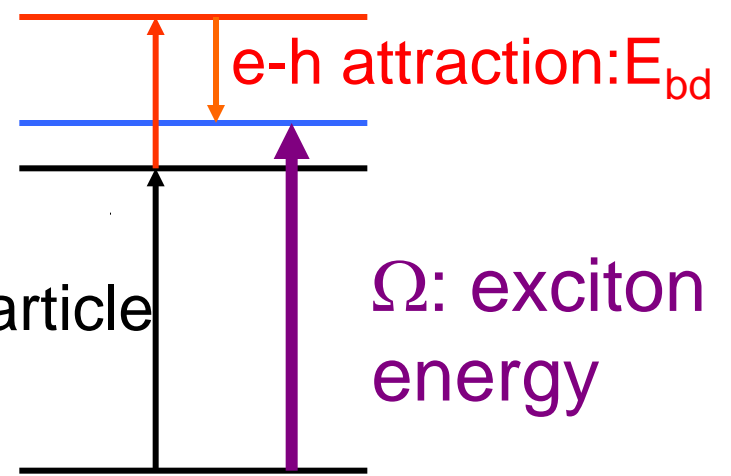
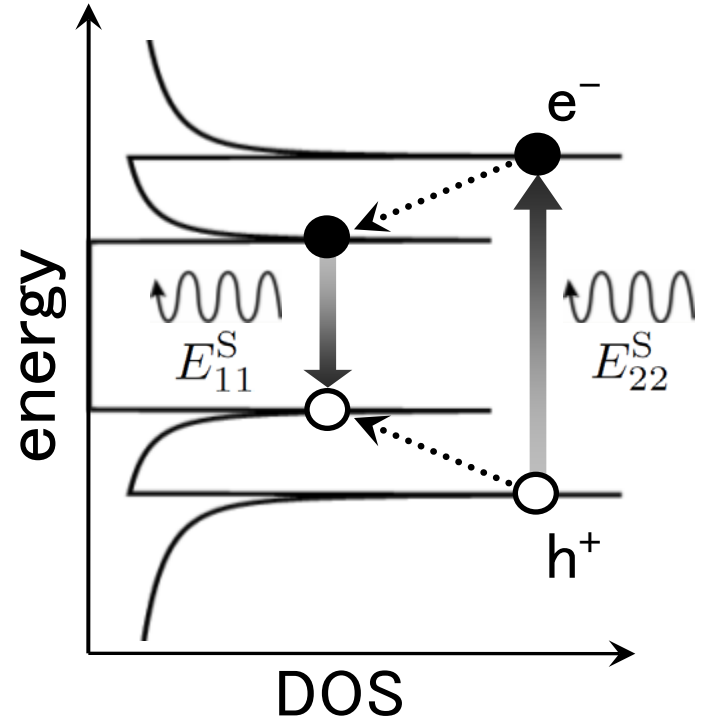
Dielectric screening of the Coulomb interaction

J. Jiang et al. *Phys. Rev. B* 75 035405 and 035407(2007)

Many body term is modified.



e-e repulsion (self energy)



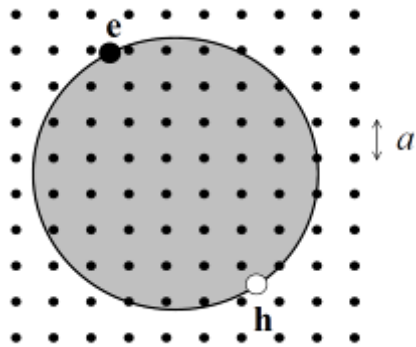
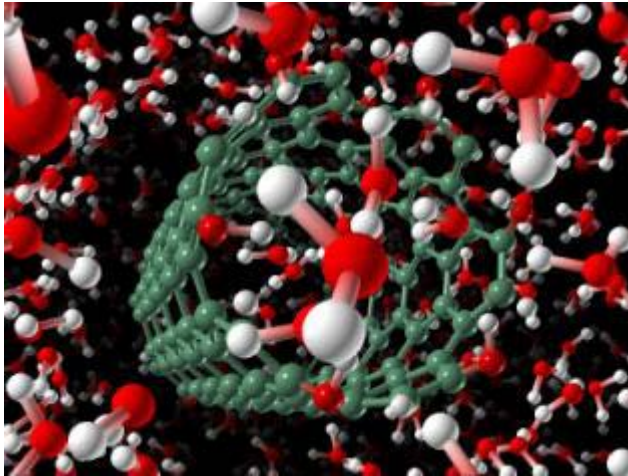
Ω decreases with increasing κ

κ : dielectric constant

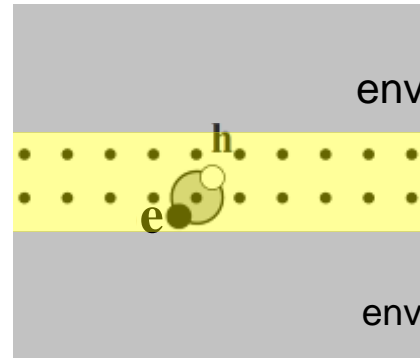
T. Ando, JPSJ 66, 1066 (97), (04), (05)
 S. D. Spataru et al. PRL 92, 077402(04).
 V. Perebeinos, et al. PRL. 92, 257402(04)
 J. Maultzsch et al. PRB 72 2414026(05)

Environmental effect of excitons in SWNTs

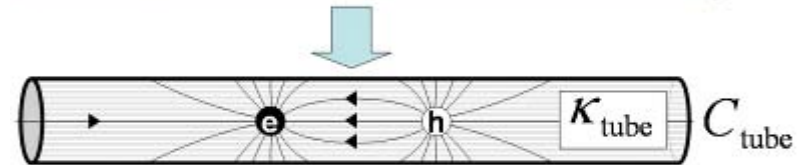
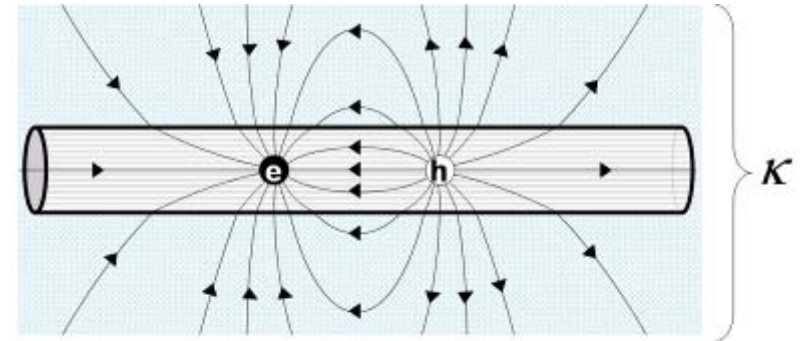
Y. Miyauchi et al. , *Chem. Phys. Lett* 442, 394 (2007)



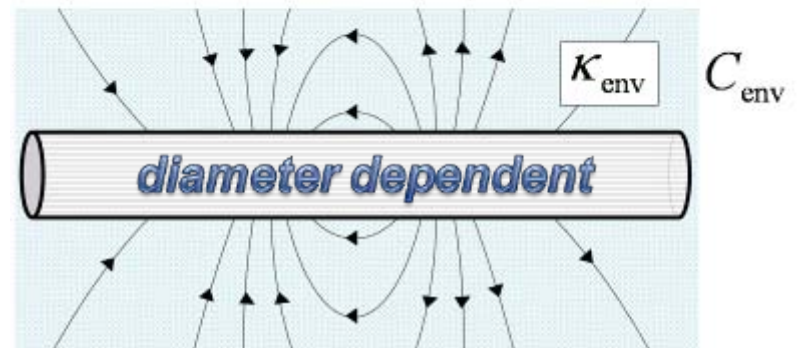
2D(3D) exciton



1D exciton



+

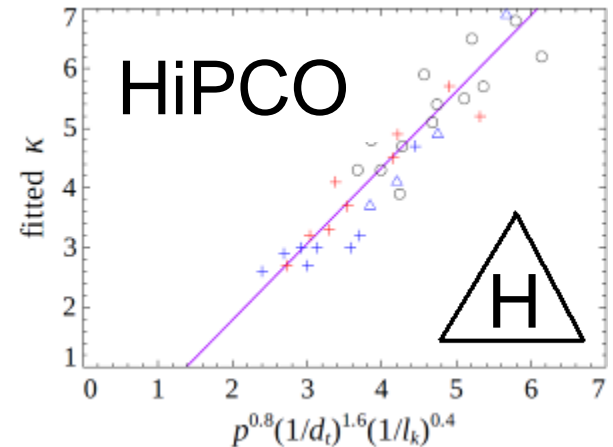
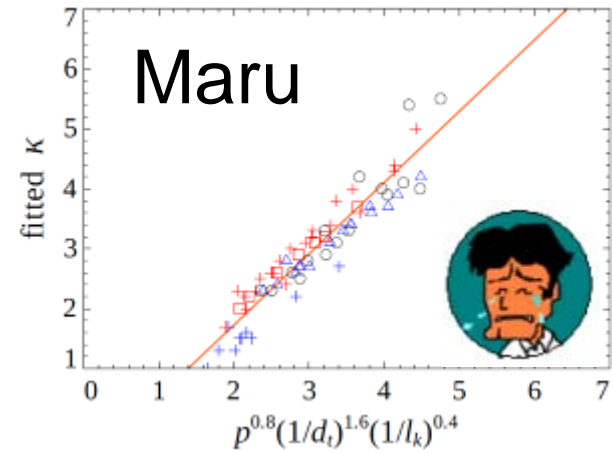
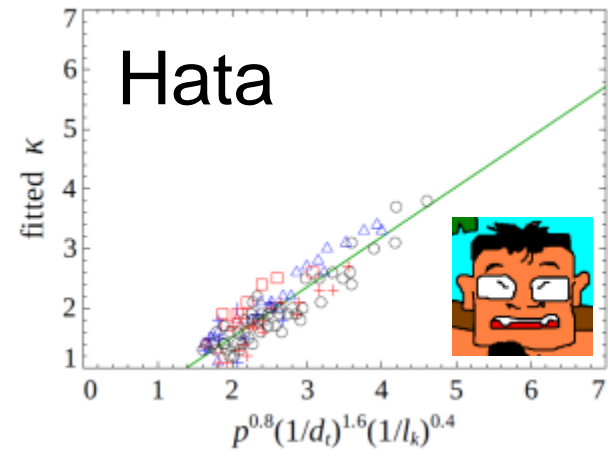
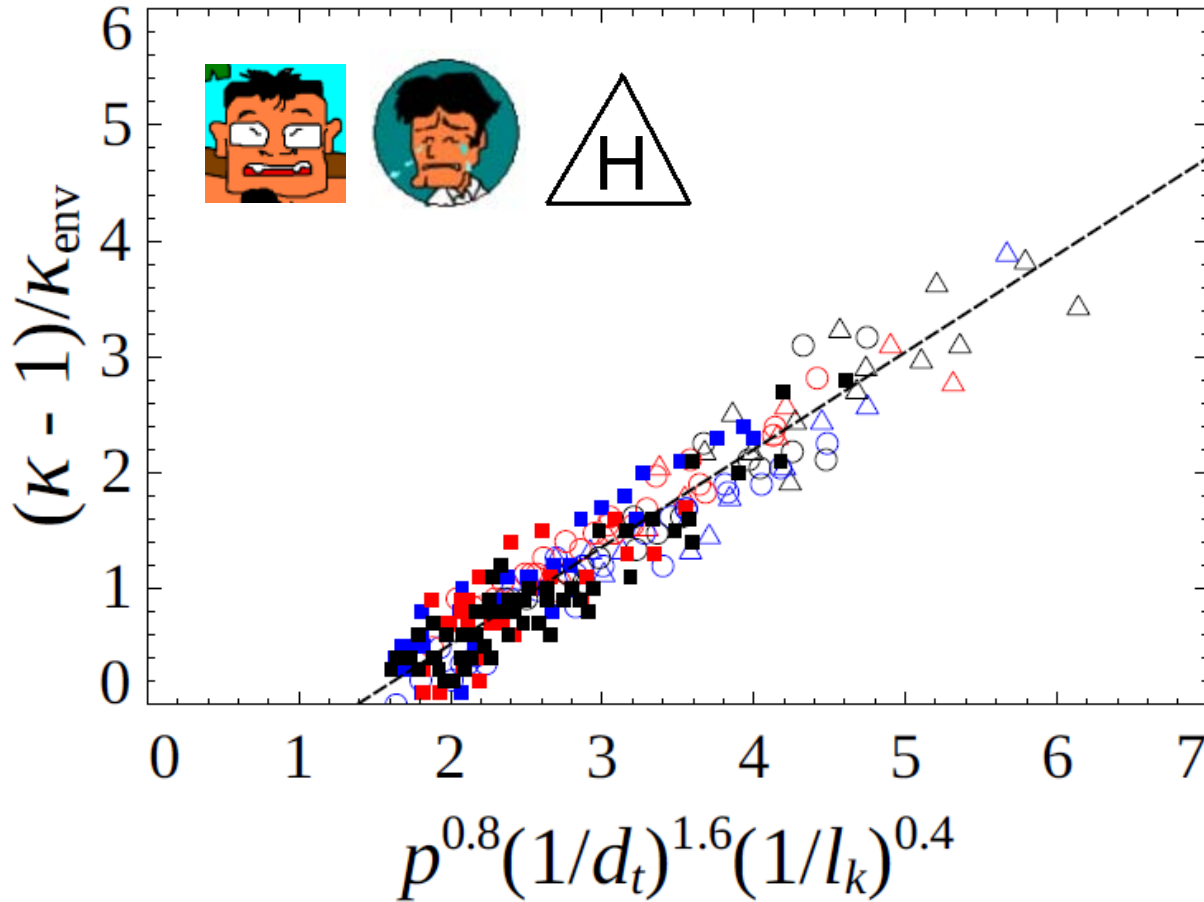


$$\frac{1}{K} = \frac{C_{\text{tube}}}{K_{\text{tube}}} + \frac{C_{\text{env}}}{K_{\text{env}}}$$



Exciton scaling function

A. R. T. Nugraha et al, APL 97, 091905, (2010)



$$K_{env}^{SG} : K_{env}^{alc.ass} : K_{env}^{HiPco} = 1.00 : 1.42 : 1.52$$

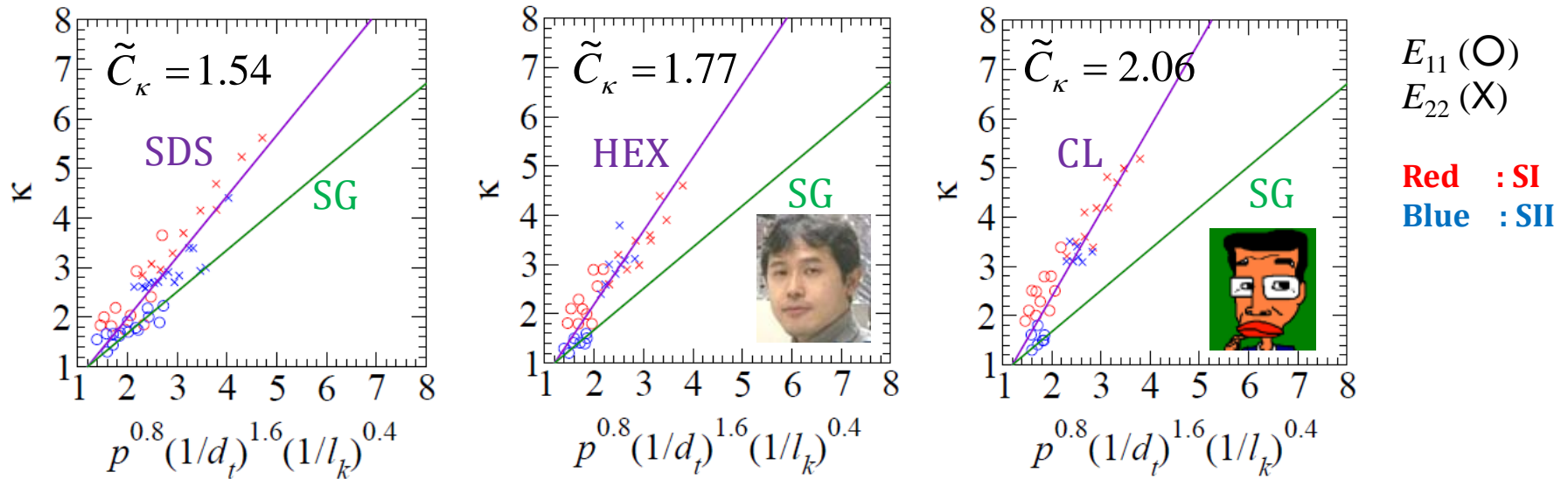
Only slope is different!



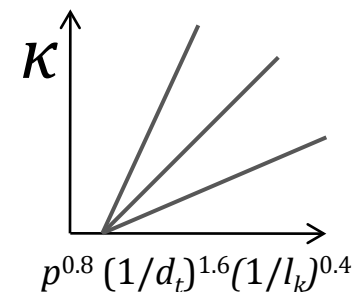
Web Pages of Exciton Kataura Plot

<http://flex.phys.tohoku.ac.jp/eii/>

□ Data from photoluminescence spectroscopy

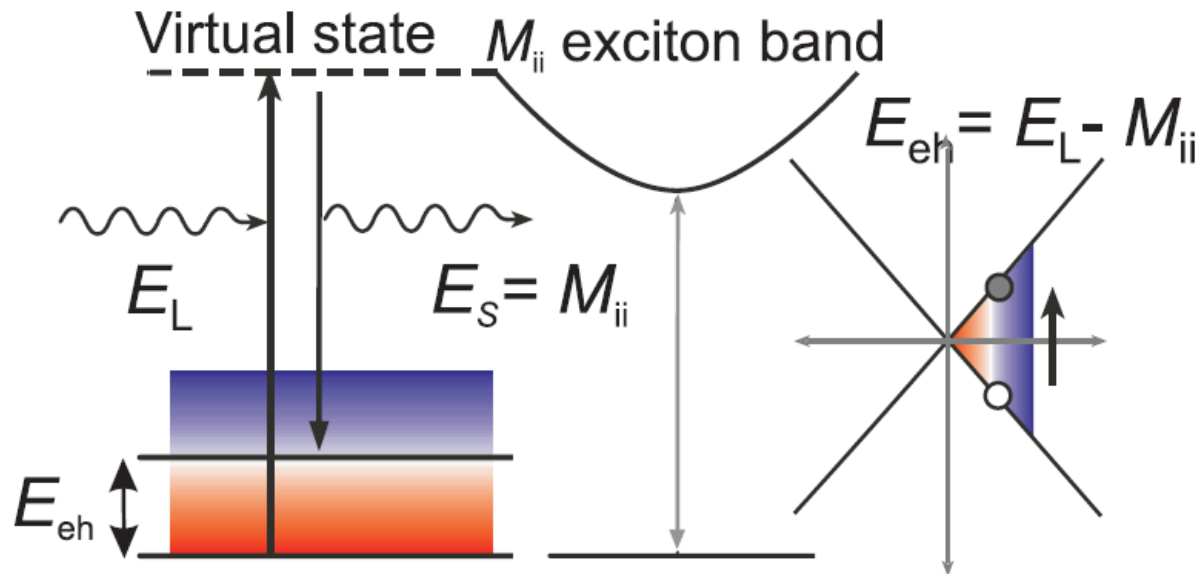


Measurement	RRS			PL		
	Synthesis method (Environment)	RRS	PL	Synthesis method (Environment)	RRS	PL
\tilde{C}_κ	SG (as-grown)	ACCVD (as-grown)	HiPco (SDS)	HiPco (SDS)	ACCVD (HEX)	ACCVD (CL)
	1.00 ± 0.08	1.42 ± 0.03	1.52 ± 0.05	1.54 ± 0.05	1.77 ± 0.04	2.06 ± 0.06



Electronic Raman

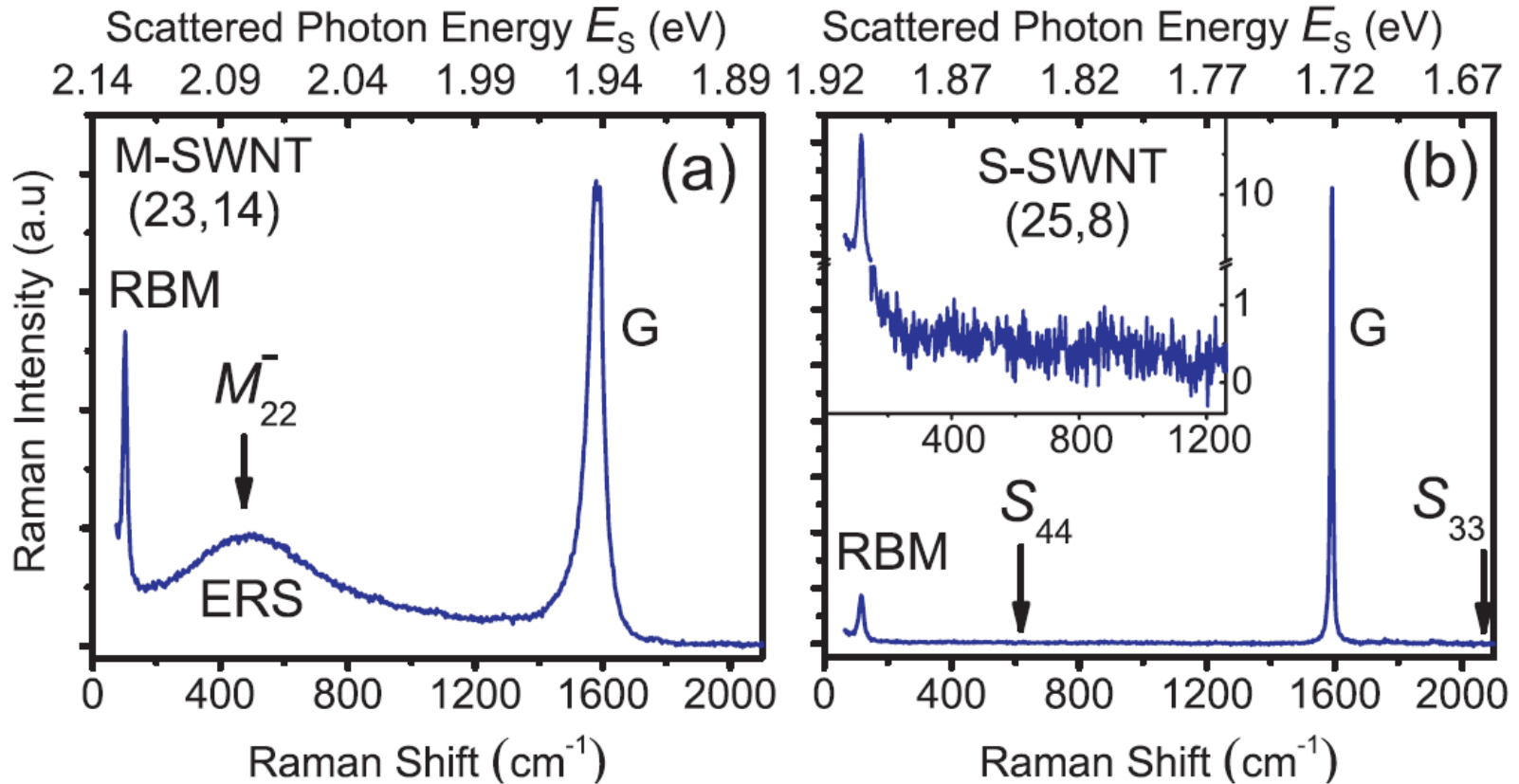
How to characterize metallic SWNTs?





Observation of Electronic Raman Scattering

Farhat, et al. Phys. Rev. Lett. 107, 1547401 (2011)

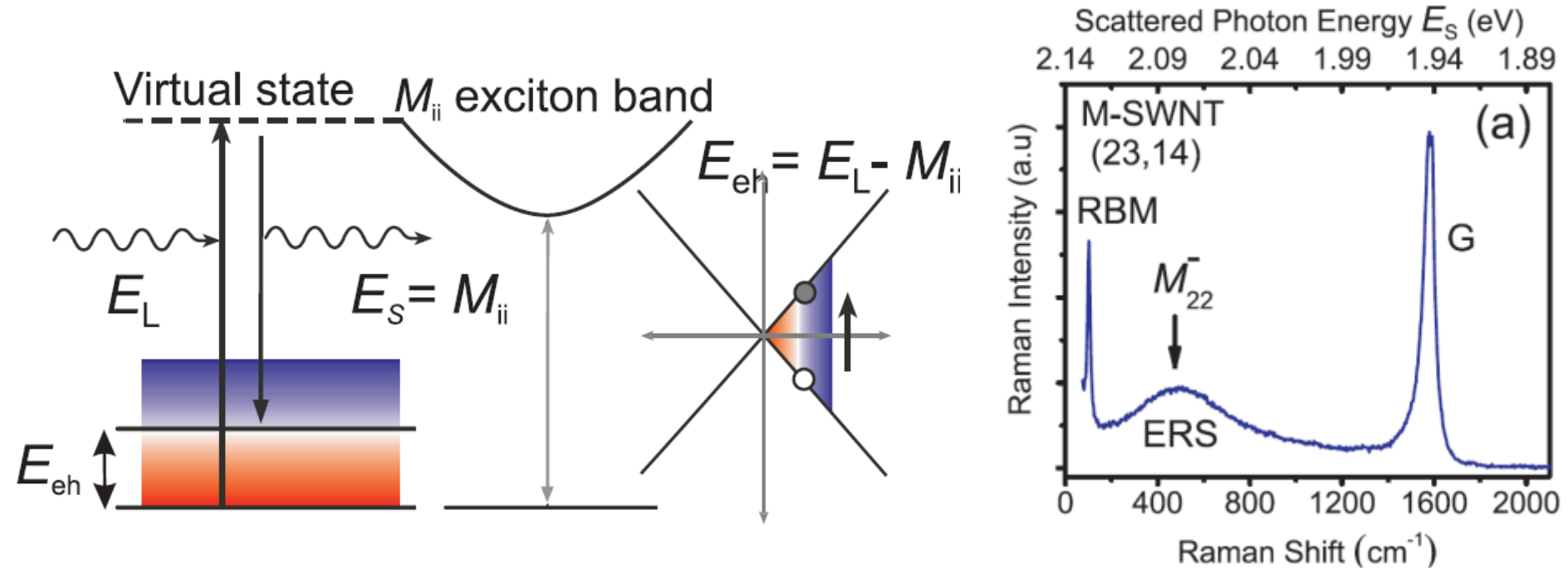


- ERS has no corresponding phonon mode
- ERS is observed only in MSWNT, with peak at M_{ij}



ERS mechanism

Farhat, et al. Phys. Rev. Lett. 107, 1547401 (2011)



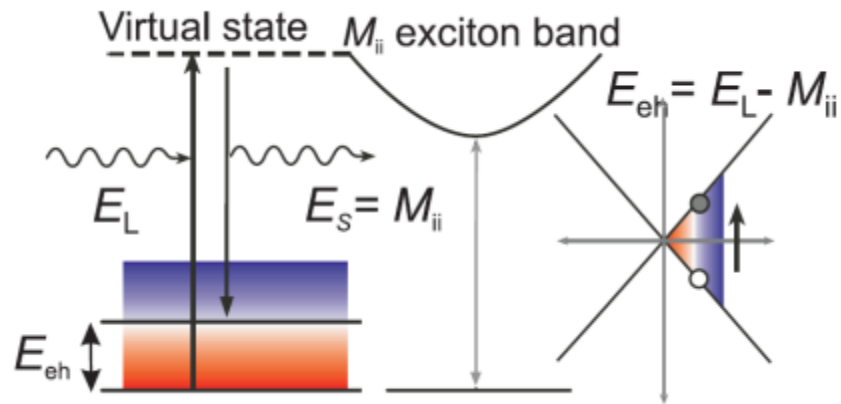
Electronic excitation around linear band by Coulomb interaction (broad spectra \rightarrow fast process 10fs)
No M22 PL, optical forbidden e-h excitation.



