

# Two classes of finite $p$ -groups

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**Abstract.** Assume  $G$  is a finite  $p$ -group.  $G$  is called an  $\mathcal{A}_t$ -group if every subgroup of index  $p^t$  of  $G$  is abelian, but there is at least one non-abelian subgroup of index  $p^{t-1}$ .  $G$  is called a  $\mathcal{C}_t$ -group if  $G$  has at least a cyclic subgroup of index  $p^t$  and all subgroups of index  $p^{t-1}$  of  $G$  are not cyclic. For  $t \leq 3$ ,  $\mathcal{A}_t$ -groups and  $\mathcal{C}_t$ -group are classified. In this talk, we will introduce some application of the classification of  $\mathcal{A}_3$ -groups and some characterizations of  $\mathcal{C}_t$ -groups.

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