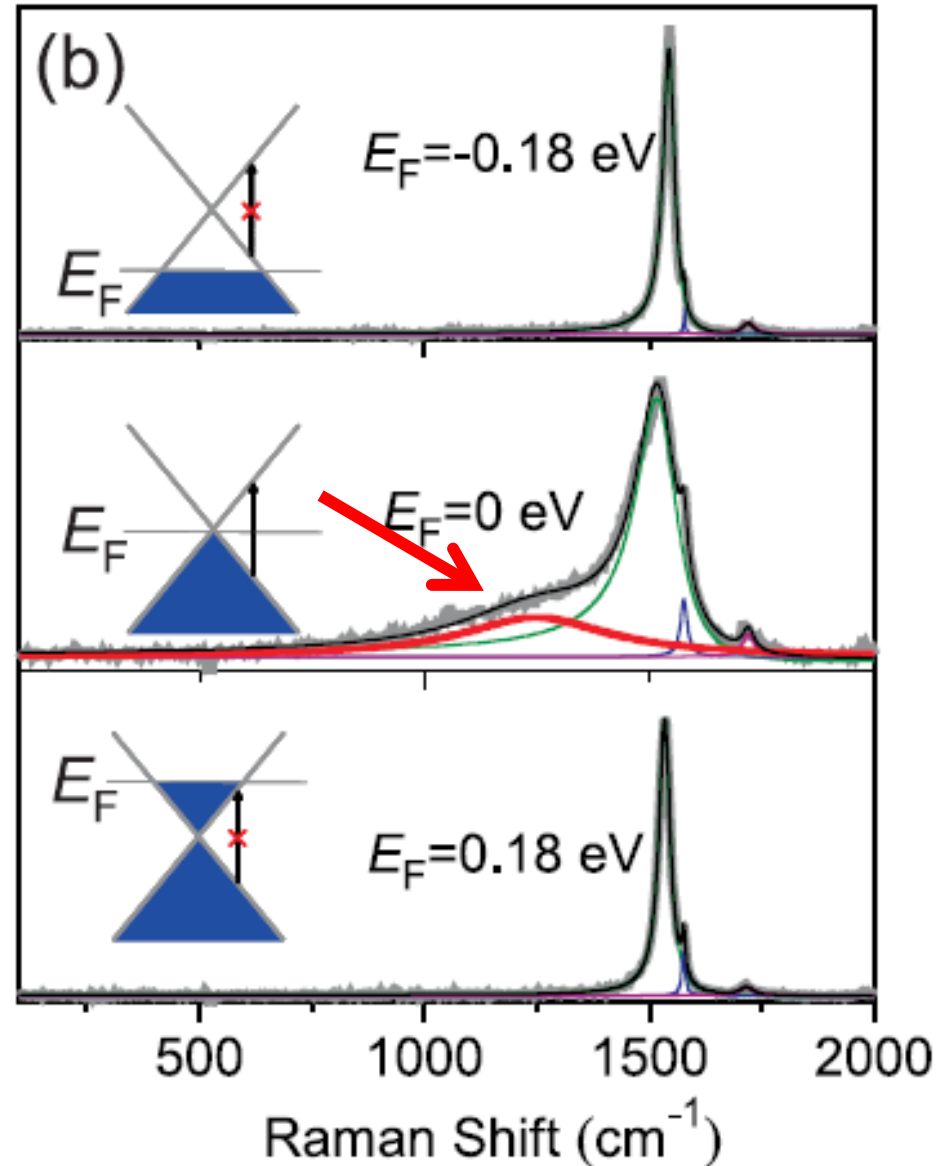
Gate dependence of ERS

Farhat, et al. Phys. Rev. Lett. 107, 1547401 (2011)

Changing E_F
suppresses ERS
→ Evidence that e-h
excitation is essential.



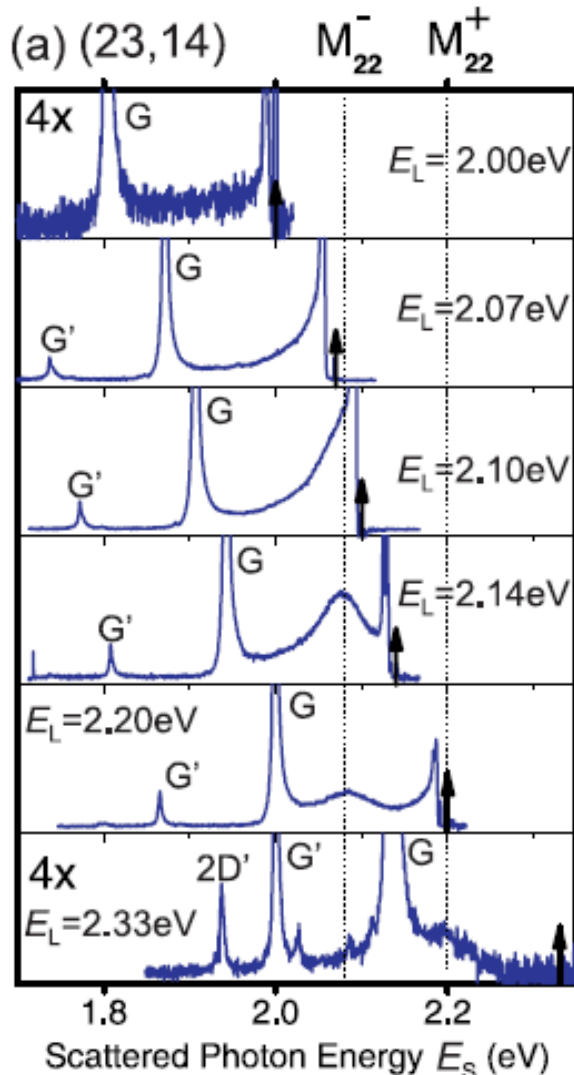
$q=0$ Coulomb interaction





The ERS peak modifies phonon G band

Farhat, et al. Phys. Rev. Lett. 107, 1547401 (2011)

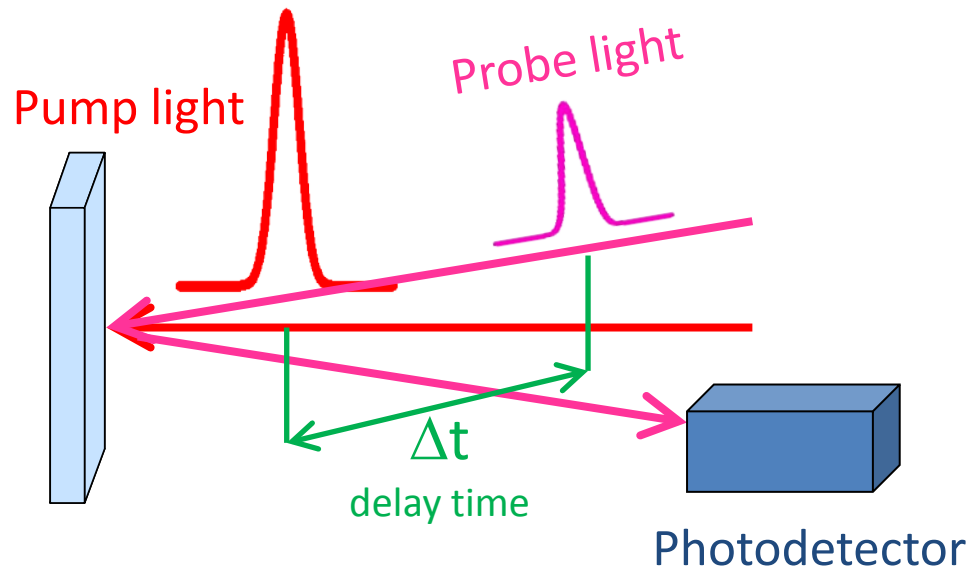


The farther laser energy from resonance, the broader ERS feature
More asymmetric G band.

Origin of BWF lines
(asymmetric broadening of G-band Raman)

Coherent phonon

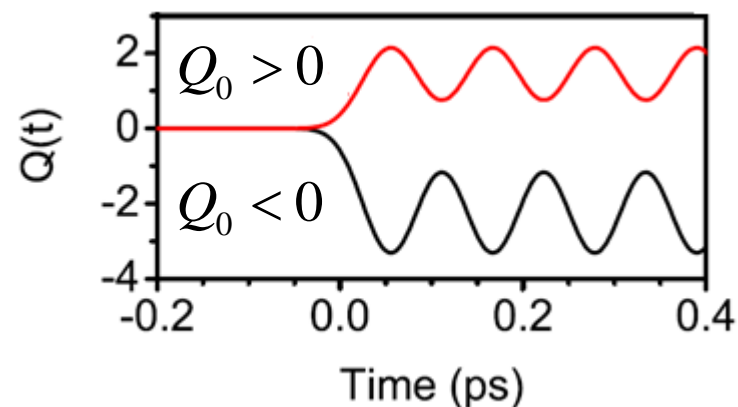
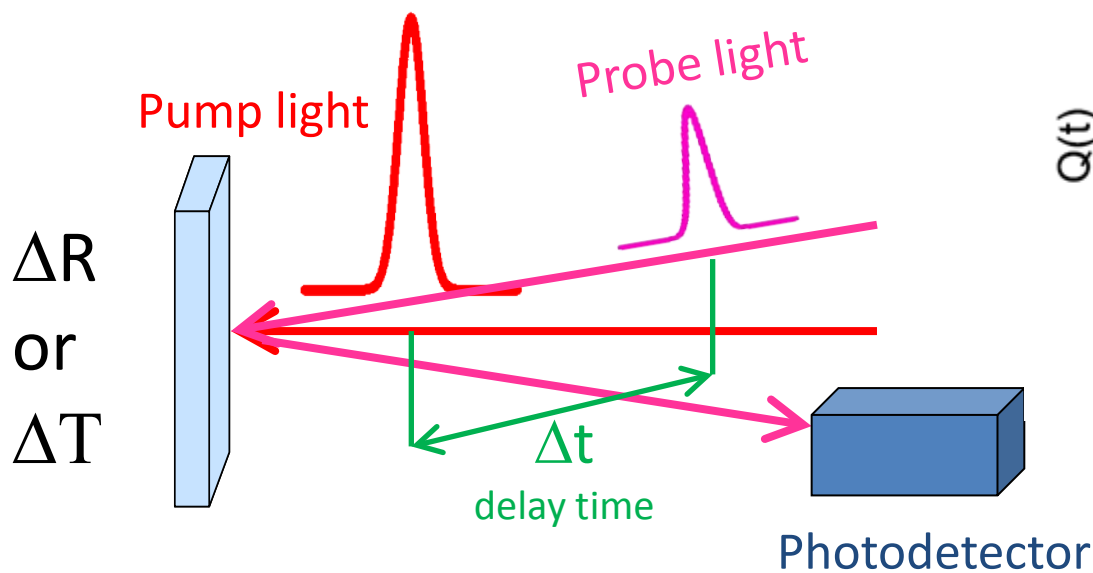
How to know the relaxation of photo-excited electron as a function of time?





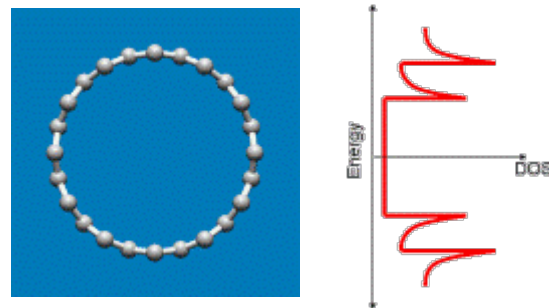
Coherent phonon Spectroscopy of nanotube

$$\tau_{\text{pulse}} \ll T_{\text{phonon}}$$

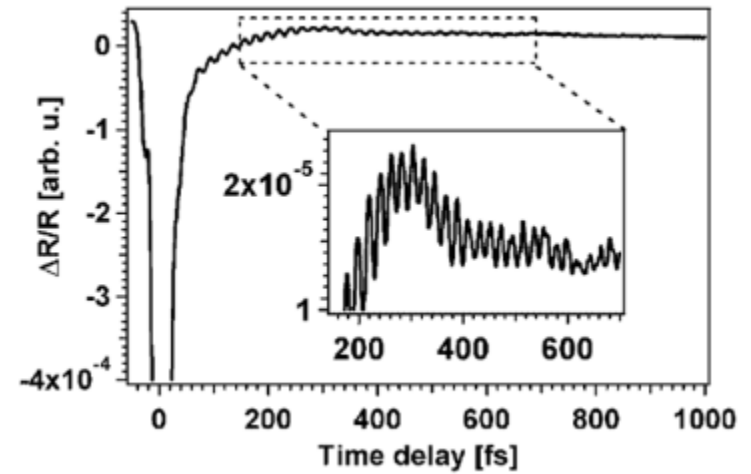
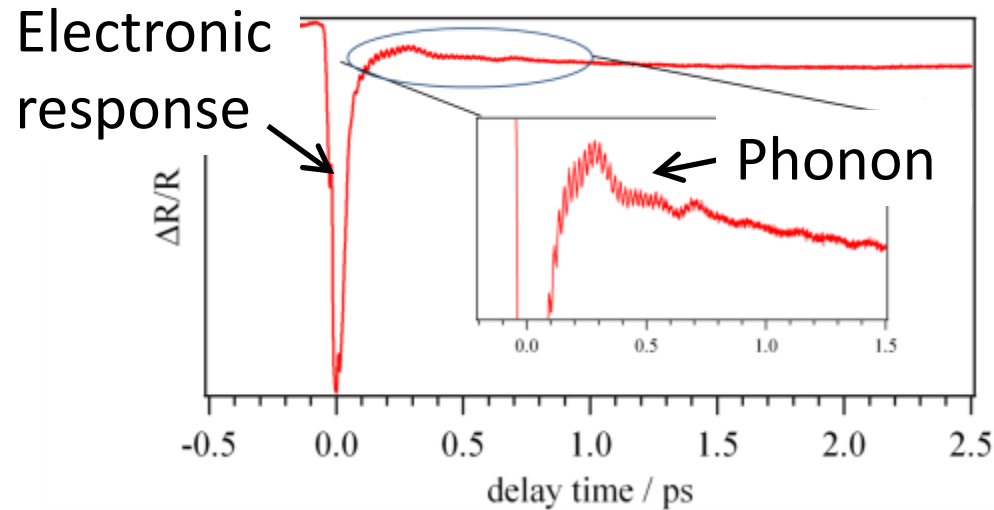


CP RBM amplitude

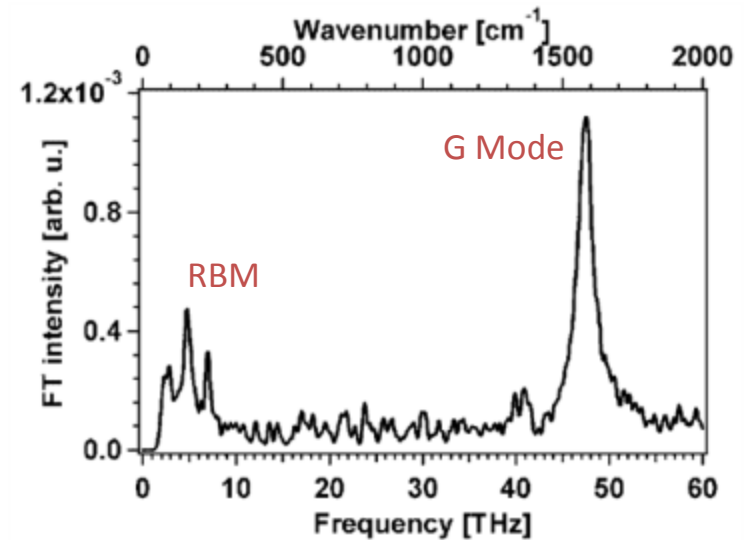
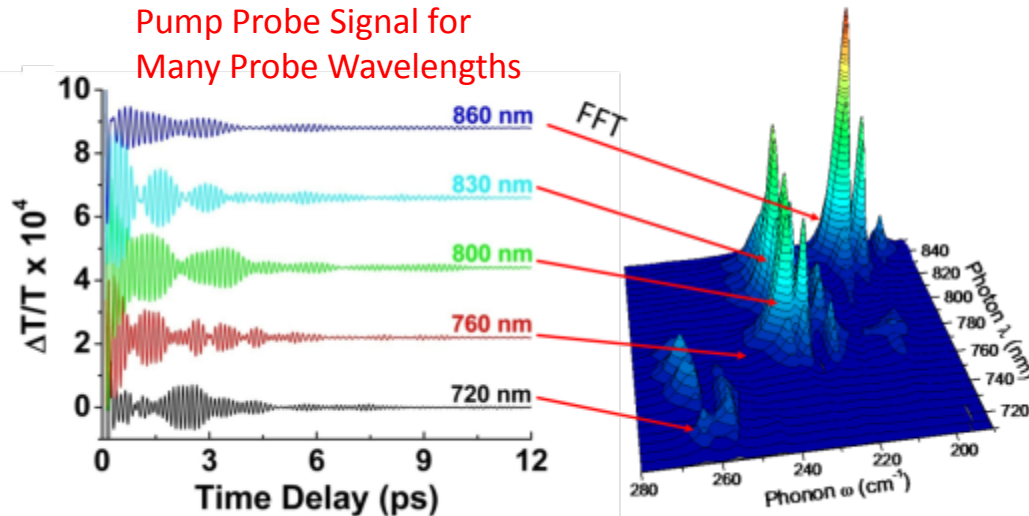
$$Q(t) = Q_0 (1 - \cos(\omega_{\text{RBM}} t))$$



Coherent phonons (CP) in carbon nanotubes



Fourier Transform

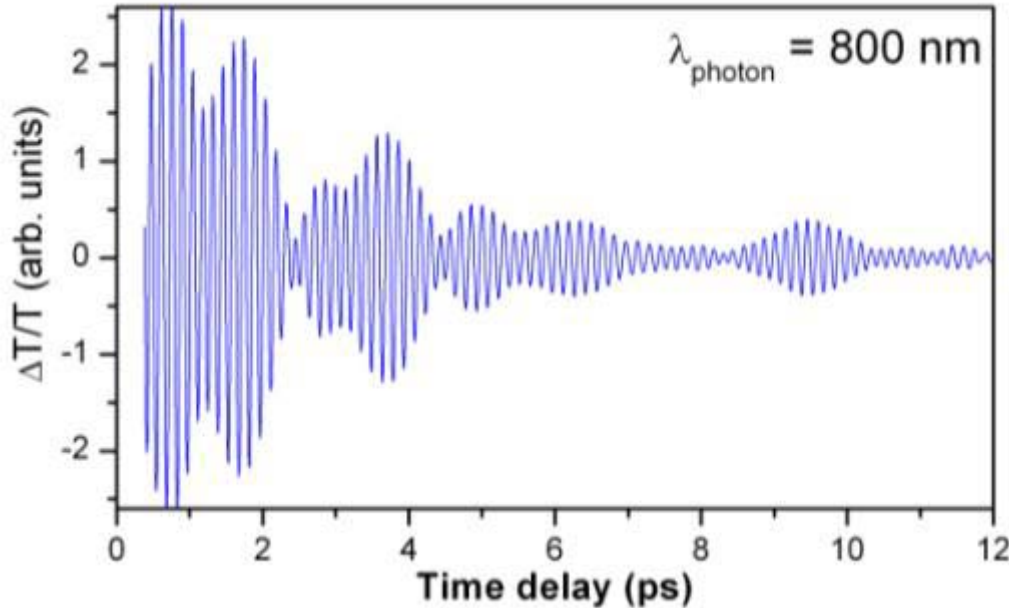


Y. S. Lim et al, *Nano Lett.* 6, 2696 (2006)

K. Kato et al, *Nano Lett.* 8, 3102(2008)

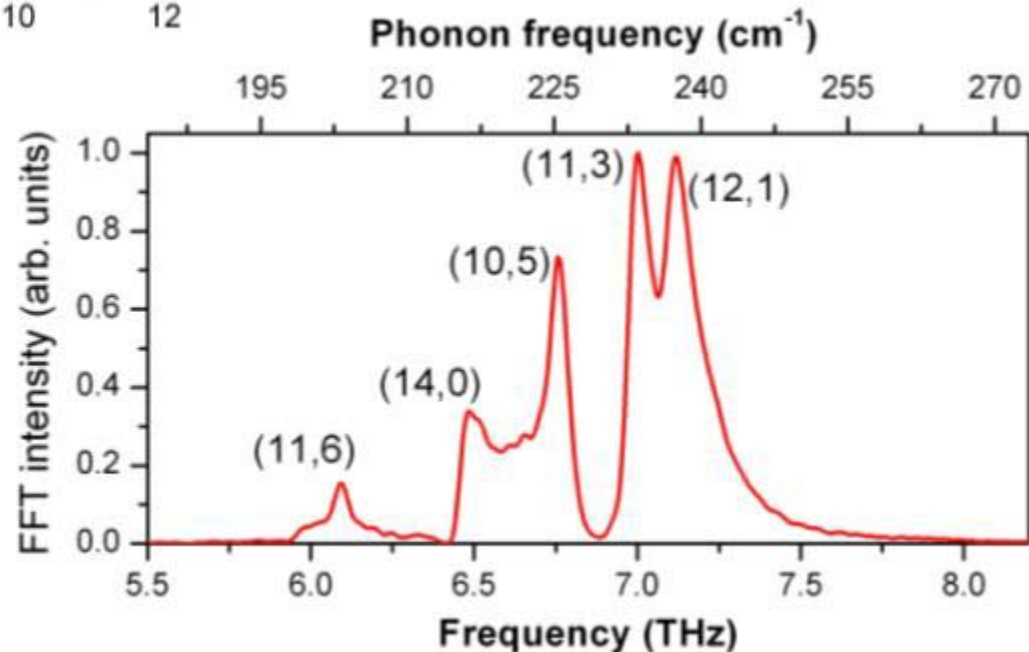


Chirality-dependent frequency



Radial Breathing Mode (RBM)

Kono group
(Rice University)

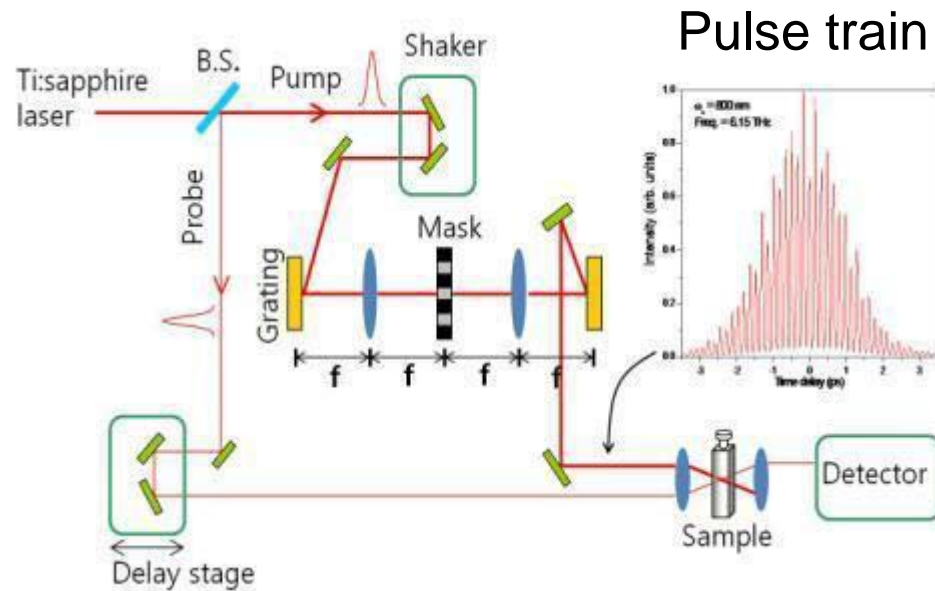


- Nano Lett. 6, 2696 (2006)
- Phys. Rev. Lett. 102, 037402 (2009)
- Phys. Rev. B 79, 205434 (2009)
- ACS Nano 4, 3222 (2010)



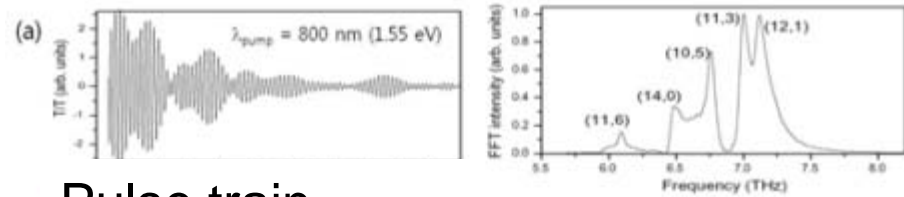
Pulse train excitation

J.-H. Kim et al., PRL 102, 037402 (2009)

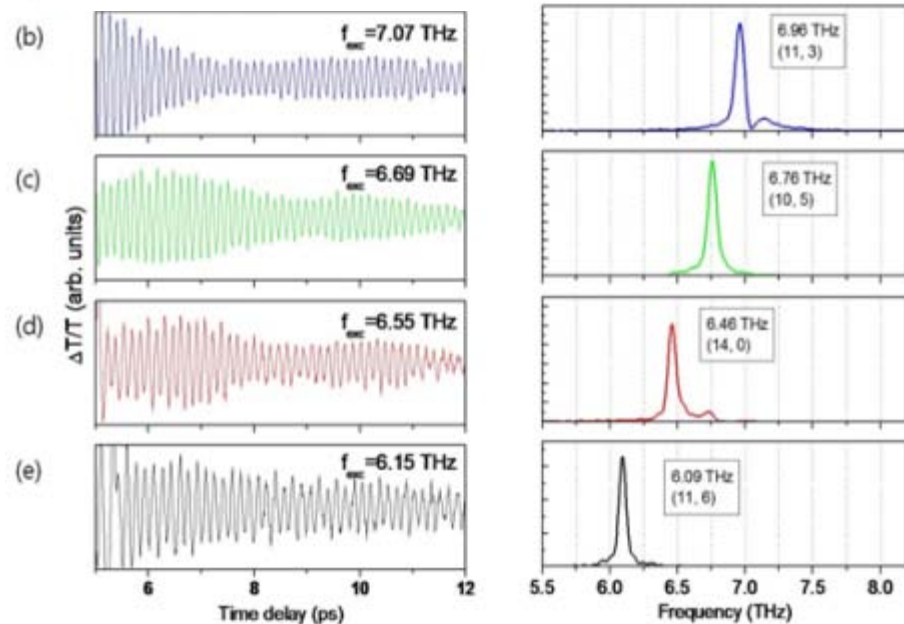


Pump pulses with frequency of ω_{RBM}

Single pulse



Pulse train

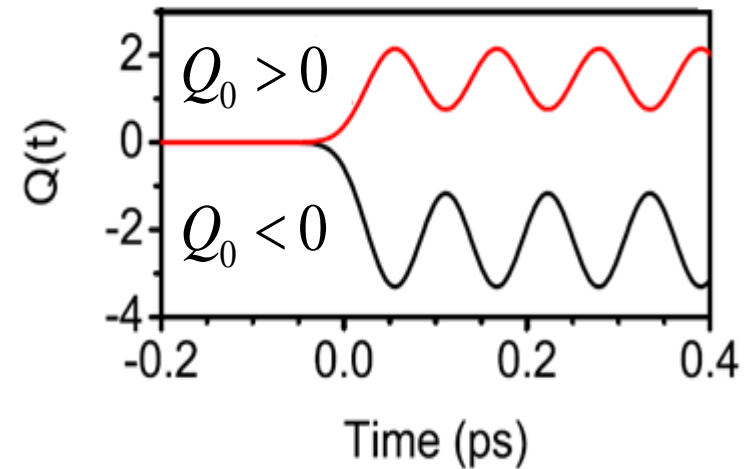
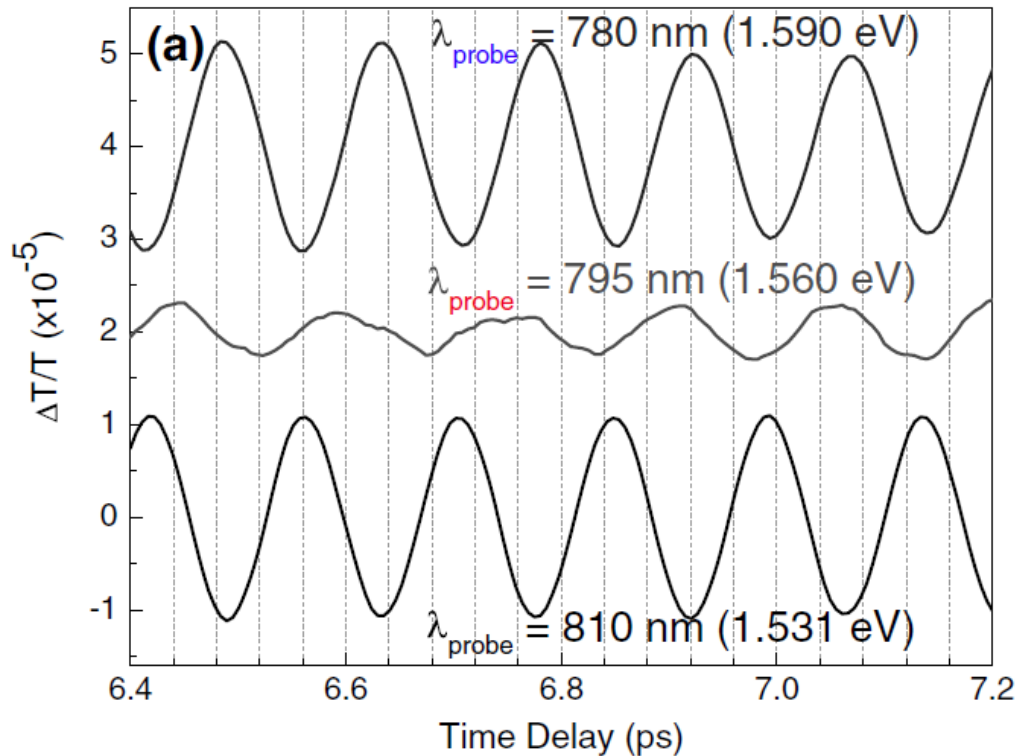




Wavelength dependent CP amplitude

J.-H. Kim et al., PRL 102, 037402 (2009)

(11,3) tube



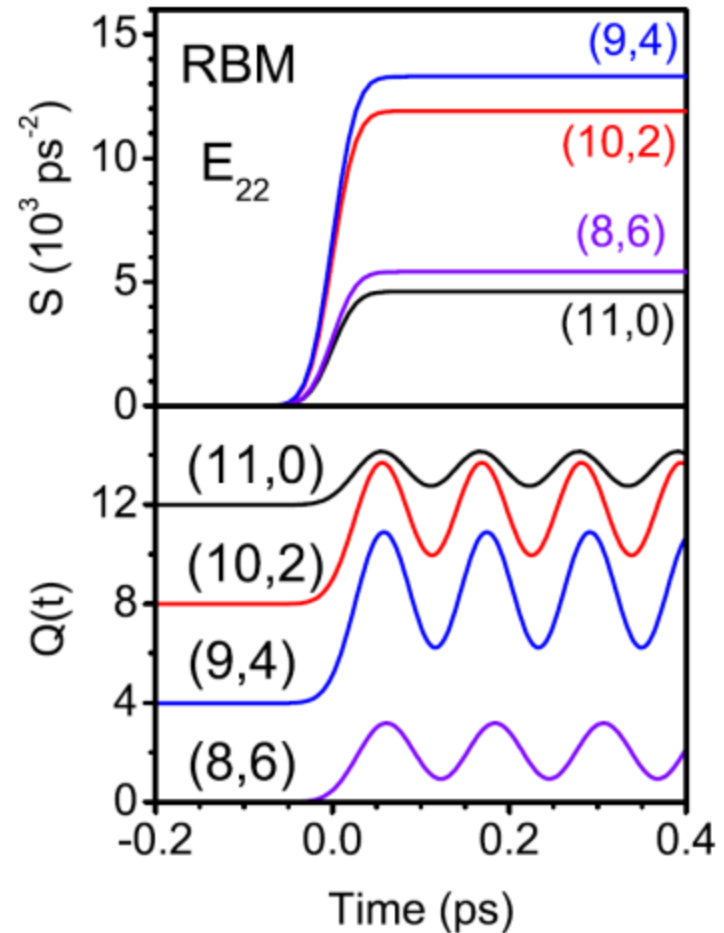
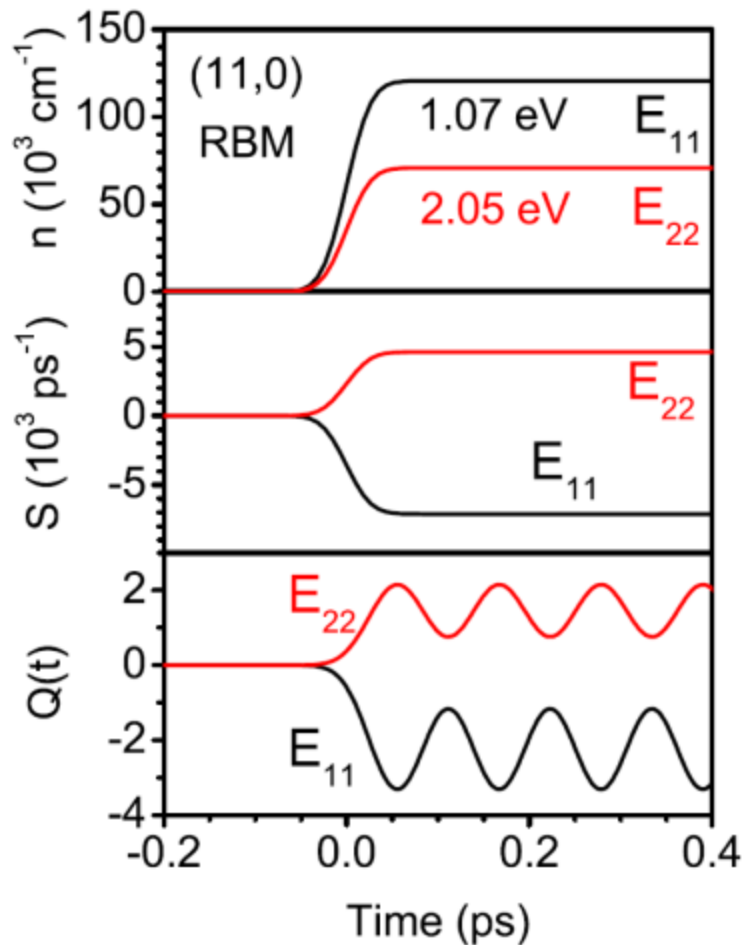


Family behavior of CP amplitude

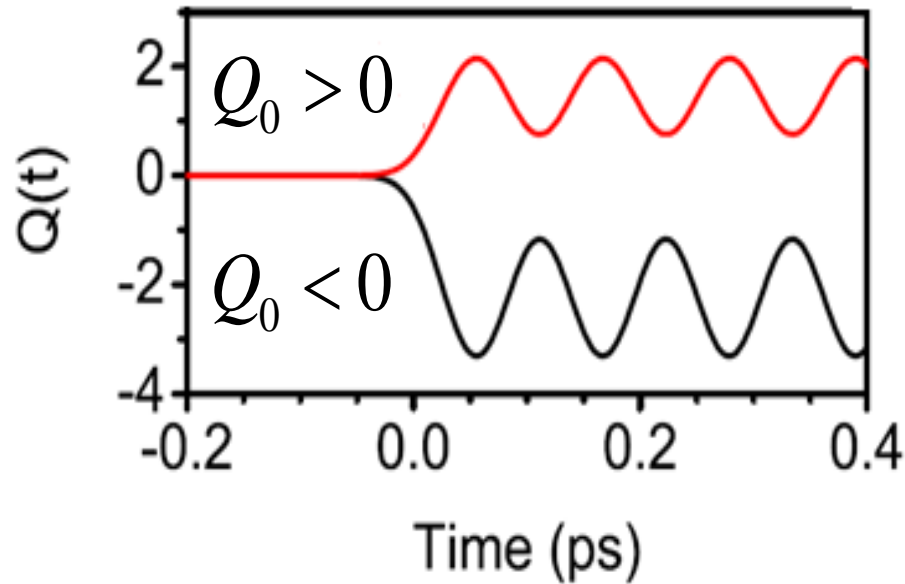
G. Sanders et al, Phys. Rev. B 79, 205434 (2009)

E11 and E22 for (11,0)

Family number $2n + m = 22$



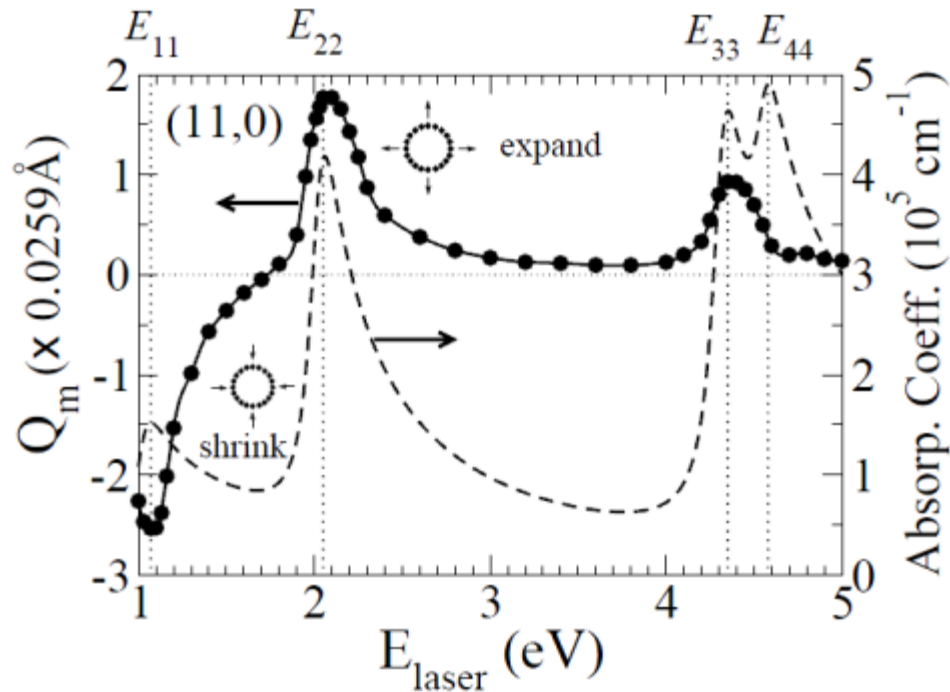
To expand or to shrink,
that is the question.





Resonance behavior of CP amplitude

Nugraha et al, Phys. Rev. B 84, 174302 (2011).



$$\frac{\partial^2 Q_\beta(t)}{\partial t^2} + \omega_\beta^2 Q_\beta(t) = S_\beta(t)$$

$$S_\beta(t) = \sum_{\mu k} S_\mu^\beta(k) [f_{c\mu}(k) - f_{v\mu}(k)]$$

contains M_{op}

$$S_\mu^\beta(k) = -\frac{2\omega_\beta}{\hbar} [M_{c\mu}^\beta(k) - M_{v\mu}^\beta(k)]$$

Magnitude of oscillations

$$|Q| \propto |M_{el-ph}| \cdot |M_{op}|$$

Shrink or Expand?

M_{el-ph}
sign (+/-) of el-ph matrix



Effective mass model for RBM el-ph interaction

K. Sasaki et al, Phys. Rev. B 78, 235405 (2008)

For zigzag tubes:

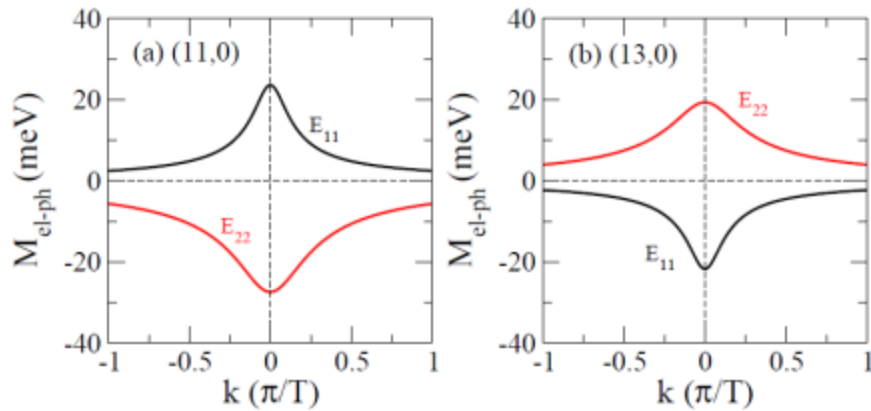
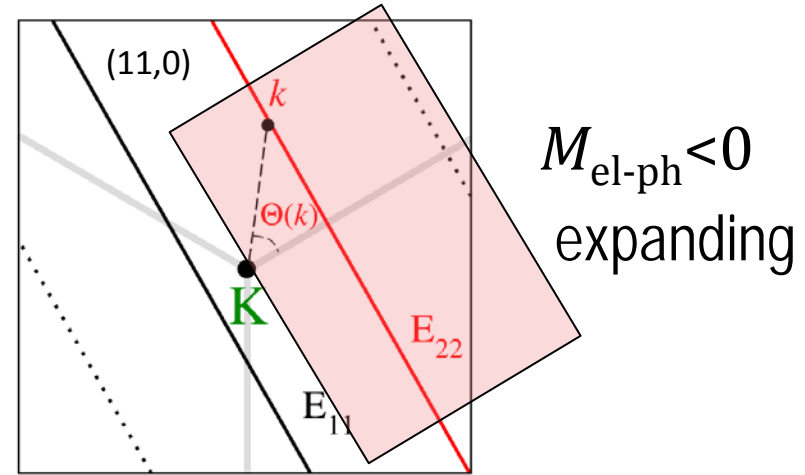
$$M_{\text{el-ph}}^c = \langle c | H_{\text{el-ph}} | c \rangle = \frac{s_z}{d_t} (2g_{\text{on}} - g_{\text{off}} \cos \Theta(\mathbf{k}))$$

$$M_{\text{el-ph}}^v = \langle v | H_{\text{el-ph}} | v \rangle = \frac{s_z}{d_t} (2g_{\text{on}} + g_{\text{off}} \cos \Theta(\mathbf{k}))$$

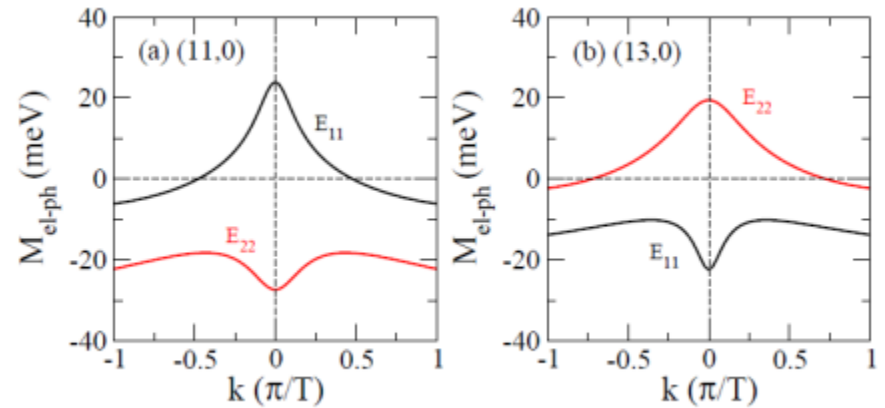
$$M_{\text{el-ph}} = M_{\text{el-ph}}^c - M_{\text{el-ph}}^v = \frac{s_z}{d_t} (-2g_{\text{off}} \cos \Theta(\mathbf{k}))$$

For chiral tubes:

$$M_{\text{el-ph}} = \frac{s_z}{d_t} (-2g_{\text{off}} \cos[\Theta(\mathbf{k}) + \theta])$$



Eff. mass Model

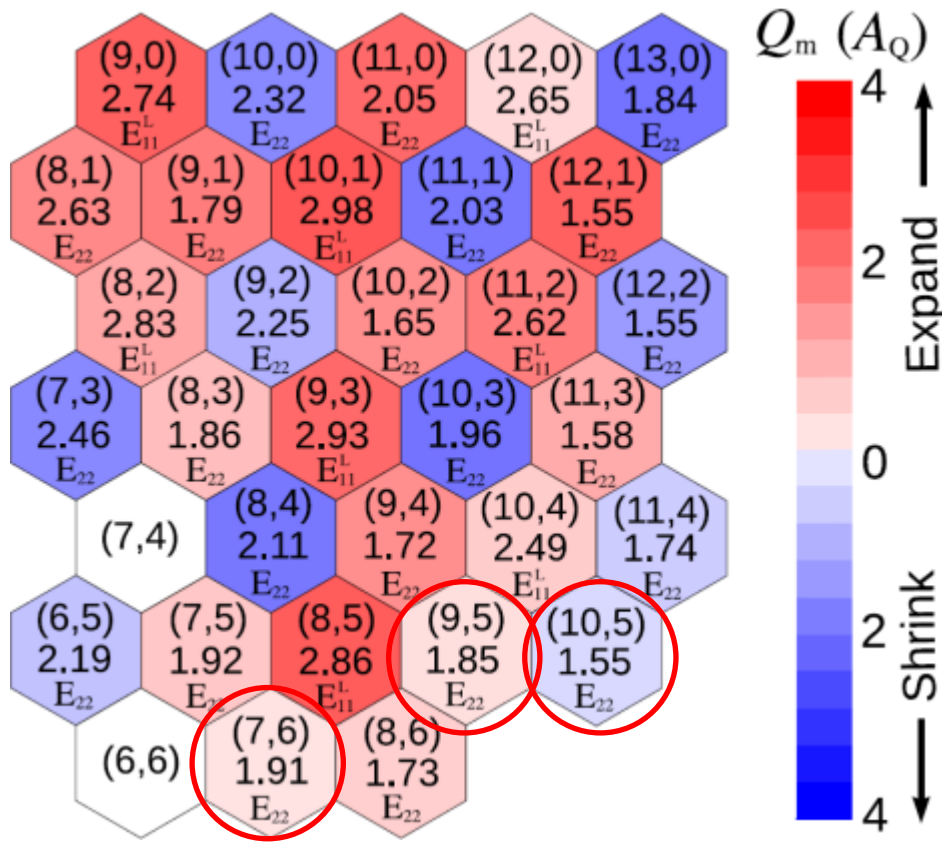


ETB Model

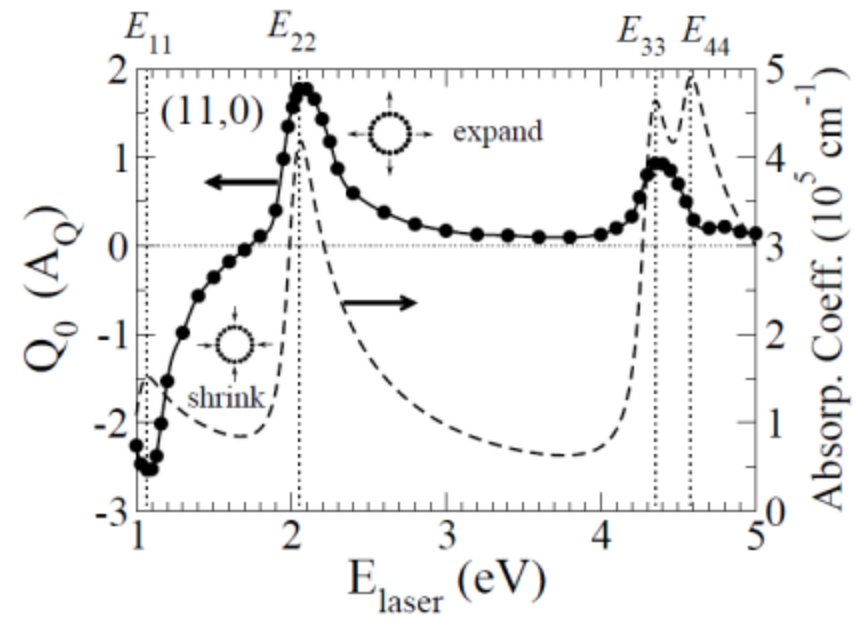


Map of coherent phonon amplitudes

Nugraha et al, Phys. Rev. B 84, 174302 (2011).



$$A_Q = \sqrt{\hbar / M \omega_{\text{RBM}}}$$



□ Deviated results from basic rules: (7,6), (9,5), (10,5) etc. → near-armchair tubes

$$M_{\text{el-ph}} = \frac{A_Q}{d_t} (-2g_{\text{off}} \cos[\Theta(\mathbf{k}) + 3\theta])$$

Phonon Softening

How do know the information of the Fermi energy?

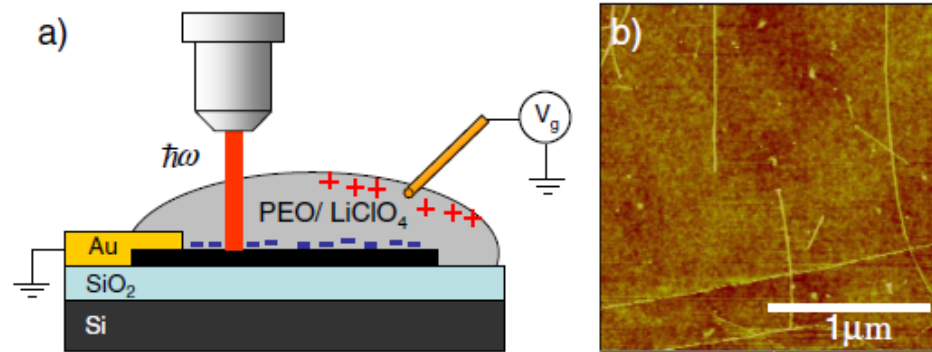


FIG. 1 (color online). (a) Schematic diagram of the experimental setup. The excitation laser shines through the PEO/LiClO₄ polymer electrolyte. (b) An AFM image indicating that the nanotubes are spaced out and are typically isolated from one another.

Electro-chemical doping and Raman spectroscopy of single wall carbon nanotubes



H. Farhat *et al.*, *Phys. Rev. Lett.*, 99 145506(2007)

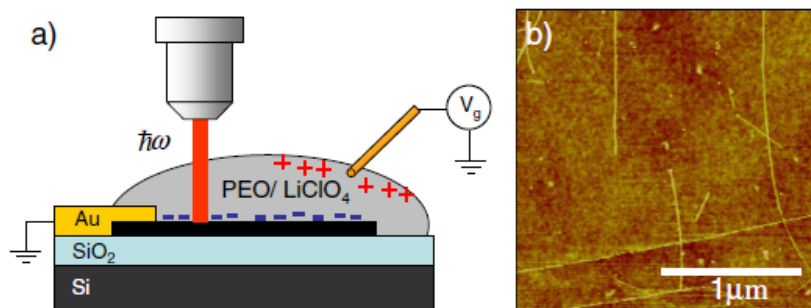
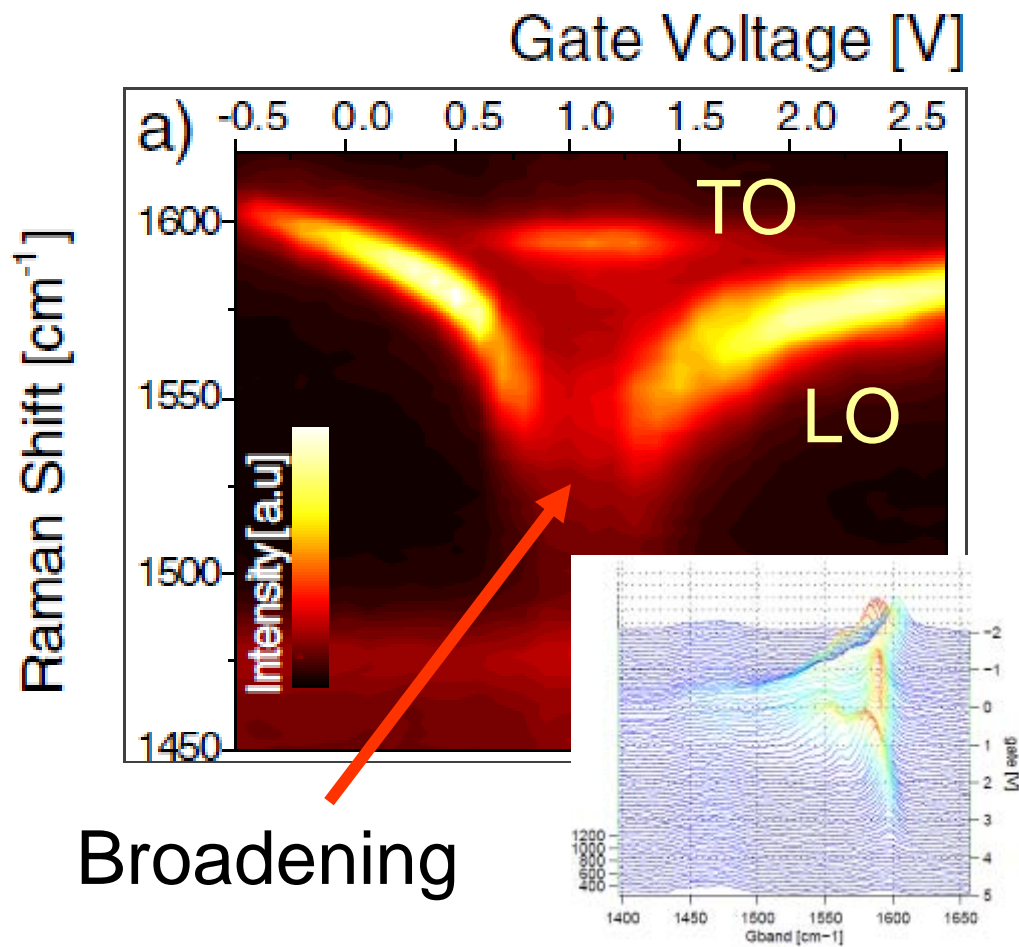


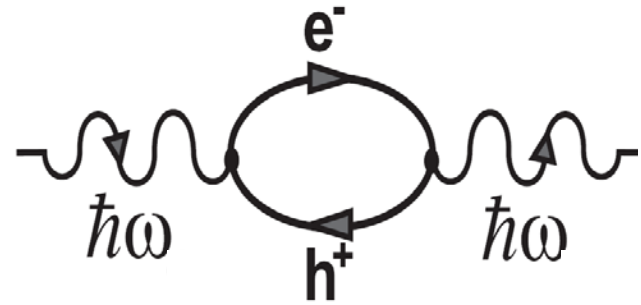
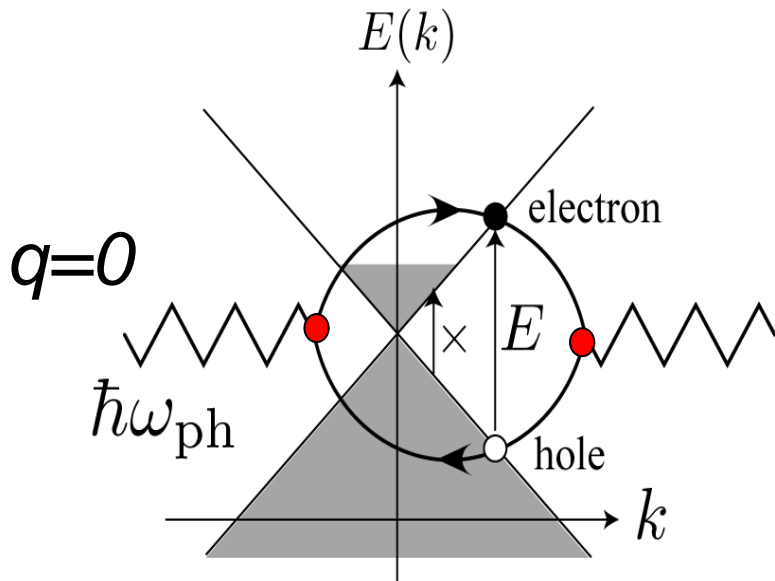
FIG. 1 (color online). (a) Schematic diagram of the experimental setup. The excitation laser shines through the PEO/LiClO₄ polymer electrolyte. (b) An AFM image indicating that the nanotubes are spaced out and are typically isolated from one another.

- isolated metallic SWNT
- E_F dependent
- upshift of TO?



Electron-phonon interaction in Graphene

Renormalization of phonon energy (Kohn anomaly)

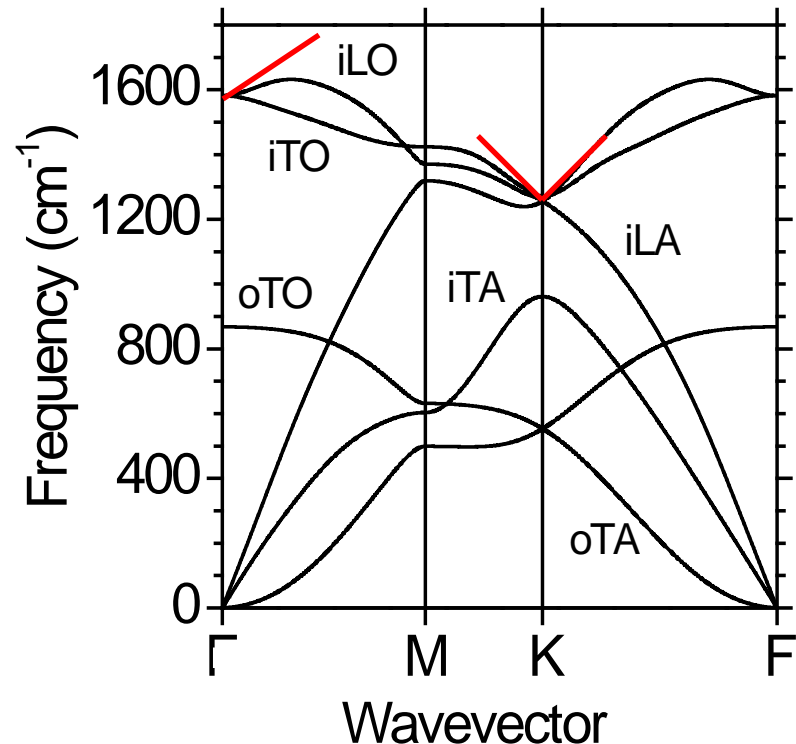


$$\hbar\omega = \hbar\omega^{(0)} + \hbar\omega^{(2)}$$

Piscanec et al. PRL (2004)

Ando et al, JPSJ (2006)

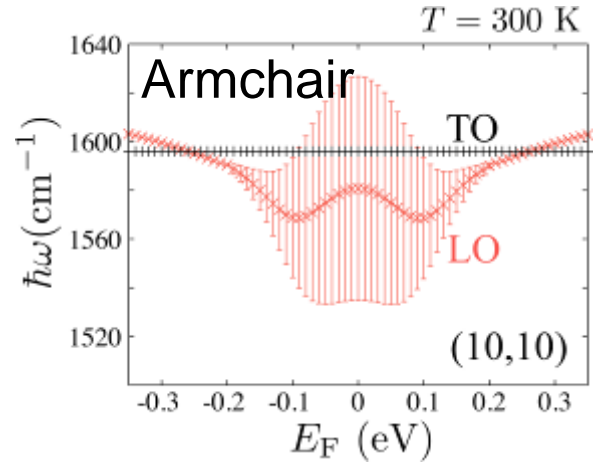
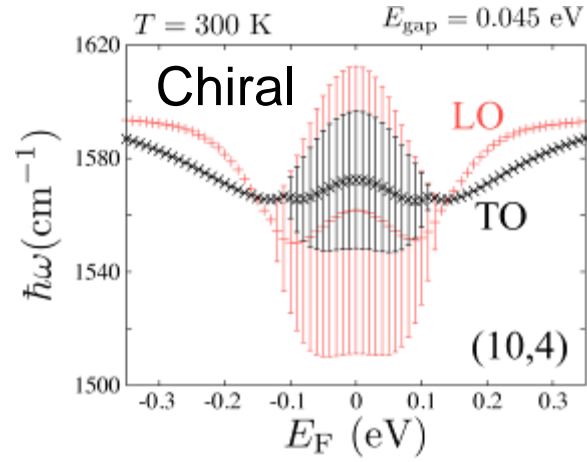
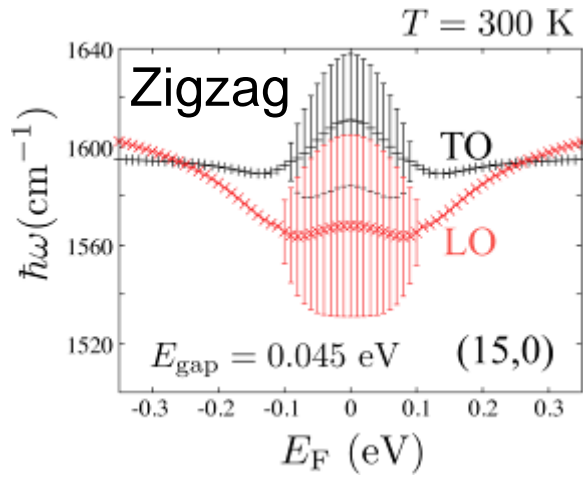
Sasaki et al. PR (2008)



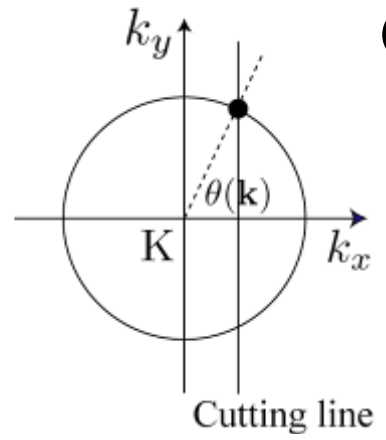
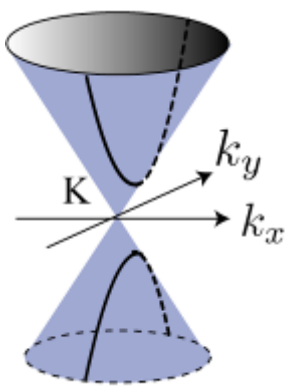


Chiral angle dependence of KA

K. Sasaki, R. Saito, et al. Phys. Rev. B, 77, 245441 (2008)



Why TO becomes hard for zigzag NT?



⊕ dependent el-ph interaction

$$\text{LO: } \langle eh(\mathbf{k}) | \mathcal{H}_{ep} | \omega_l \rangle = -igu \sin \theta(\mathbf{k})$$

$$\text{TO: } \langle eh(\mathbf{k}) | \mathcal{H}_{ep} | \omega_t \rangle = -igu \cos \theta(\mathbf{k})$$

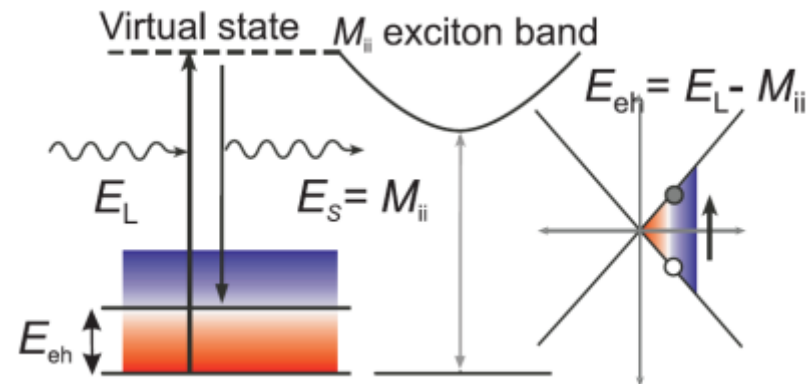
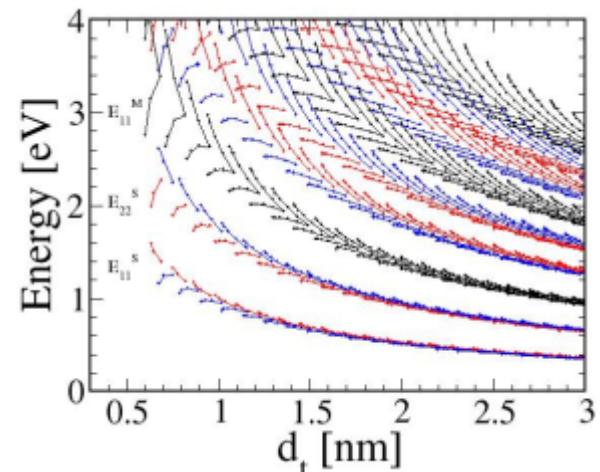
$$v_F(A_x(\mathbf{r}), A_y(\mathbf{r})) = g(u_y(\mathbf{r}), -u_x(\mathbf{r}))$$

K. Ishikawa and T. Ando, J. Phys. Soc. Jpn. **75**, 84713 (2006).

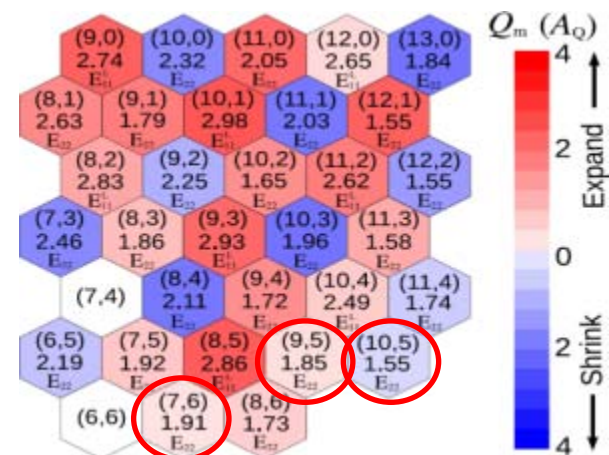
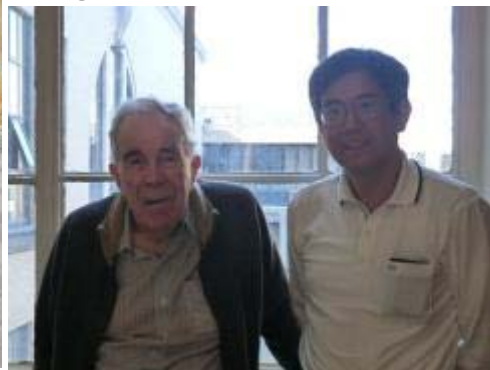
T. Ando, J. Phys. Soc. Jpn. **77**, 14707 (2008).

Summary of NTs

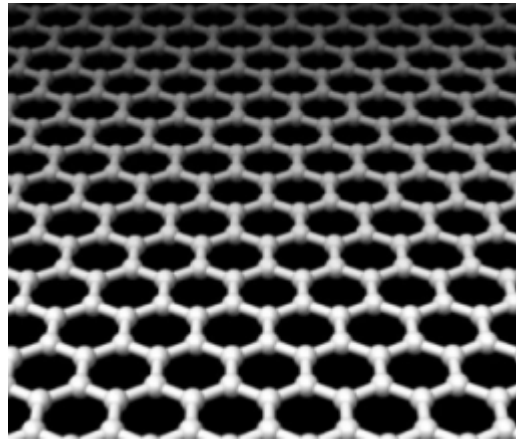
- Exciton Kataura Plot
 - environment effect
- Electric Raman spectra
 - Coulomb interaction
- Coherent phonon
 - expand/shrink map
- Kohn anomaly
 - Chirality dependnt



2011 MIT



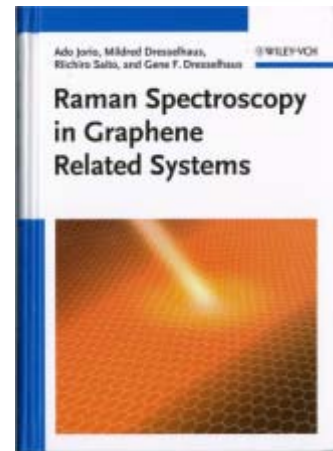
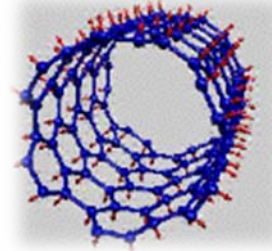
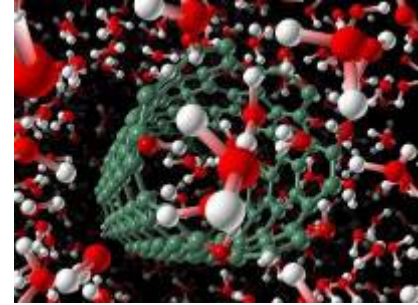
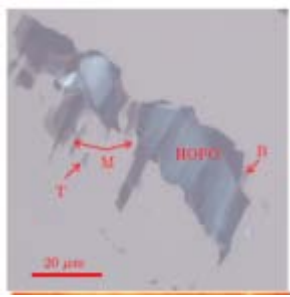
Raman Spectroscopy of graphene



Outline

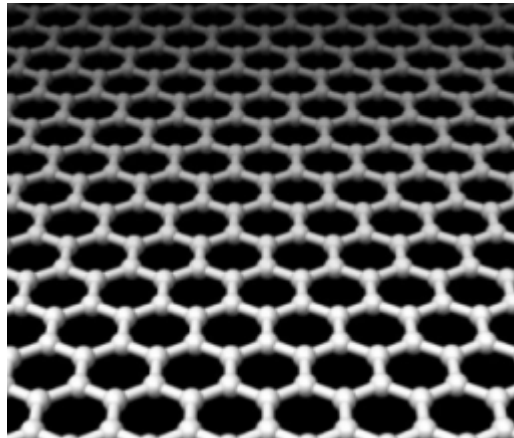
- Graphene Raman spectroscopy
 - Raman spectra of bilayer G (2LG)
 - ABA and ABC stacking order of 3LG
- Electro-Chemical doping
 - E_F dep. on double resonance Raman
 - origin of the 2450cm^{-1} peaks

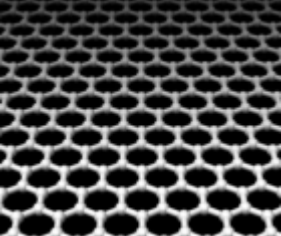
A. Jorio, R. Saito, G. Dresselhaus, M. S. Dresselhaus
"Raman Spectroscopy of graphene related systems"
Wiley-VCH, in press (2011)



Raman Spectroscopy of bilayer graphene

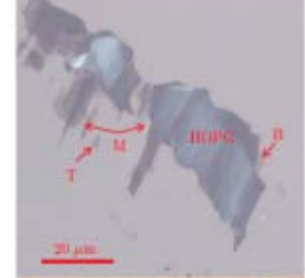
How to know the number of
layers?





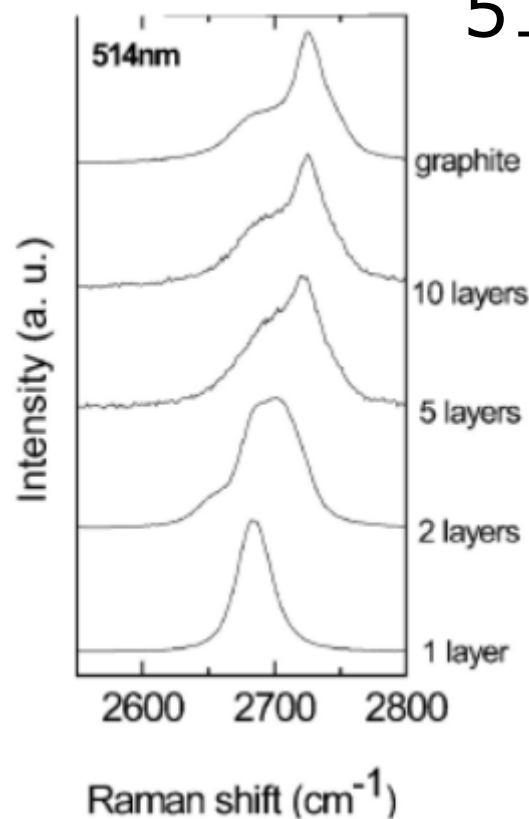
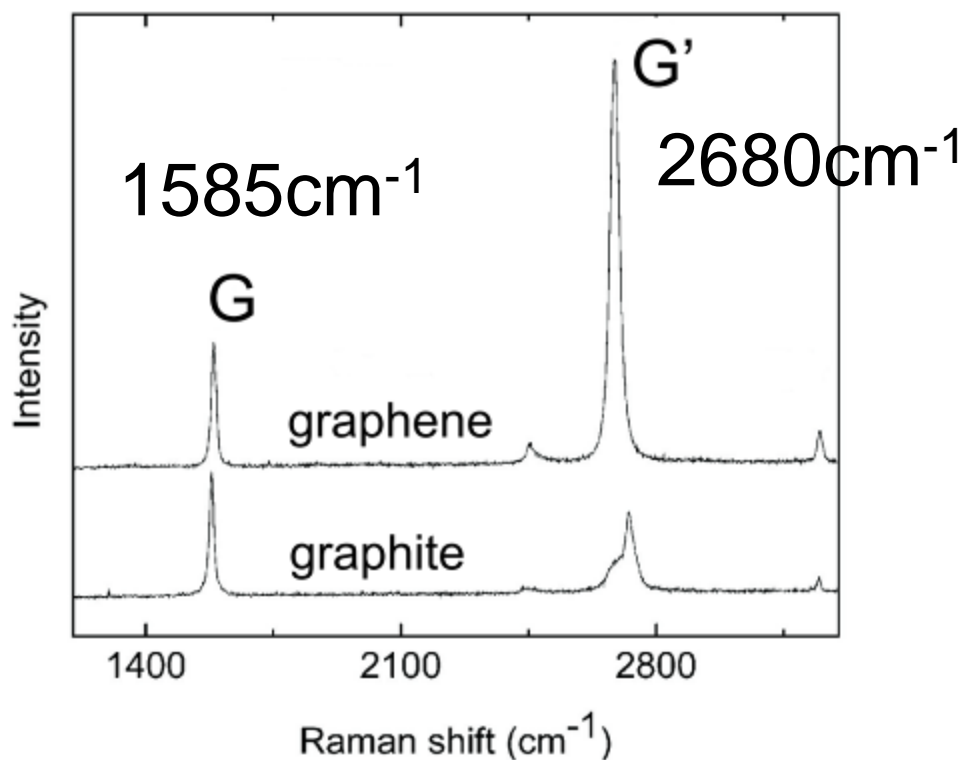
Raman spectra of graphene

A.C. Ferrari et al. PRL (2006)



- G'(2D) band is sharp and strong.
- number of graphene layer

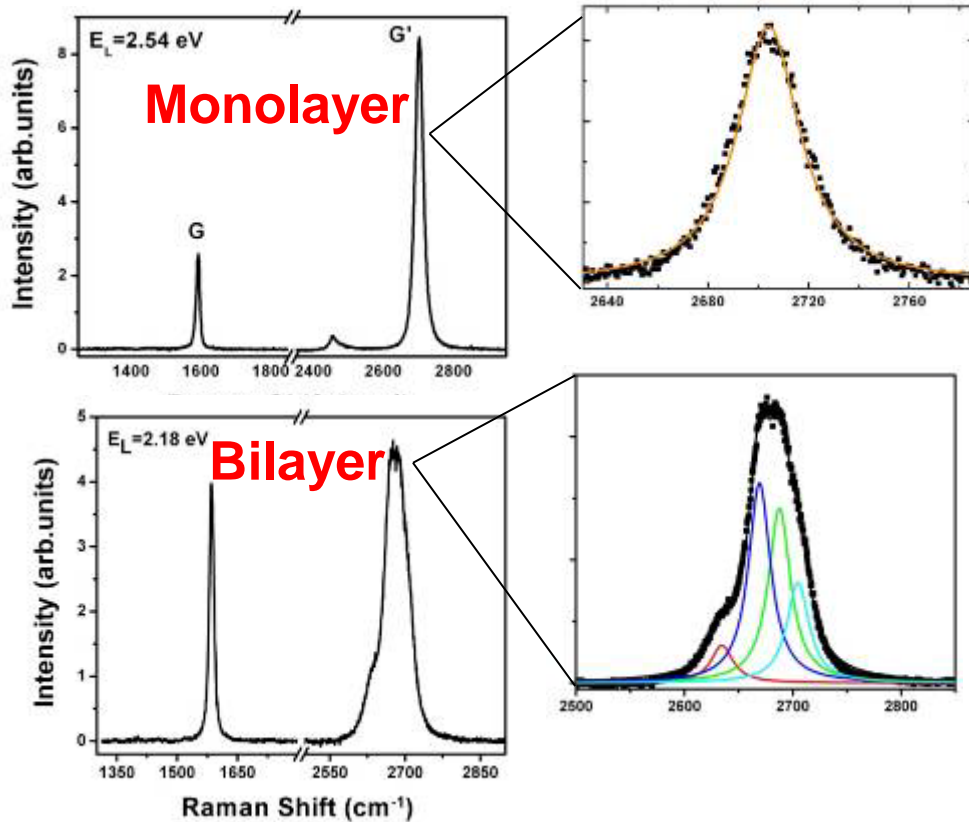
$E=2.41\text{eV}$
514nm



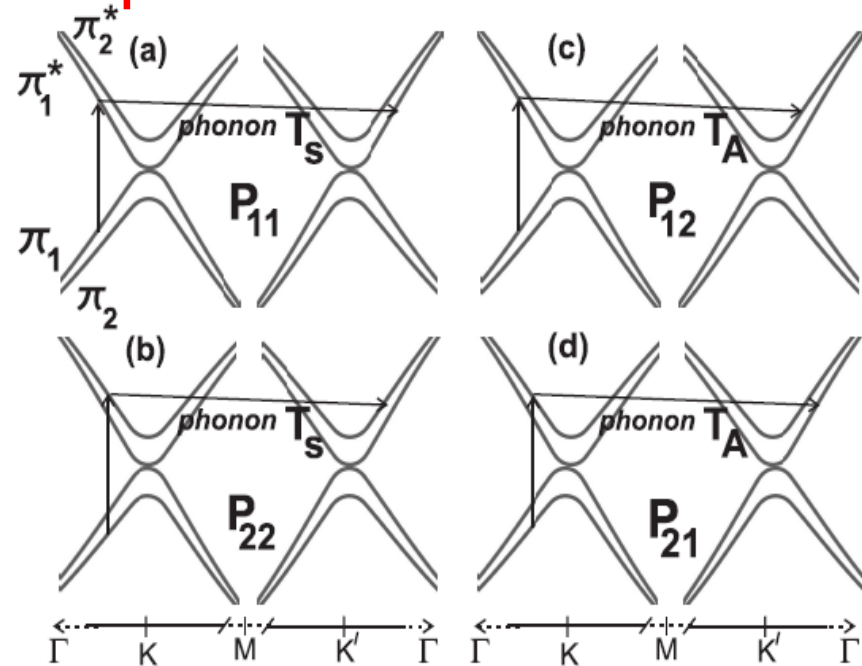


The G' (2D) Raman band of bilayer graphene

J. S. Park et al. *Carbon* 47, 1303 (2009).

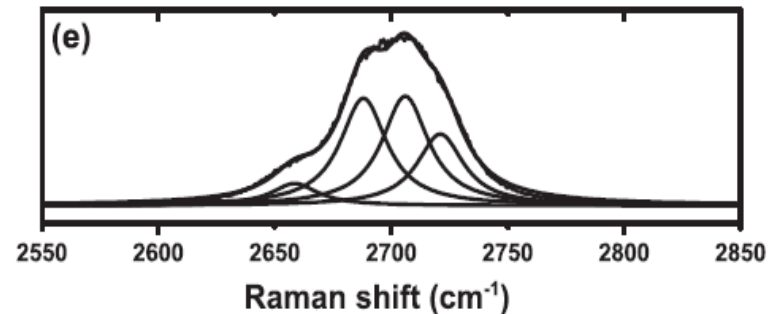


Double resonance processes in 2LG



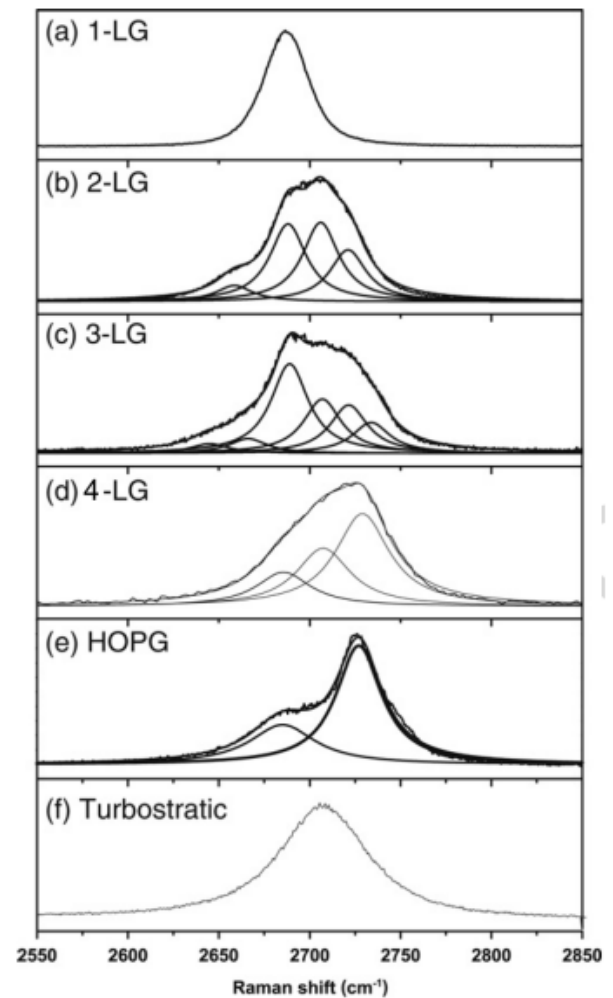
The G' (2D) band of bilayer graphene consists of four peaks

A.C. Ferrari et al. PRL (2006)



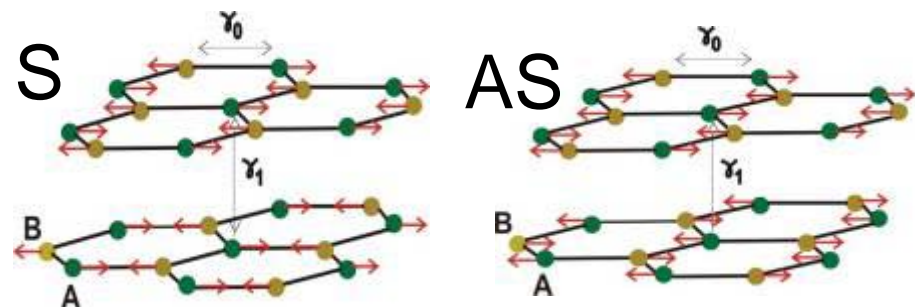
Number of graphene layer is available by

- (1) G' to G intensity ratio
- (2) Spectral shape of G'
- (3) Spectral width of G'
- (4) Raman intensity of G



Stacking order of graphene

More analysis for
interlayer interaction of
2-LG.



Malrad et al. Phys. Rev. Lett. 101,
257401, (2008)

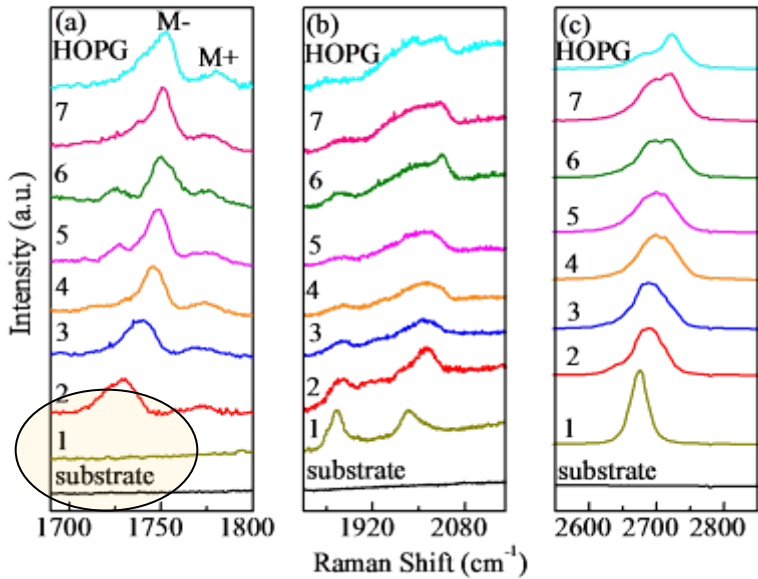


New method for number of layers

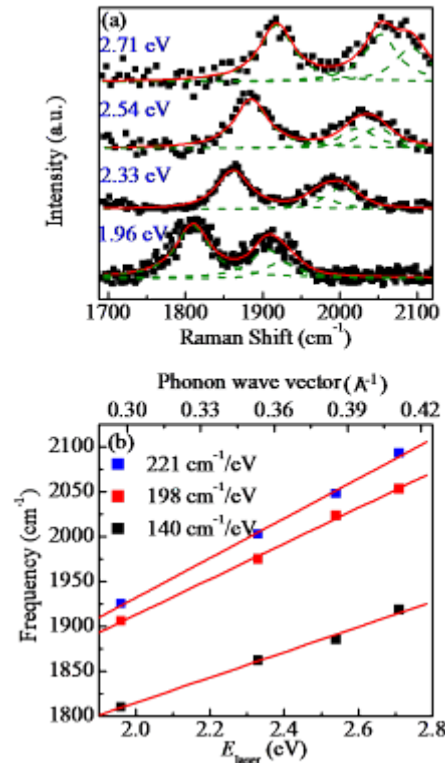
C. Cong et al. ACS Nano 5, 1600 (2011).

Y. Ting

M iTOLA G' (2D)



dispersive!



iTOLA

M

M : oTA+LO

absent for 1L-G

not affected by substrate

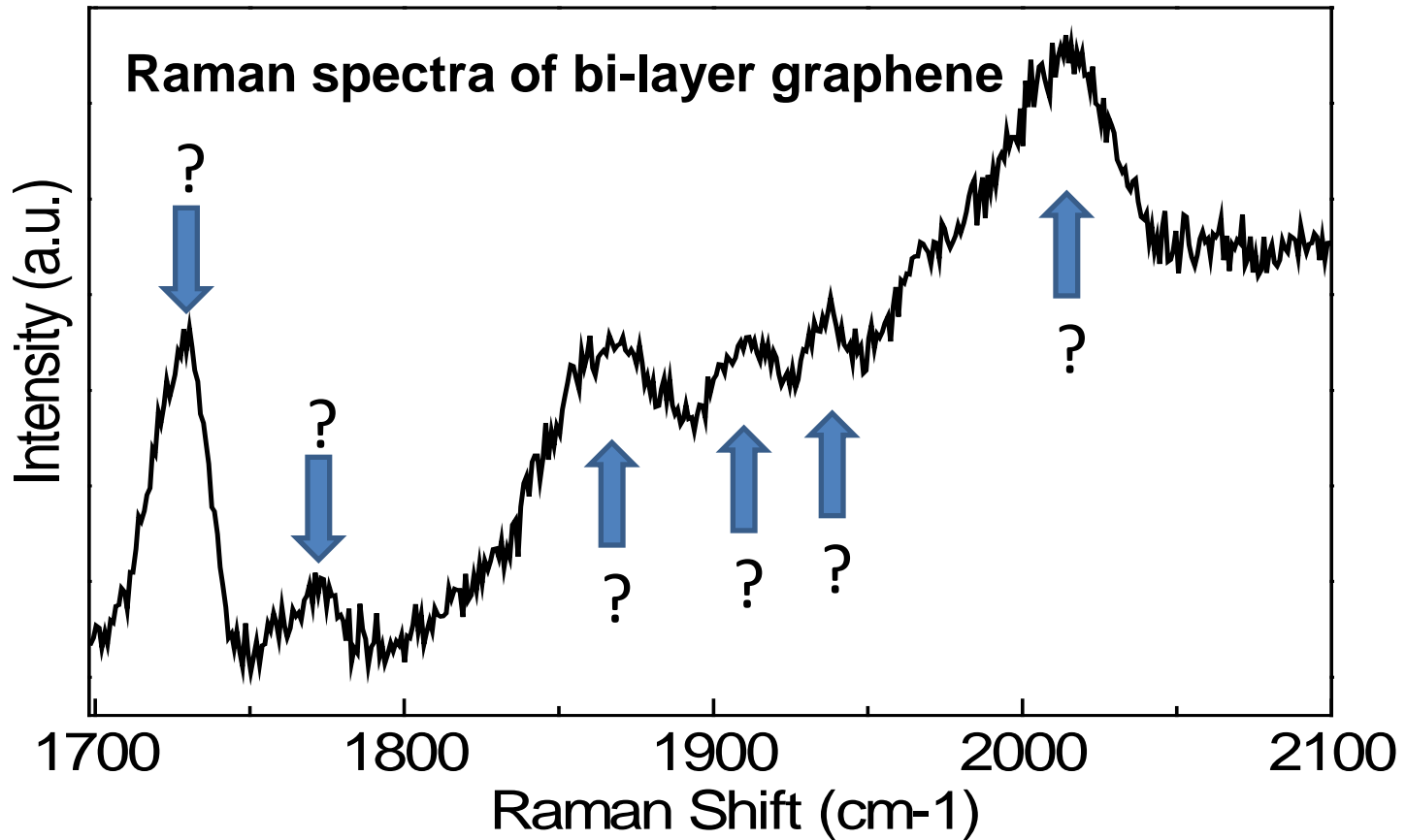
from 1700cm^{-1} to 2000cm^{-1}



Calculation of Raman peaks

from 1700cm^{-1} to 2000cm^{-1}

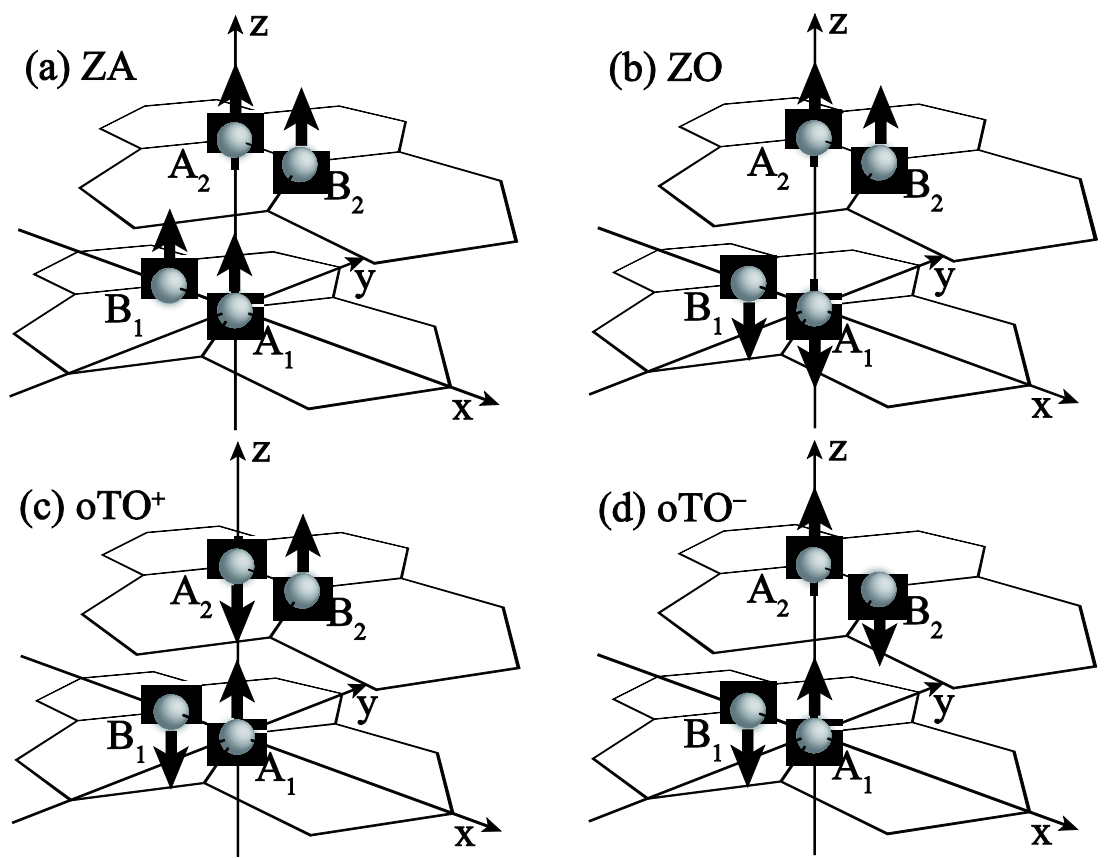
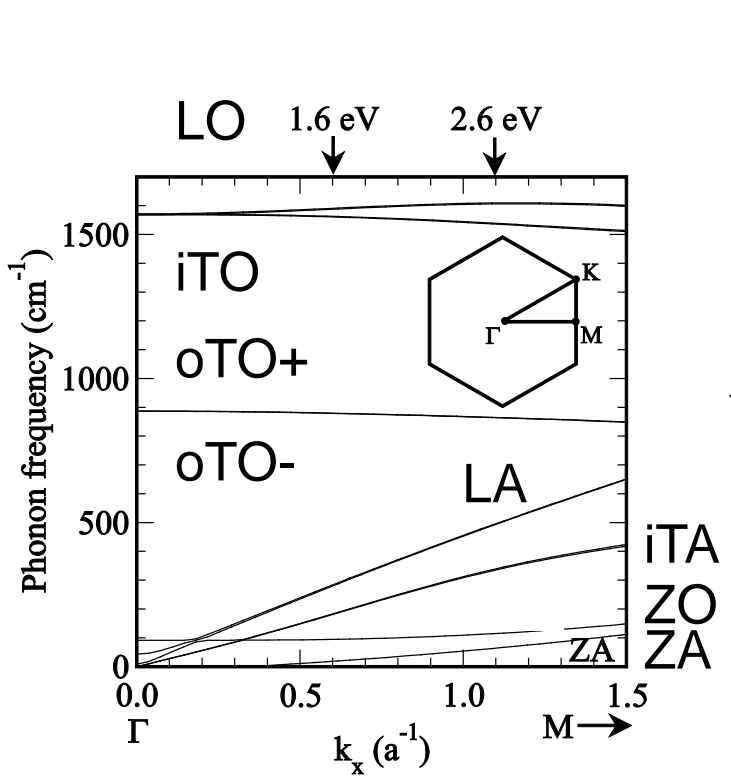
K. Sato et al. Phys. Rev. B, 84, 035419 (2011)





Four different out-of-plane phonons of bi-layer graphene

K. Sato et al. Phys. Rev. B, 84, 035419 (2011)



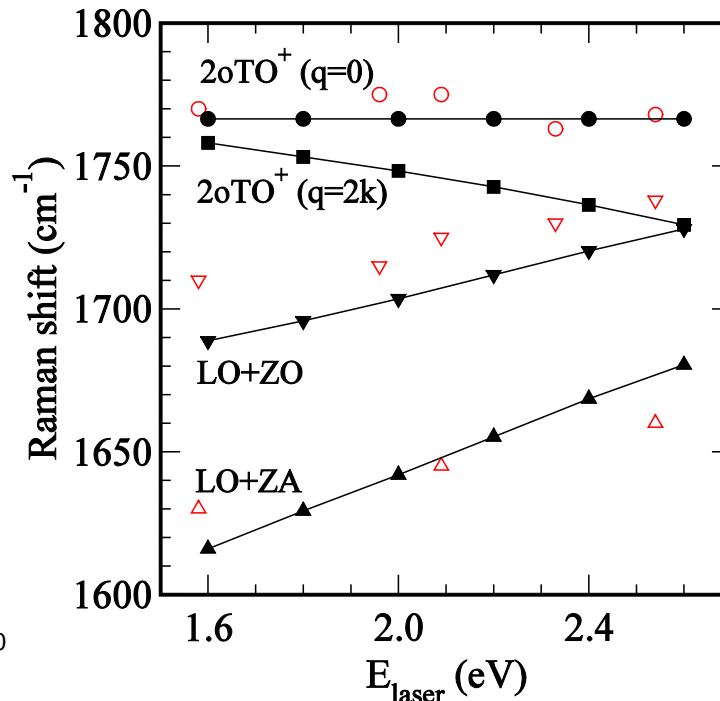
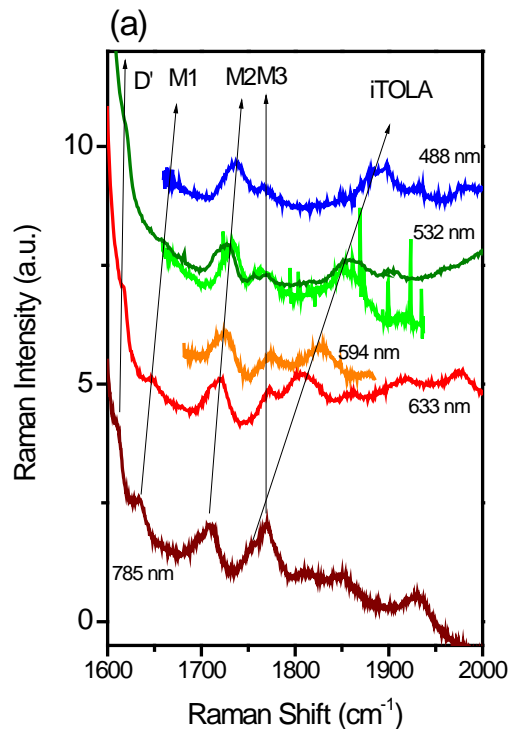
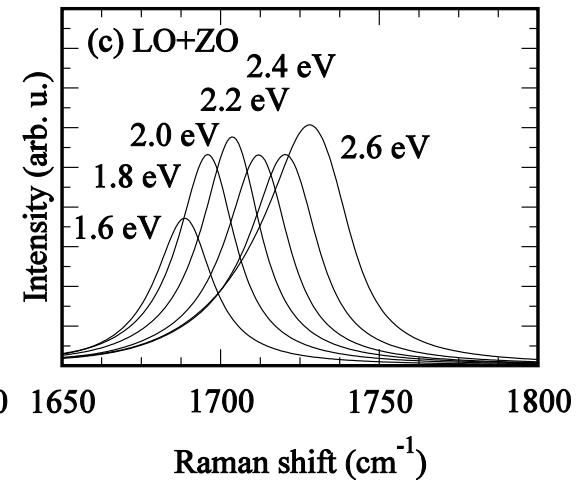
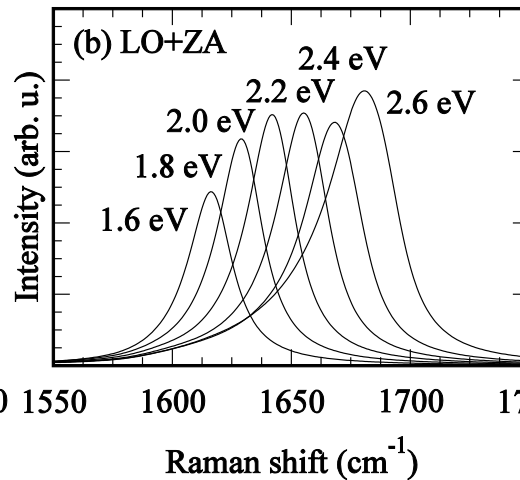
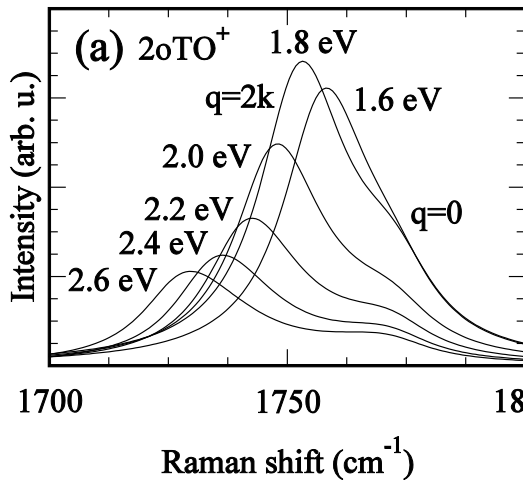
Force constant parameters

Out-of-plane : R. A. Jishi *et al.*, Phys. Rev. B 26, 4514 (1982).

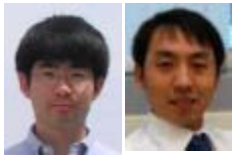
In-plane : M. Furukawa, Master thesis (2011).



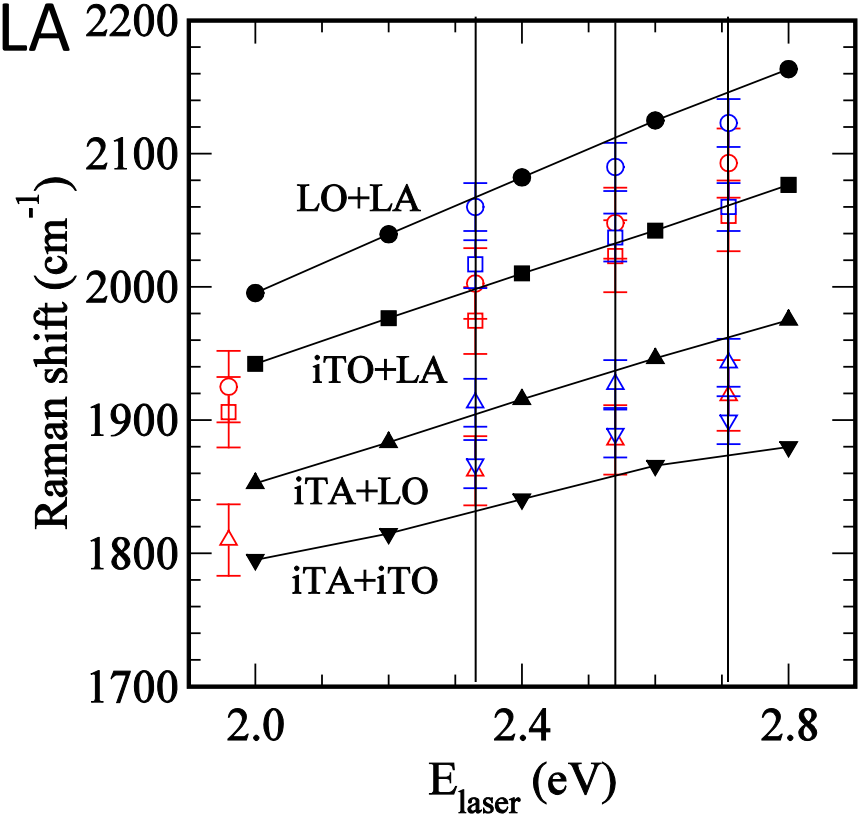
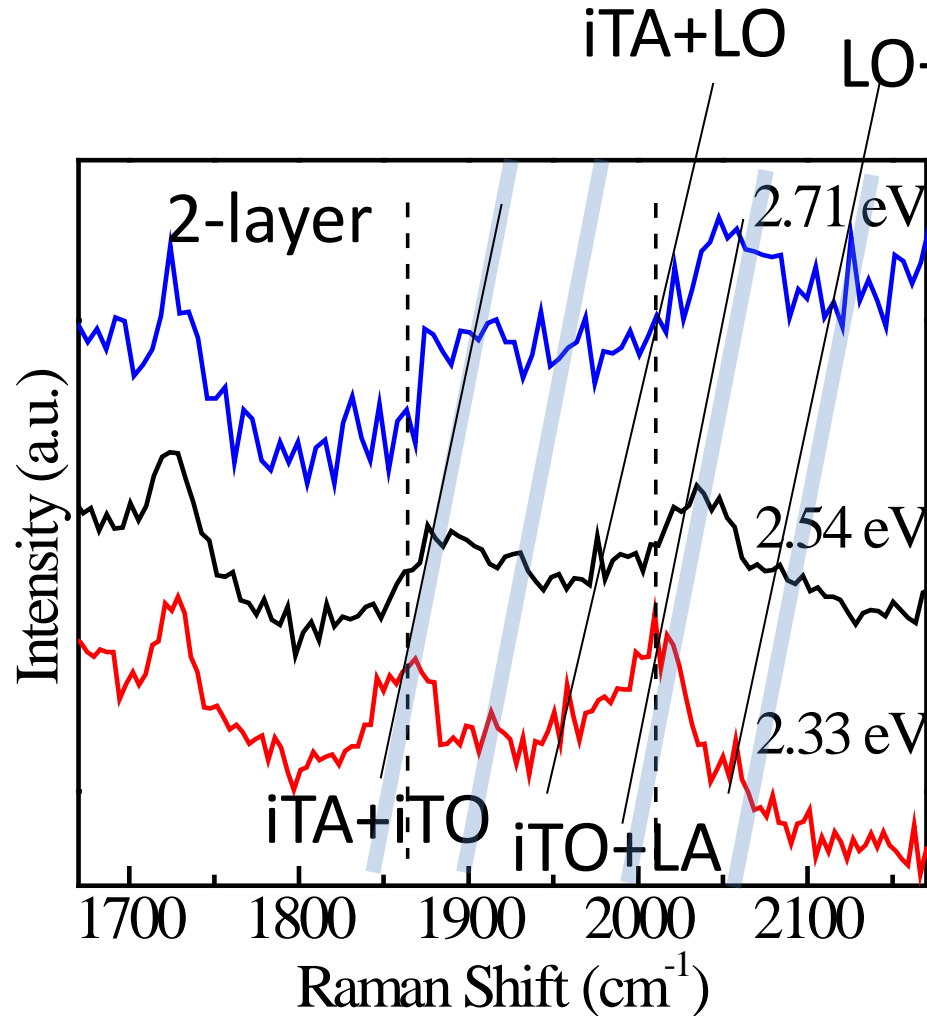
2oTO, LO+ZO, LO+ZA modes appear from 1700cm⁻¹ to 1800cm⁻¹



Black:
Calculation
Red: BLG
(experiment by
Lui @ T. Heinz)



LO+LA, iTO+LA, iTA+LO and iTA+iTO modes appear from 1850 to 2100 cm^{-1}



Black: Calculation

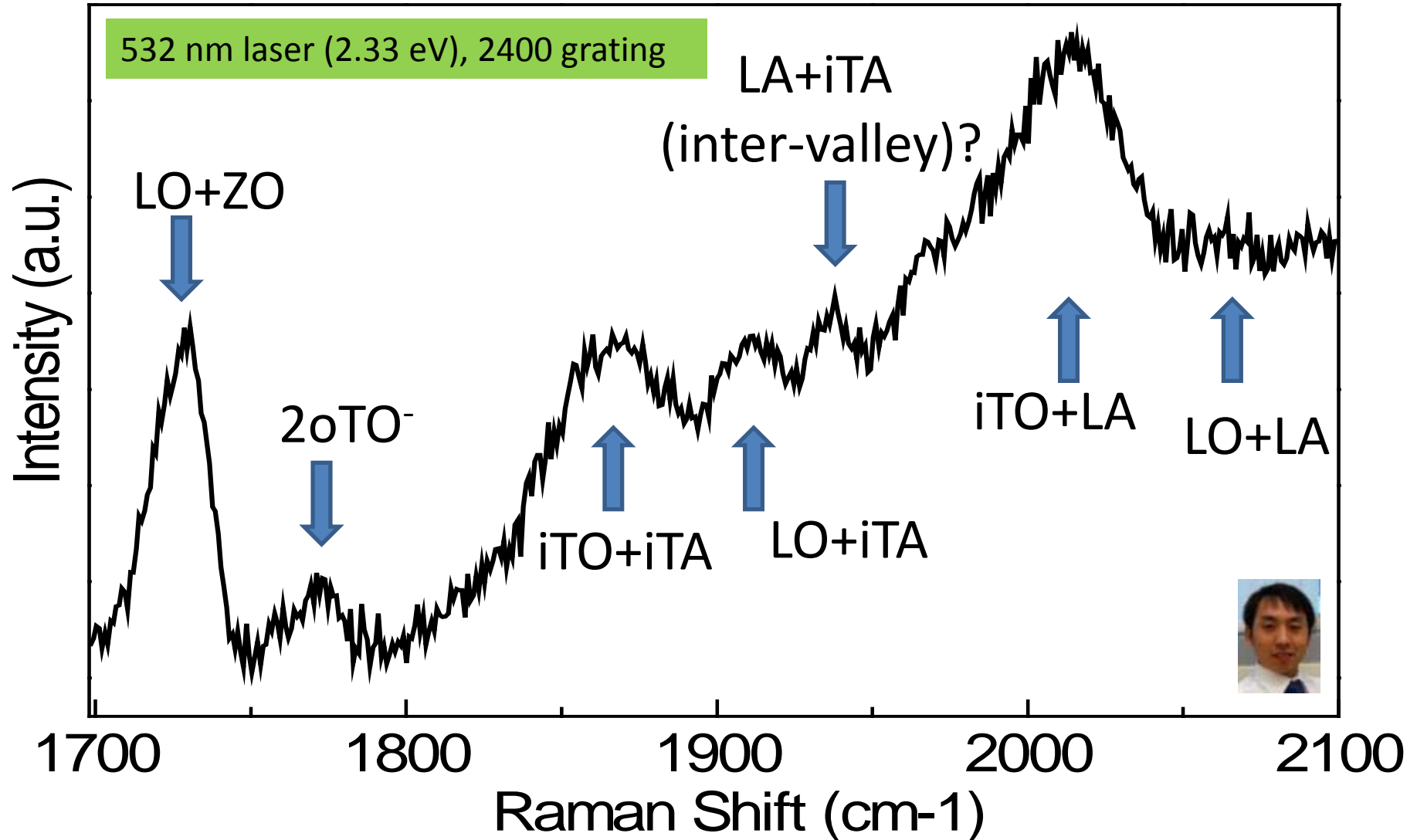
Red: SL graphene (exp.)

Blue: BL graphene (exp.)



Raman spectra of bi-layer graphene

K. Sato et al. Phys. Rev. B, 84, 035419 (2011).



Raman Spectroscopy of electro-chemical doping of single layer graphene

How to assign the combination modes of

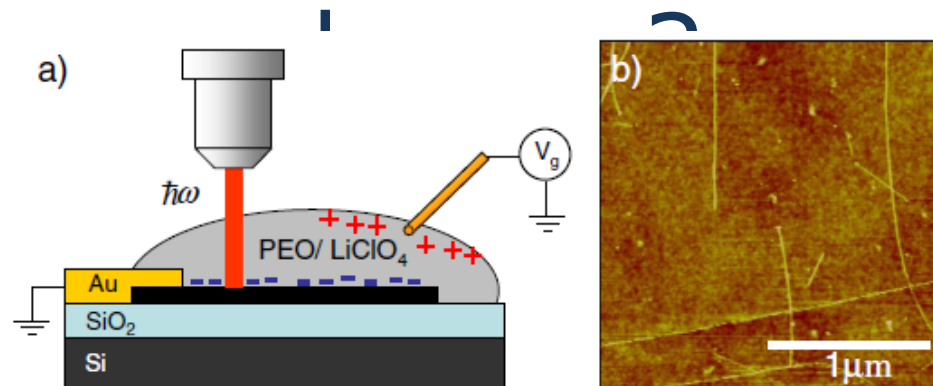
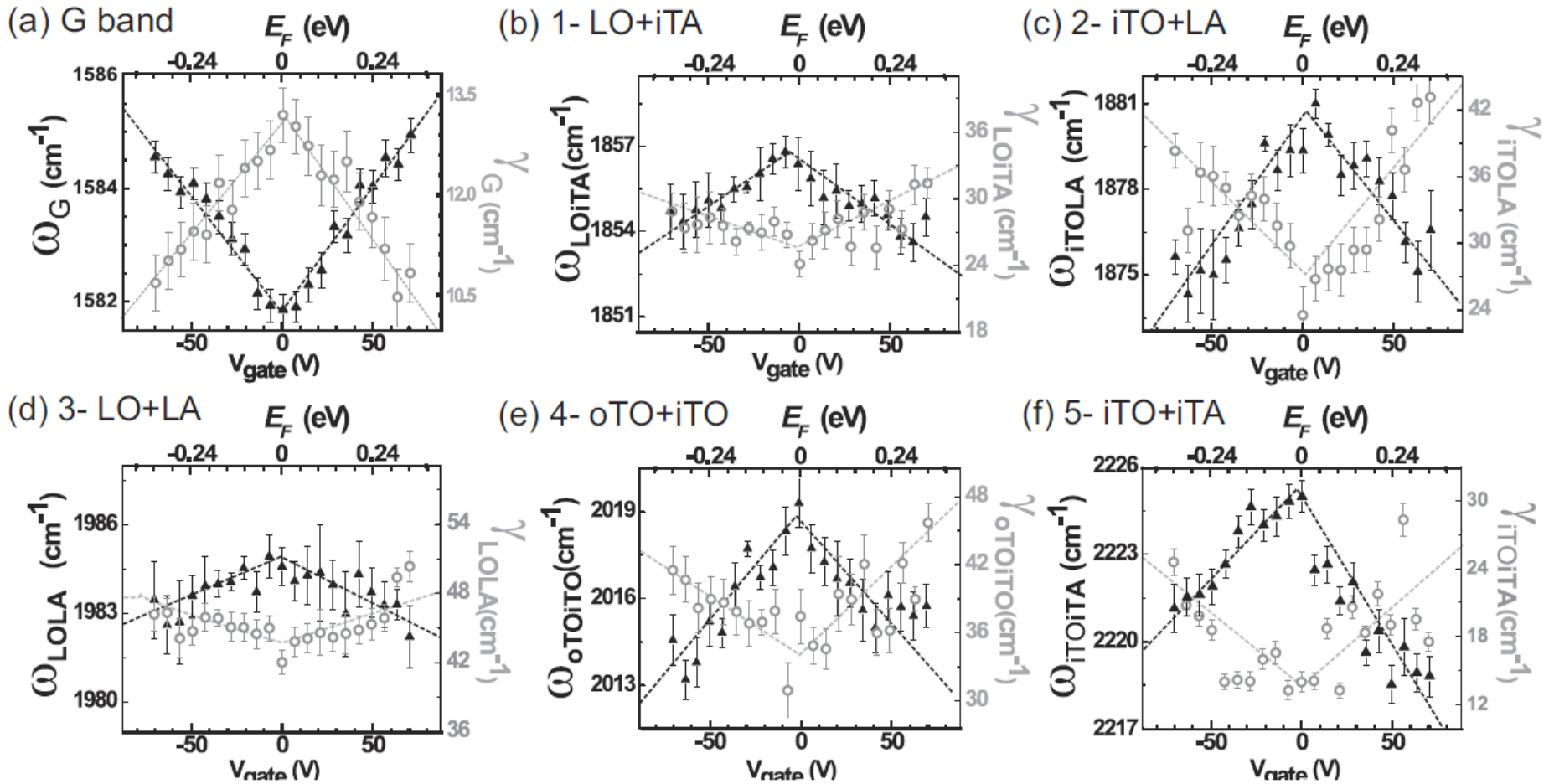
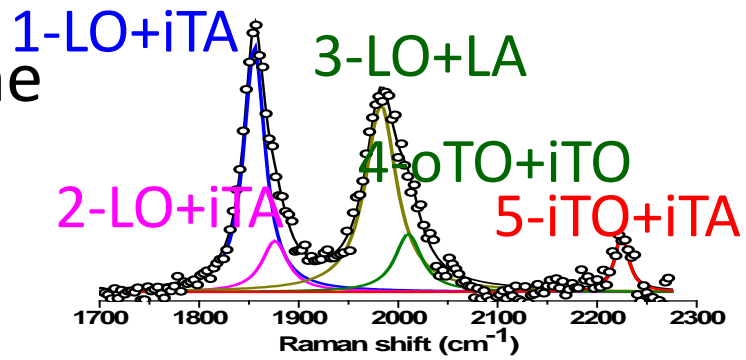


FIG. 1 (color online). (a) Schematic diagram of the experimental setup. The excitation laser shines through the PEO/LiClO₄ polymer electrolyte. (b) An AFM image indicating that the nanotubes are spaced out and are typically isolated from one another.



Gate voltage dependence of the M-bands of 1LG

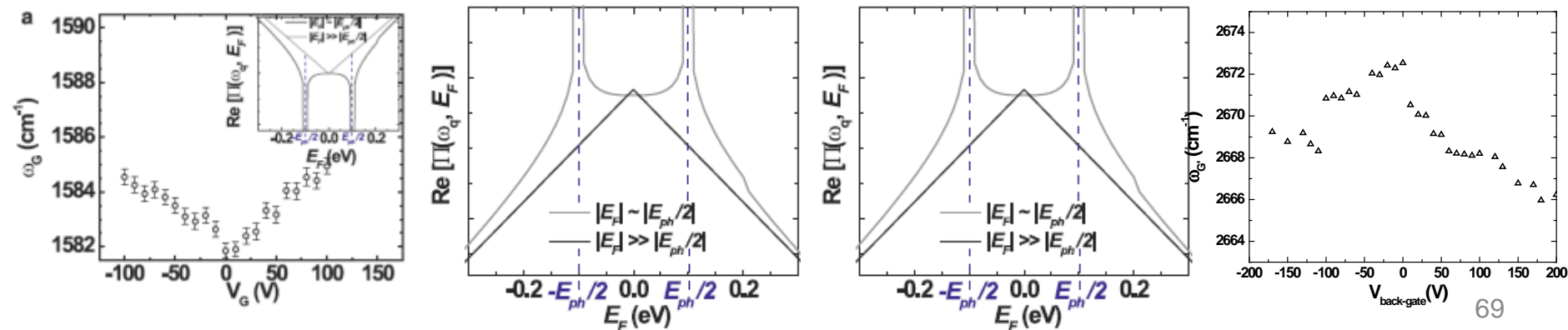
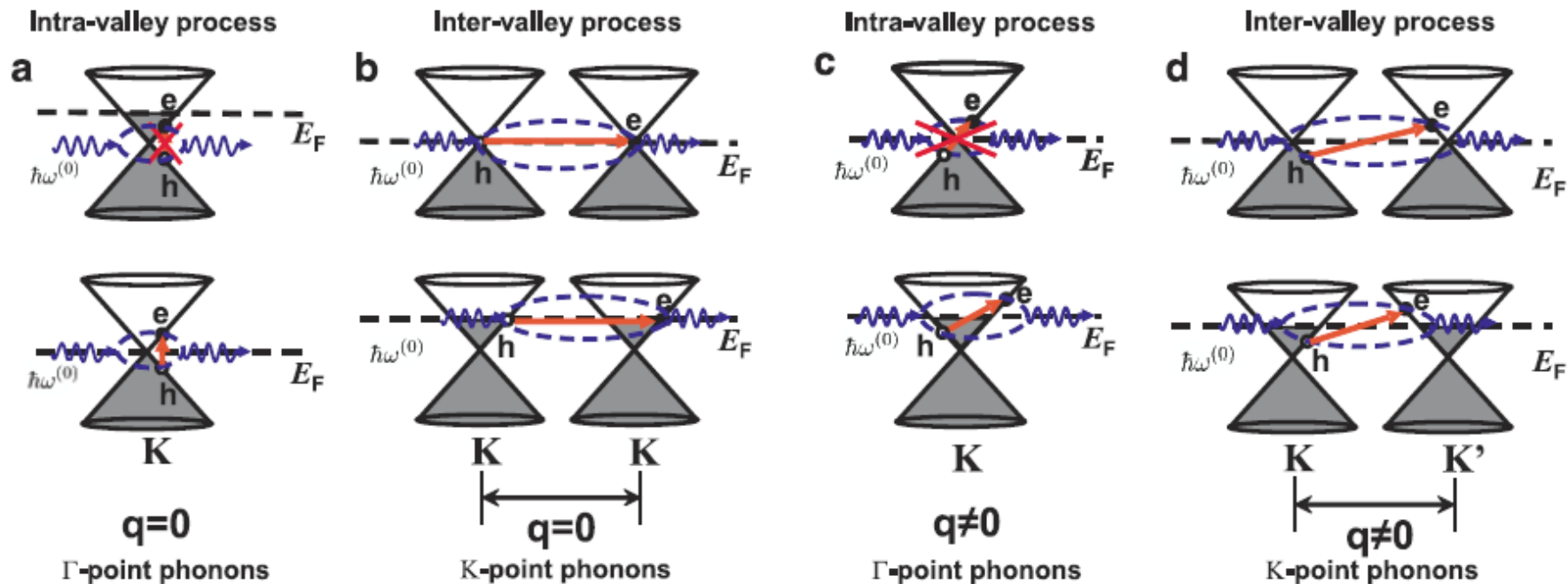
D. L. Mafra et al., submitted



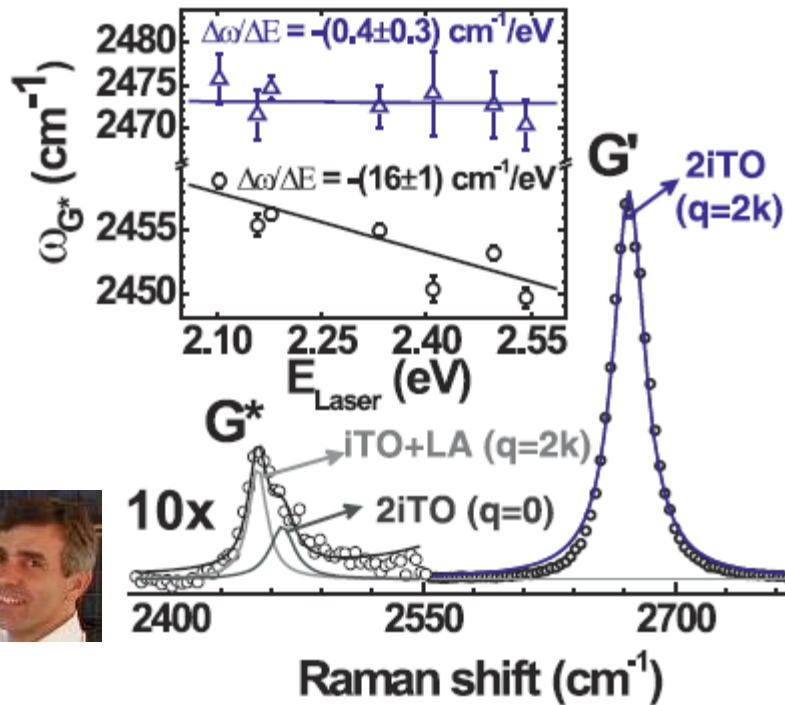


$q=0$ and $q \neq 0$ phonon gives different E_F dependence

P. T. Aroujo et al, Phys. Rev. Lett. In press



2450cm⁻¹ G* band problem



R. Saito *et al.*, *New J. Phys.*
5, 157 (2003).
both q=0 and q=2k exist in DR



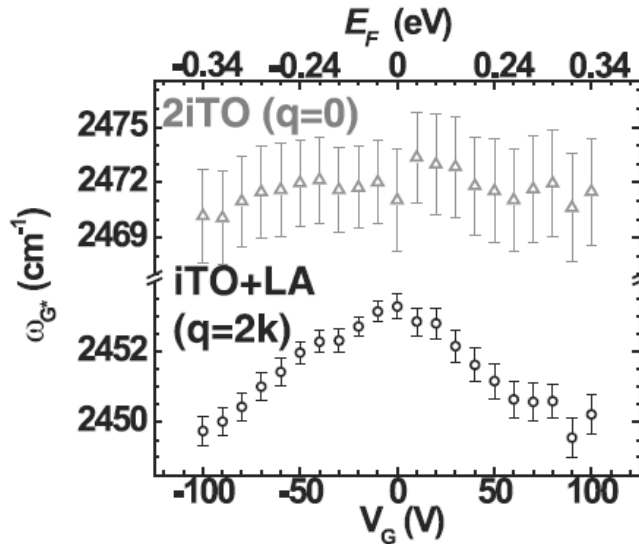
T. Shimada *et al.*, *Carbon*
43, 1049 (2005).
q=0 DR 2iTO



D. L. Mafra *et al.*, *Phys. Rev. B*
76, 233407 (2007).
q=2k DR iTO+LA



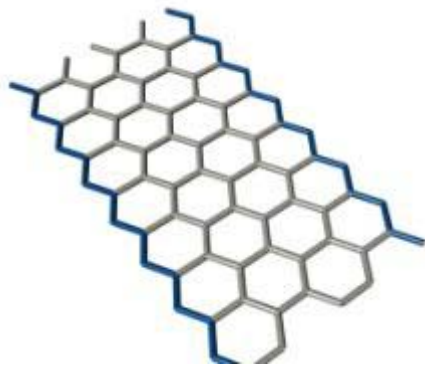
P. T. Araujo *et al.*, *Phys. Rev. Lett.*
In press
both q=0 DR 2iTO and q=2k DR iTO+LA



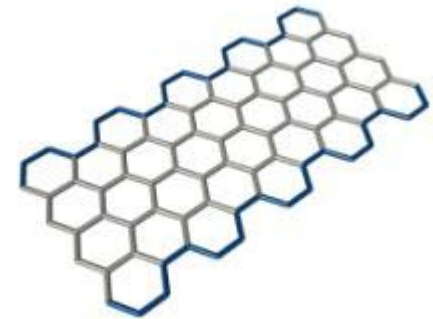
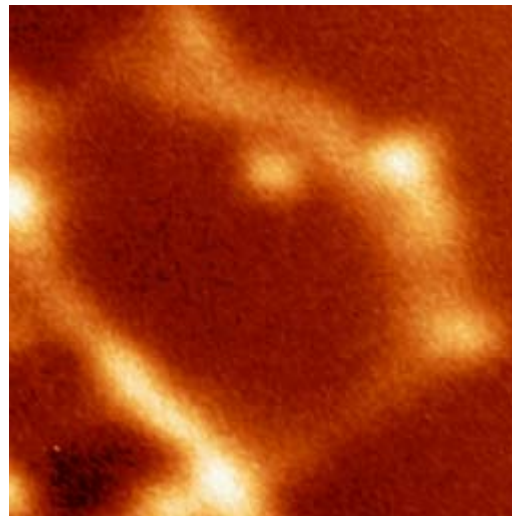
V_G measurement !

Raman imaging of graphene edge

How to know the edge structure?



zigzag edge

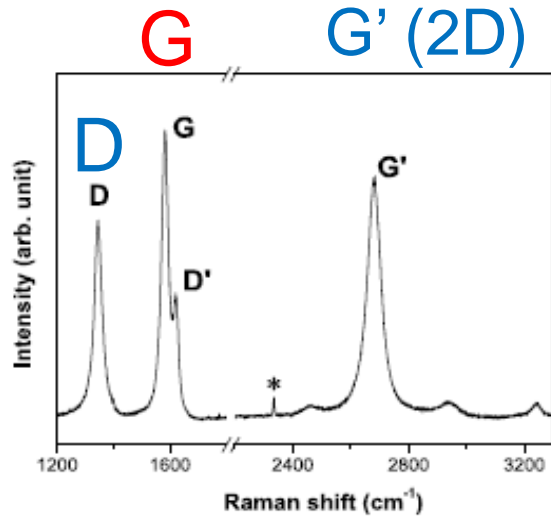


armchair edge

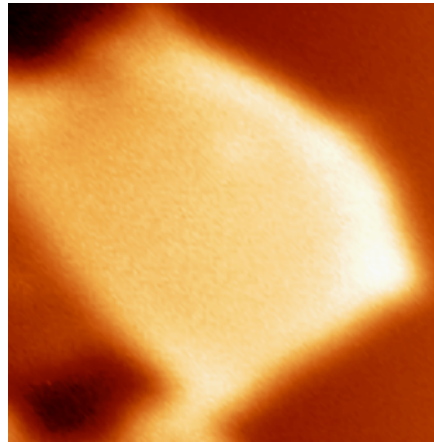


Raman imaging of graphene

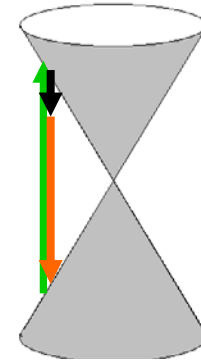
M. A. Pimenta et al., Phys. Chem. Chem. Phys. 9, 1276 (2007)



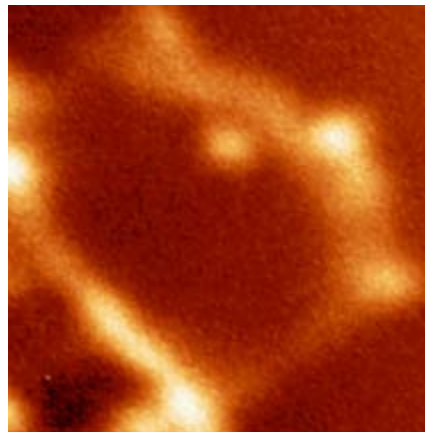
G-band image



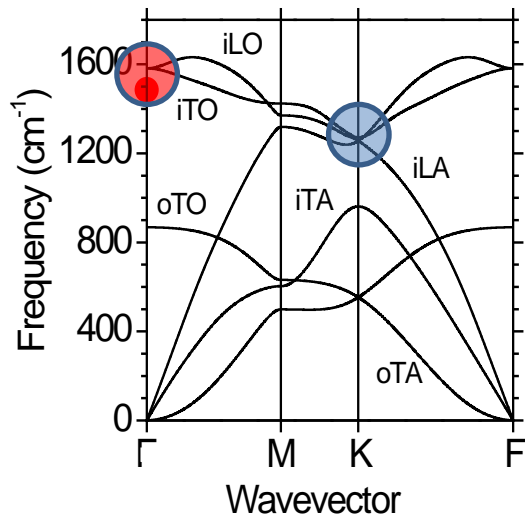
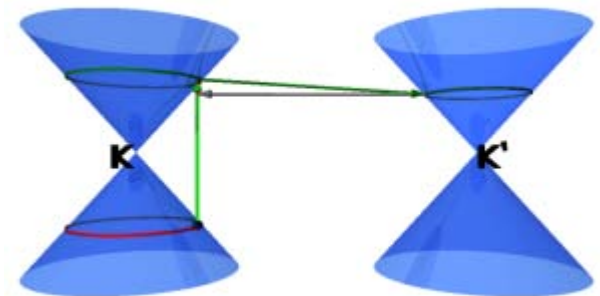
G band



D-band image

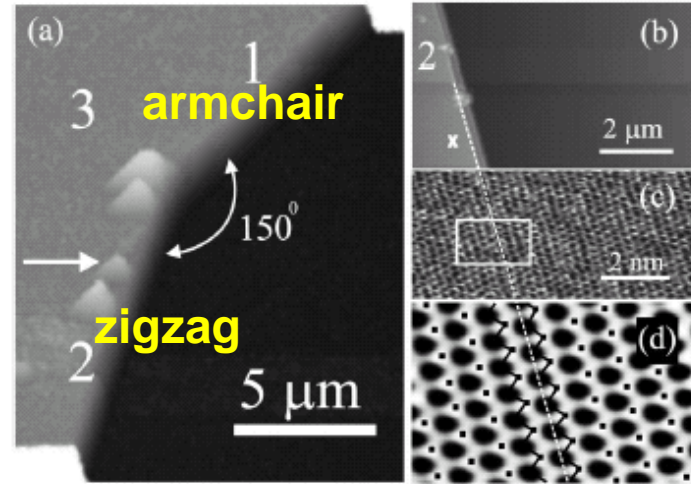
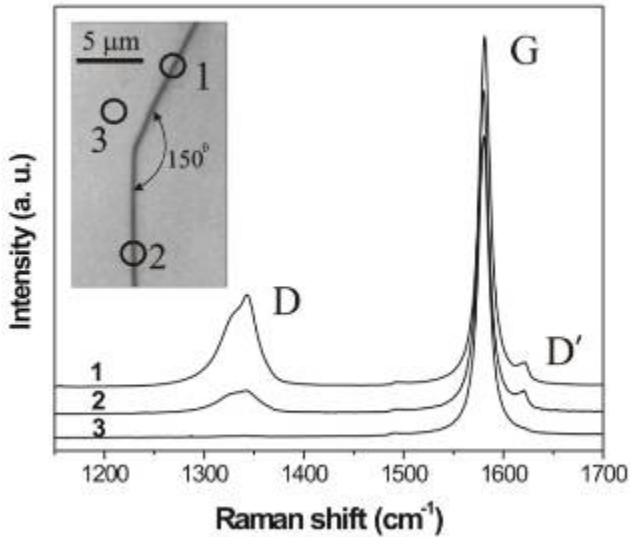


D band

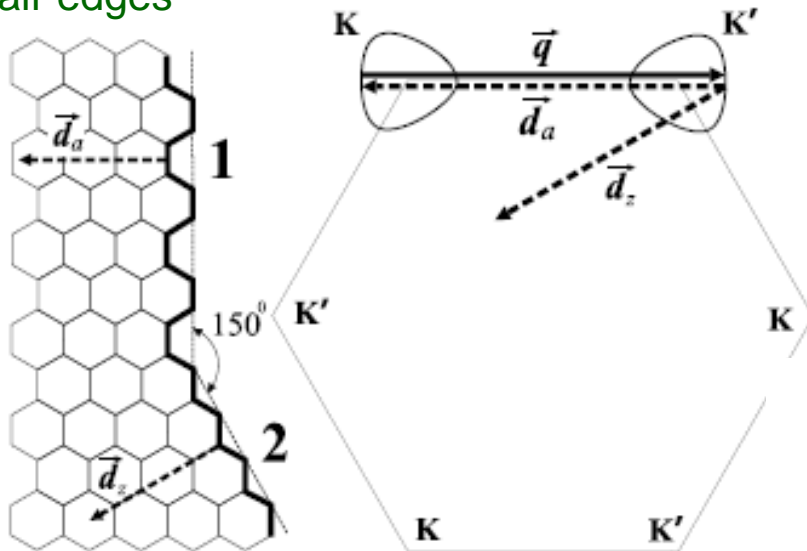


Raman scattering in graphites edges

L. G. Cançado et al. Phys. Rev. Lett., 93, 247401 (2004)



armchair edges

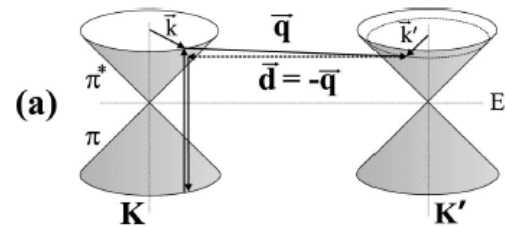


zigzag edges

armchair edges

inter-valley scattering

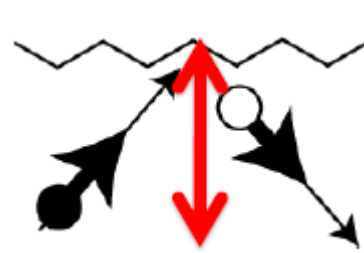
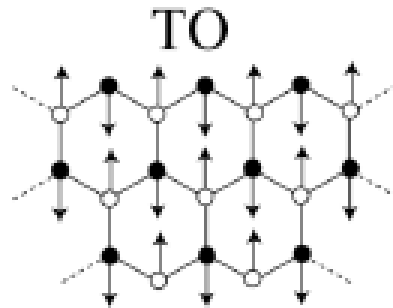
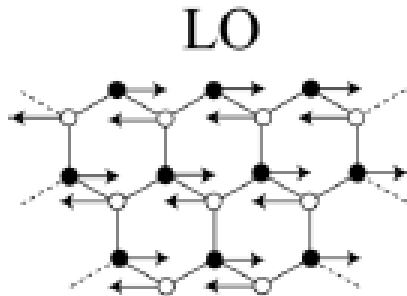
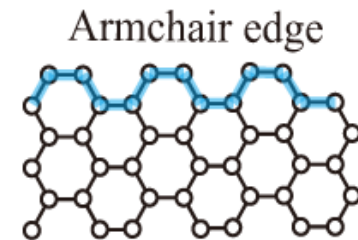
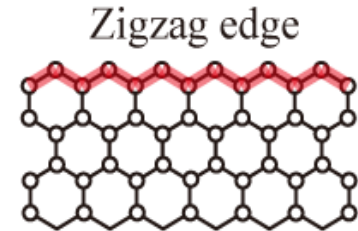
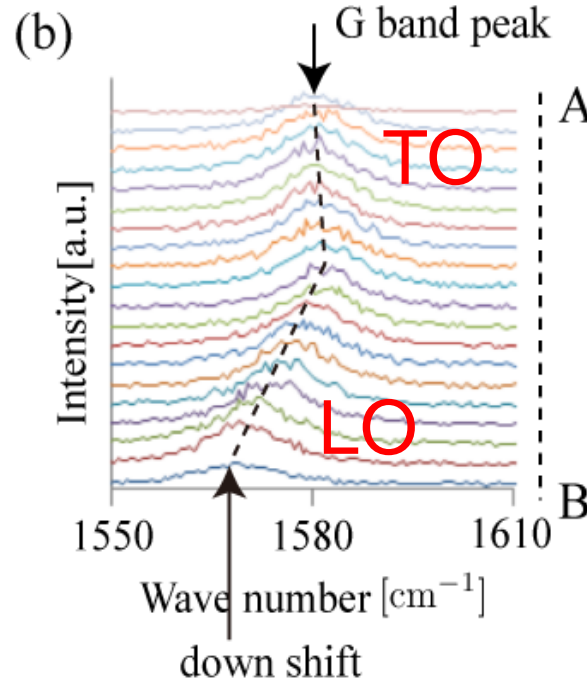
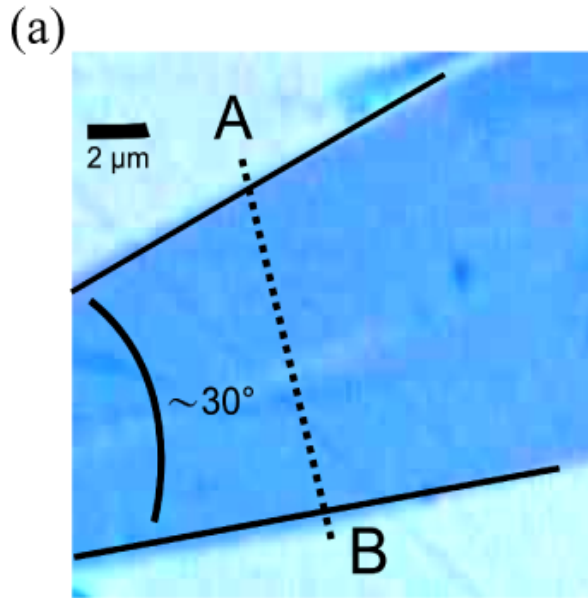
strong D signal





Edge dependent Kohn anomaly of G-band

K. Sasaki et al. Phys. Rev. B 80, 155450 (2009)



zigzag TO

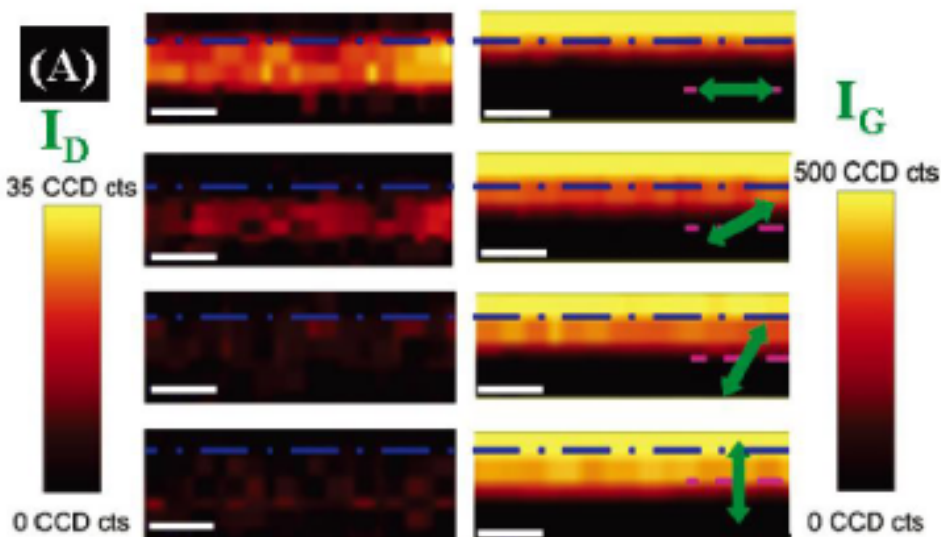


armchair LO

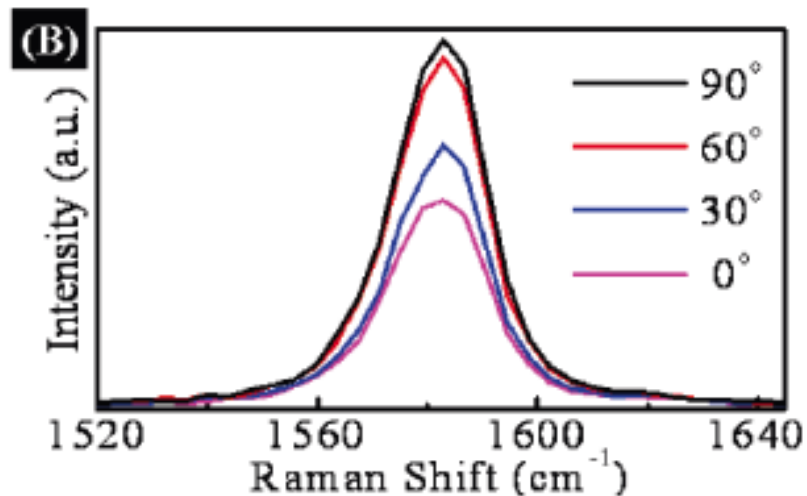
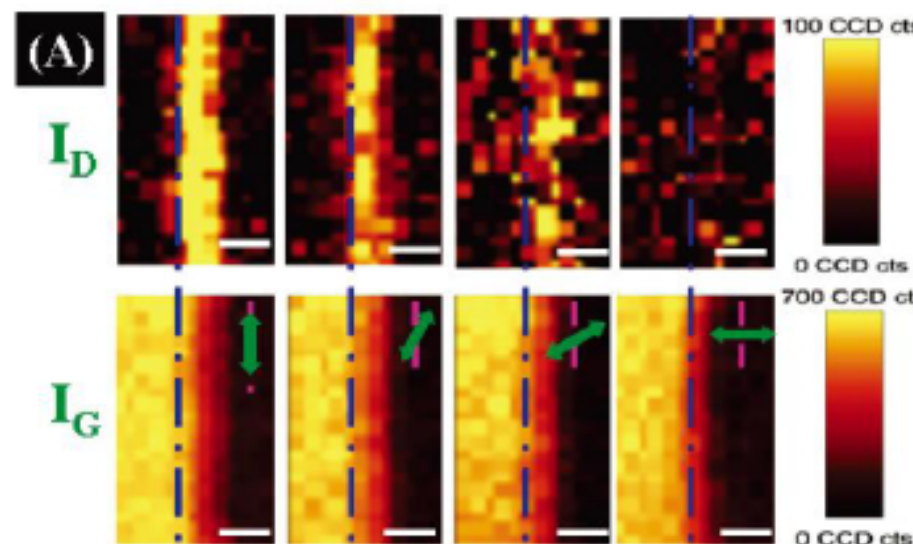
Polarization dependence of G

Two different polarization-dependences

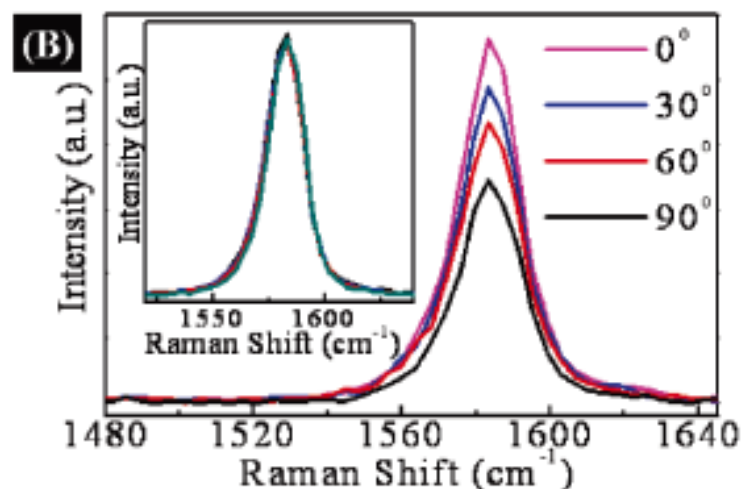
C. Cong, T. Yu and H. Wang
ACS Nano, 2010, 4, pp 3175



Scale bar 400 nm



60% Zigzag, 40% Armchair



60% Armchair, 40% Zigzag

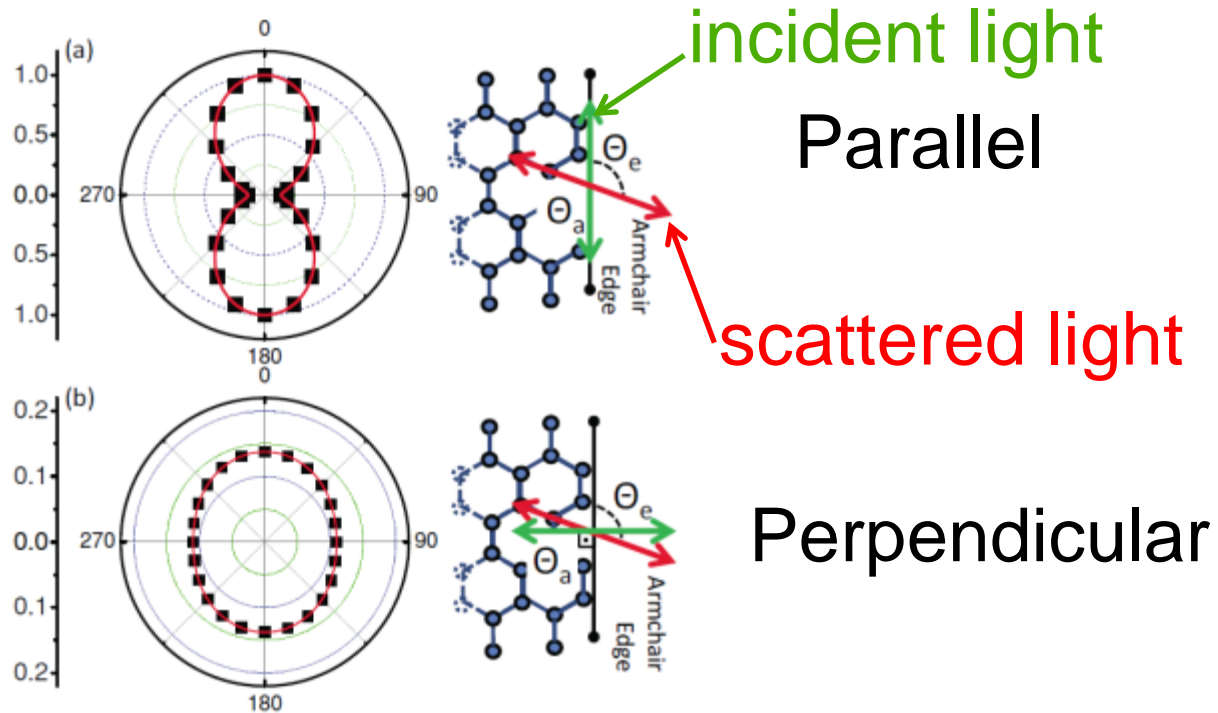


Polarization dependence of D at edges

K. Sasaki et al. Phys. Rev. B 82 205407 (2010)

E. Barros et al. Phys. Rev. B 83, 245435, (2011).

Armchair
edge



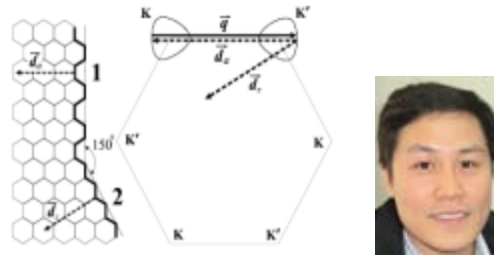
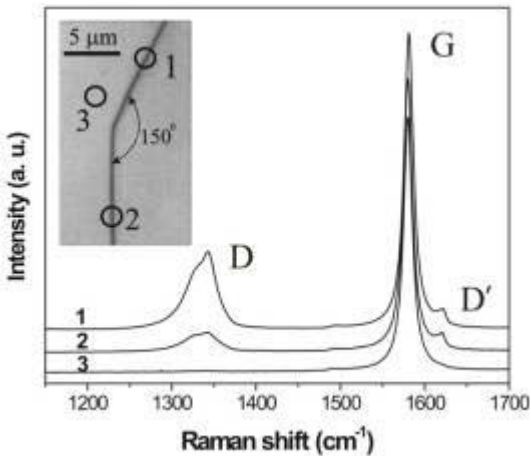
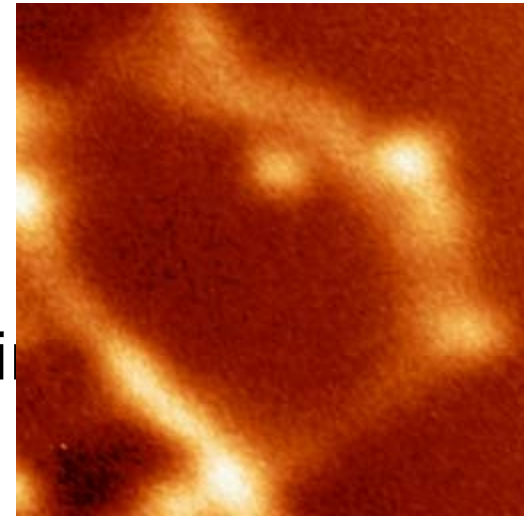
electron-phonon \Leftrightarrow pseudo spin of graphene

experiment: Honjie Dai group (unpublished)

Edge of graphene layer

- (1) Strong D-band (A)
- (2) kohn anomaly TO (Z) and LO (A, softening)
- (3) Polarization dependence (G, D, G')
- (4) 1450cm^{-1} (Z) and 1530cm^{-1} (A)

D-band image

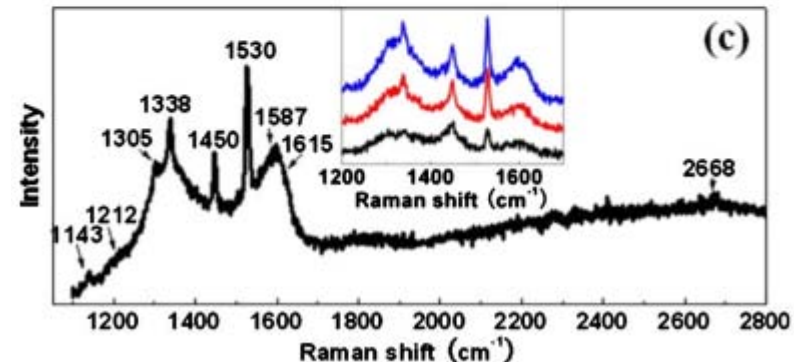
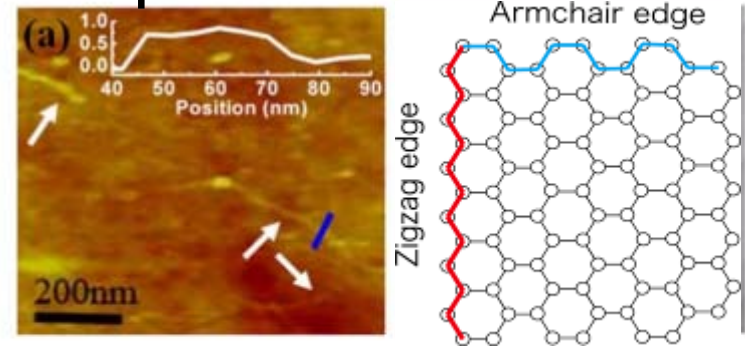


1450cm^{-1} (Z)
 1530cm^{-1} (A)

L. G. Cançado, et al.
Phys. Rev. Letters,
93, 247401 (2004)

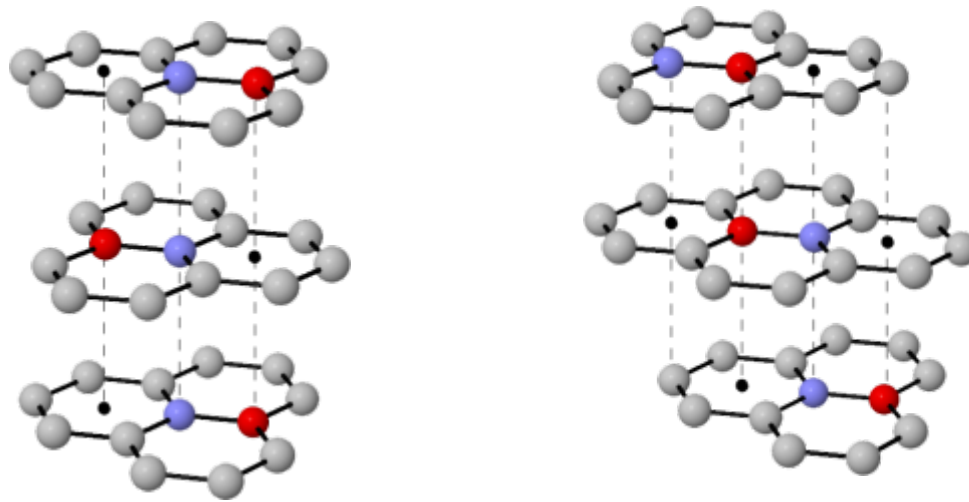
W. Ren et al.,
Phys. Rev. B 81,
035412 (2010)

Graphene nano ribbon



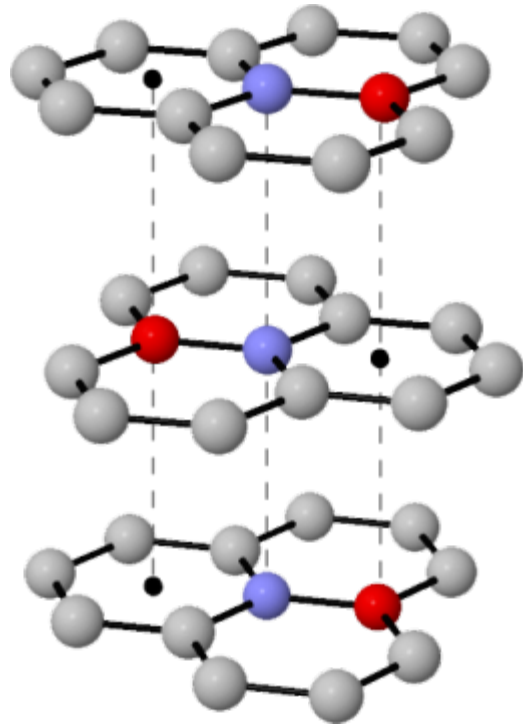
Raman of 3L graphene

How to distinguish the stacking order?



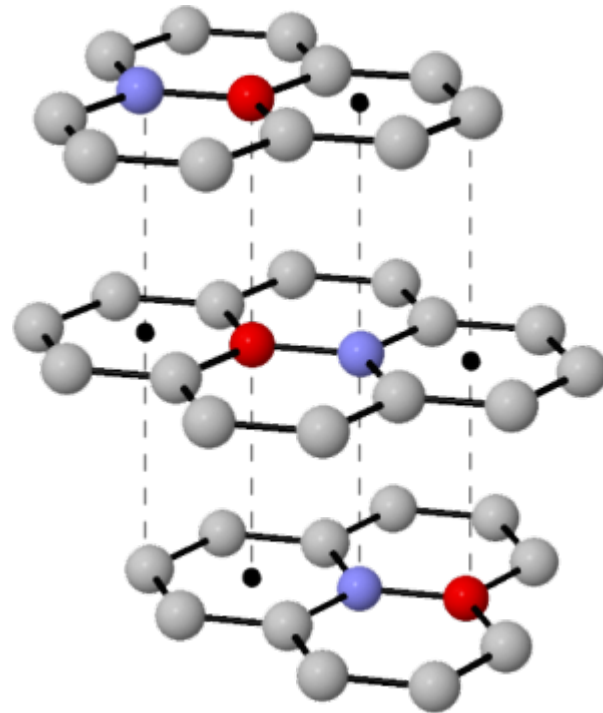
Stacking order of tri-layer graphene

ABA stacking



Bernal structure

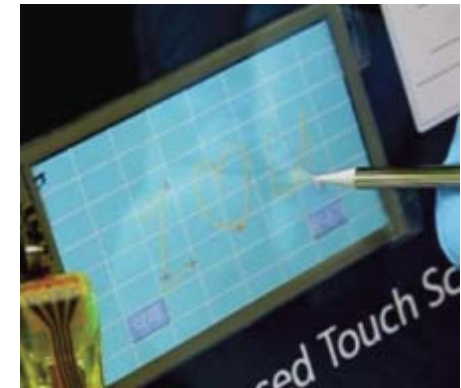
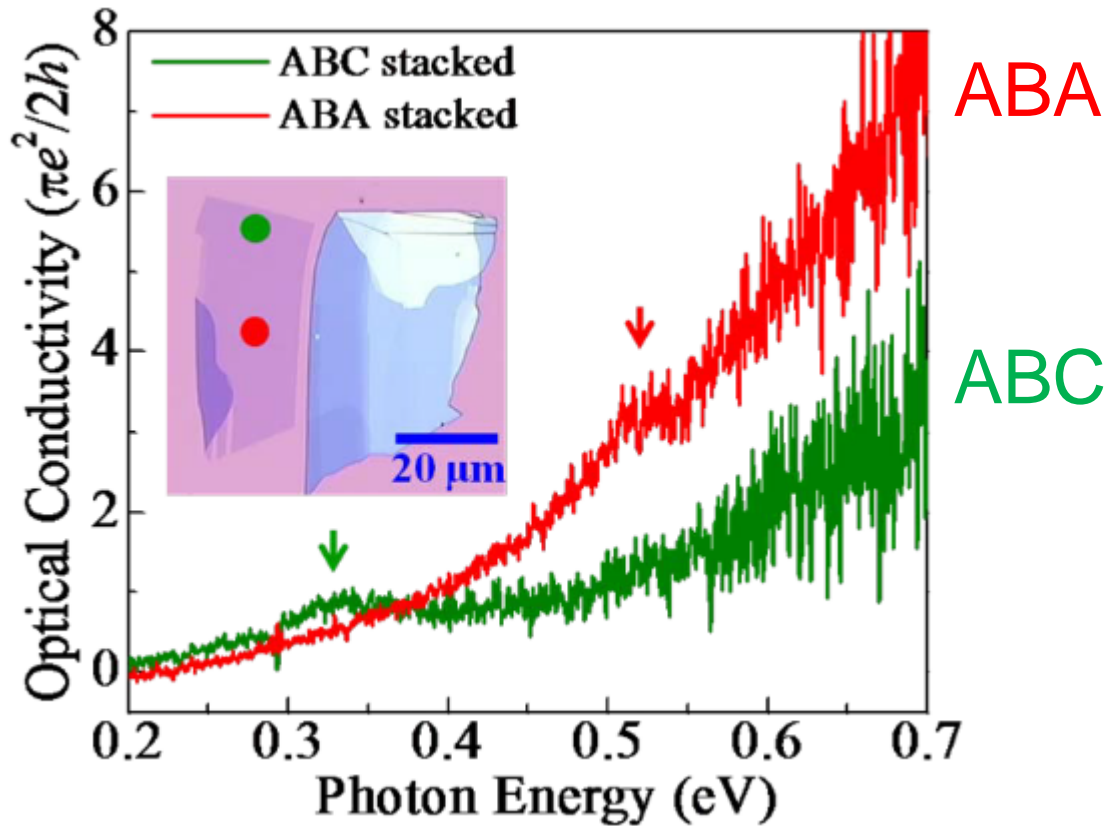
ABC stacking



Rhombohedral structure



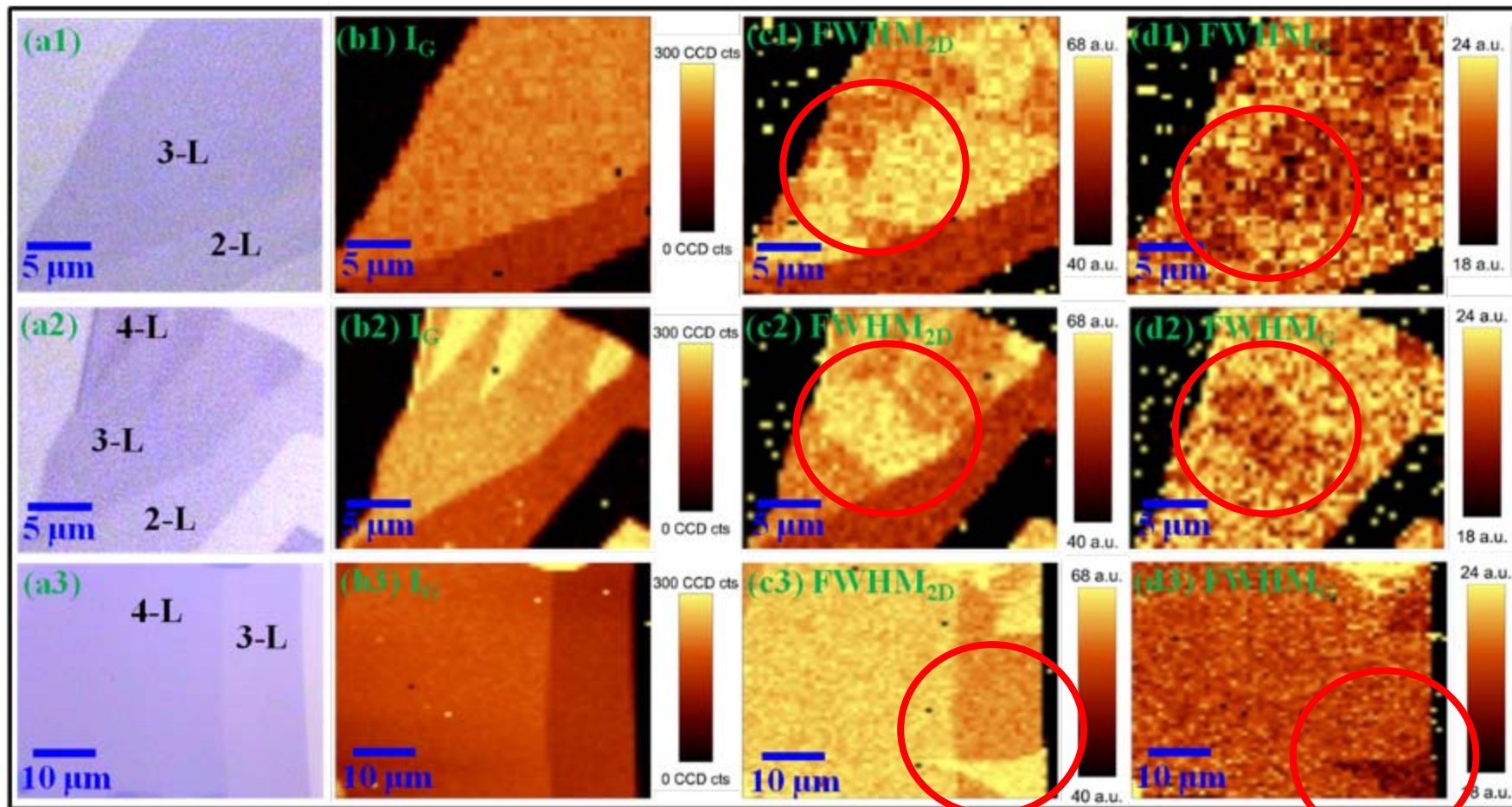
Optical conductivity is large for ABA stacking!
C. Cong et al., ACS Nano 5, 8760 (2011).





Optical and Raman images of 3L graphene

C. Cong et al., *in press*, ACS Nano (2011)



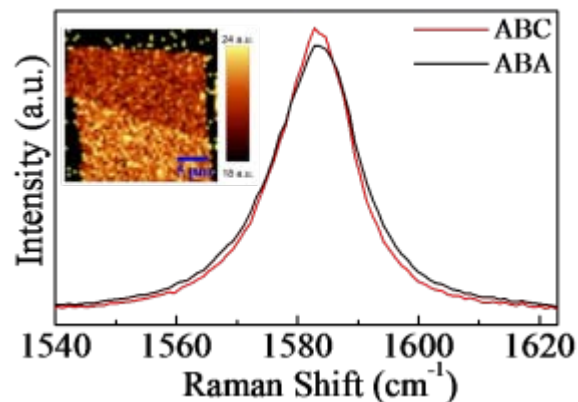
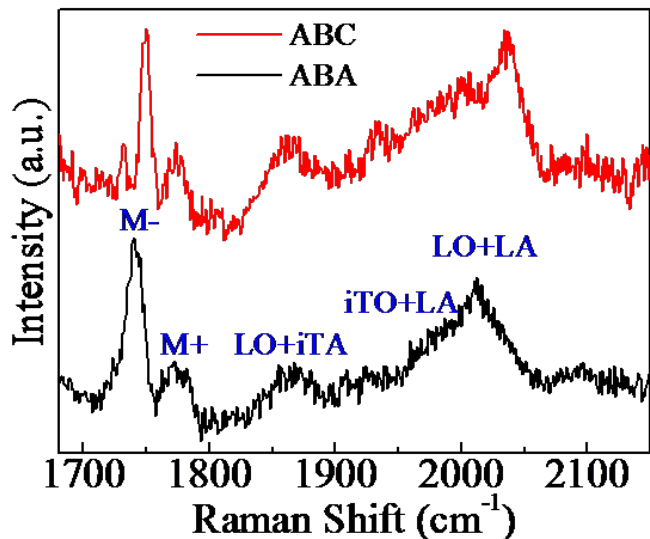
optical Intensity (G) FWHM (G') FWHM (G)

Distinguishable, however, sensitive to environment!!

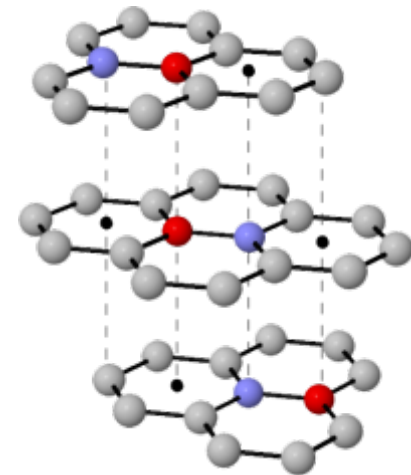


Spectral difference between ABA and ABC

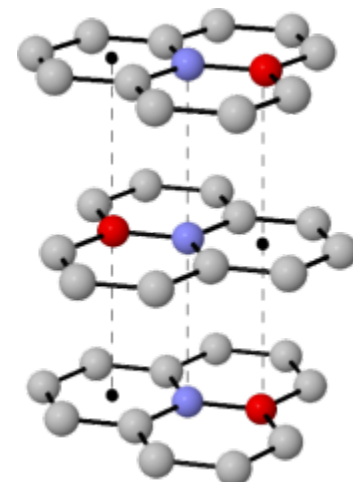
C. Cong et al., ACS Nano 5, 8760 (2011)



ABC

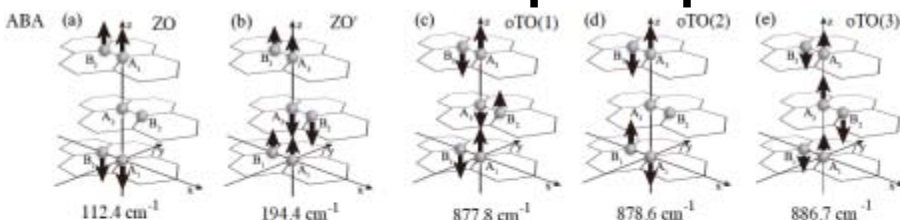


ABA

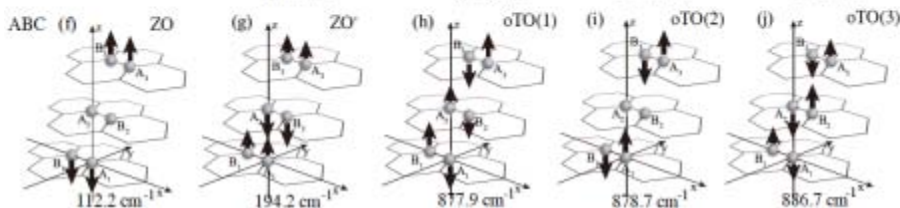


Five different out-of-plane phonons

ABA



ABC

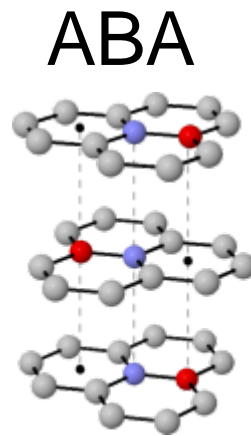
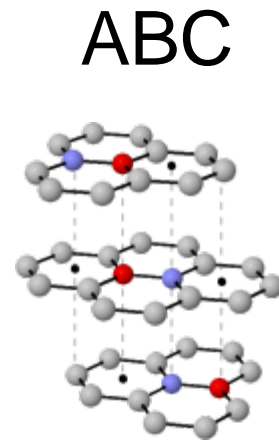
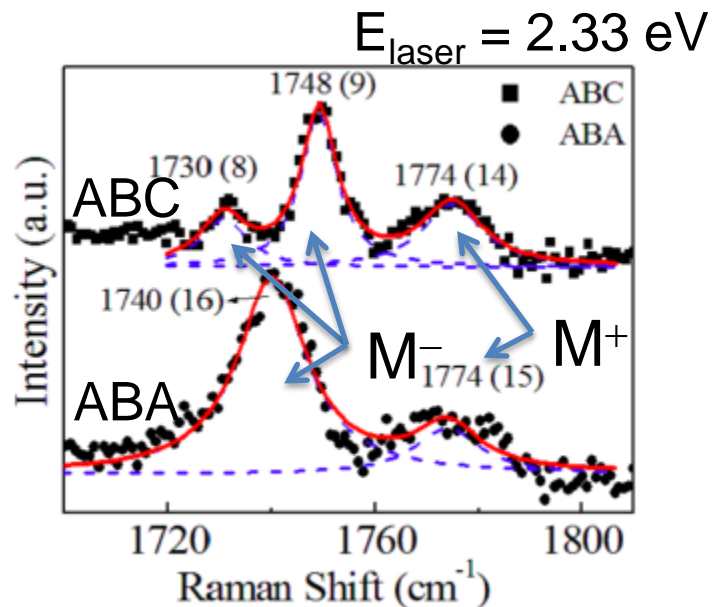
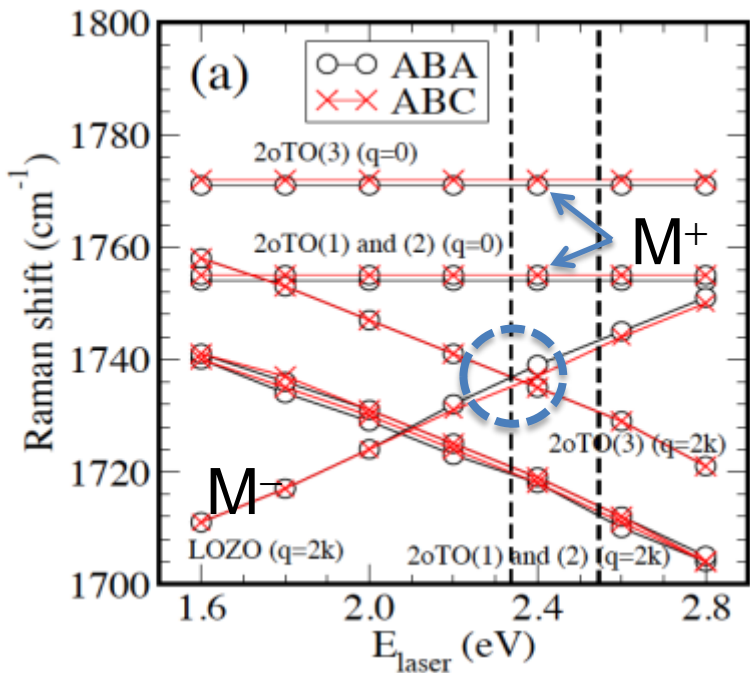


Phonon frequency is the same!



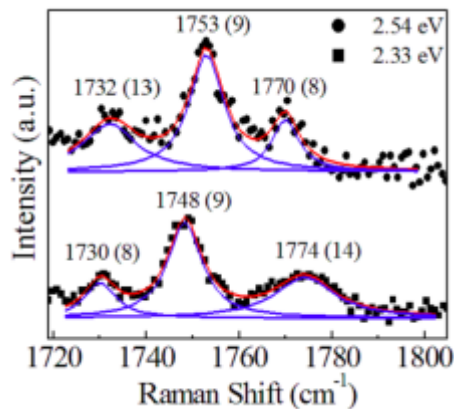
Spectral difference between ABA and ABC

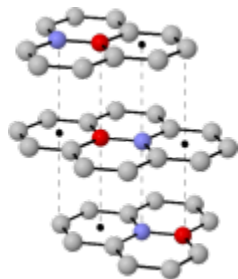
C. Cong et al., ACS Nano 5, 8760 (2011).



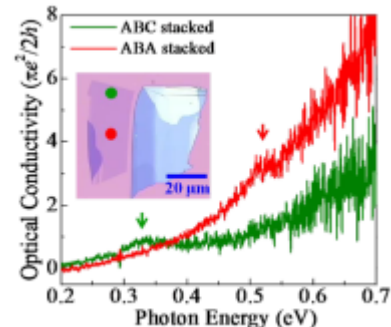
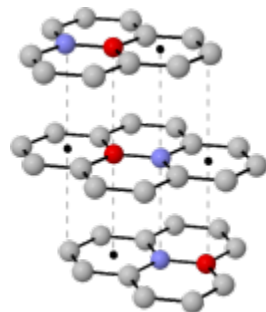
Raman spectra changes as E_{laser} changes
 → double resonance Raman

Around 1740cm^{-1}

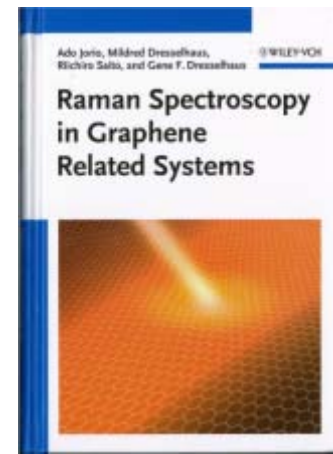
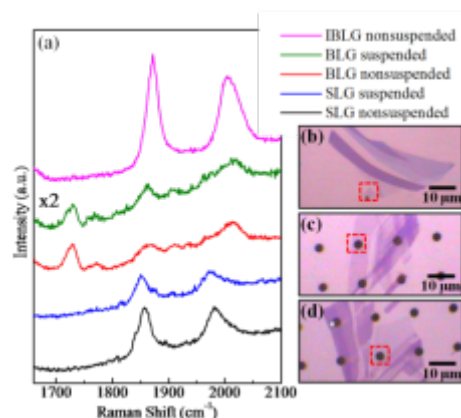
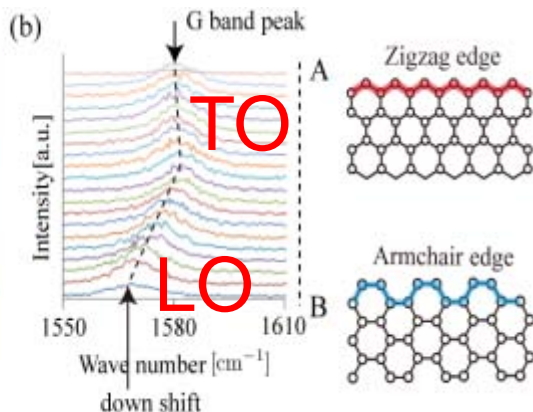
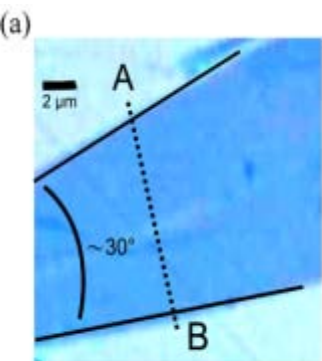
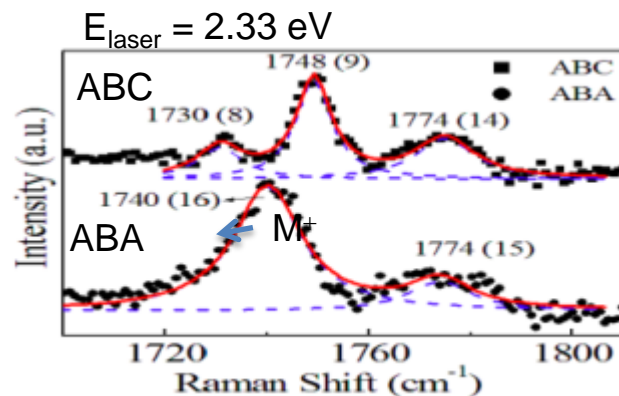




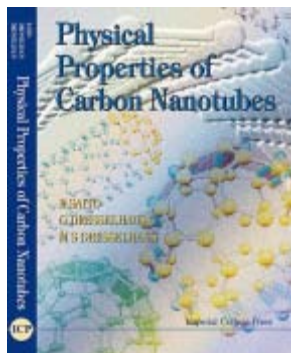
Summary of graphene



- *Stacking order of graphene*
 - $1800-2000\text{cm}^{-1}$ new modes
 - *number of layers. edge shape*
 - *Graphene edge characterization*
 - *ABA and ABC stacking in 3L-G*
 - *Width of G and G' band*
 - *double resonance Raman 1740cm^{-1} peak*



Books and review articles of groups

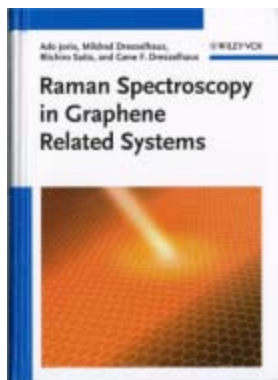


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Adv. in Phys. 60, 413-550, (2011).
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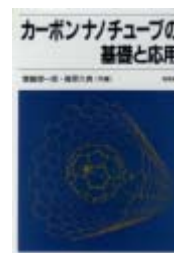


A. Jorio et al.

New. J. Phys. 5, 139.1-17 (2003)



M. A. Pimenta et al.
Phys. Chem. Chem. Phys.
9, 1276 (2007) for D-band



Thank you.